

Chapter 2 | Equations and Formulas

2.1 Solving Equations

1. $z + 8 = 50$

$$z + 8 - 8 = 50 - 8 \quad \text{Subtract 8.}$$

$$z = 42$$

2. $r + 13 = 83$

$$r + 13 - 13 = 83 - 13 \quad \text{Subtract 13.}$$

$$r = 70$$

3. $z + 95 = 400$

$$z + 95 - 95 = 400 - 95 \quad \text{Subtract 95.}$$

$$z = 305$$

4. $25 = x + 12$

$$25 - 12 = x + 12 - 12 \quad \text{Subtract 12.}$$

$$13 = x$$

5. $v - 29 = 17$

$$v - 29 + 29 = 17 + 29 \quad \text{Add 29.}$$

$$v = 46$$

6. $312 = m - 40$

$$312 + 40 = m - 40 + 40 \quad \text{Add 40.}$$

$$352 = m$$

7. $10k = 42$

$$\frac{10k}{10} = \frac{42}{10} \quad \text{Divide by 10.}$$

$$k = 4.2$$

8. $7s = 84$

$$\frac{7s}{7} = \frac{84}{7} \quad \text{Divide by 7.}$$

$$s = 12$$

9. $12q = 144$

$$\frac{12q}{12} = \frac{144}{12} \quad \text{Divide by 12.}$$

$$q = 12$$

10. $8z = 136$

$$\frac{8z}{8} = \frac{136}{8} \quad \text{Divide by 8.}$$

$$z = 17$$

11. $60 = 30m$

$$\frac{60}{30} = \frac{30m}{30} \quad \text{Divide by 30.}$$

$$2 = m$$

12. $94 = 2z$

$$\frac{94}{2} = \frac{2z}{2} \quad \text{Divide by 2.}$$

$$47 = z$$

13. $5.9y = 17.7$

$$\frac{5.9y}{5.9} = \frac{17.7}{5.9} \quad \text{Divide by 5.9.}$$

$$y = 3$$

14. $16.5x = 39.6$

$$\frac{16.5x}{16.5} = \frac{39.6}{16.5} \quad \text{Divide by 16.5.}$$

$$x = 2.4$$

15. $1.54 = 0.7y$

$$\frac{1.54}{0.7} = \frac{0.7y}{0.7} \quad \text{Divide by 0.7.}$$

$$2.2 = y$$

16. $3.9a = 15.6$

$$\frac{3.9a}{3.9} = \frac{15.6}{3.9} \quad \text{Divide by 3.9.}$$

$$a = 4$$

17. $3.92w = 3.136$

$$\frac{3.92w}{3.92} = \frac{3.136}{3.92} \quad \text{Divide by 3.92.}$$

$$w = 0.8$$

18. $2.773m = 3.3276$

$$\frac{2.773m}{2.773} = \frac{3.3276}{2.773} \quad \text{Divide by 2.773.}$$

$$m = 1.2$$

19. $0.0002x = 0.08$

$$\frac{0.0002x}{0.0002} = \frac{0.08}{0.0002} \quad \text{Divide by 0.0002.}$$

$$x = 400$$

20. $0.0324 = 0.0135y$
 $\frac{0.0324}{0.0135} = \frac{0.0135y}{0.0135}$ *Divide by 0.0135.*
 $2.4 = y$
21. $\frac{s}{7} = 42$
 $\frac{s}{7} \cdot 7 = 42 \cdot 7$ *Multiply by 7.*
 $s = 294$
22. $\frac{m}{5} = 6$
 $\frac{m}{5} \cdot 5 = 6 \cdot 5$ *Multiply by 5.*
 $m = 30$
23. $\frac{r}{7} = 1$
 $\frac{r}{7} \cdot 7 = 1 \cdot 7$ *Multiply by 7.*
 $r = 7$
24. $\frac{c}{7} = 2$
 $\frac{c}{7} \cdot 7 = 2 \cdot 7$ *Multiply by 7.*
 $c = 14$
25. $\frac{2}{3}b = 8$
 $\frac{3}{2} \cdot \frac{2}{3}b = \frac{3}{2} \cdot 8$ *Multiply by $\frac{3}{2}$.*
 $b = 12$
26. $22 = \frac{5}{4}s$
 $\frac{4}{5} \cdot 22 = \frac{4}{5} \cdot \frac{5}{4}s$ *Multiply by $\frac{4}{5}$.*
 $\frac{88}{5} = s$
 $17.6 = s$
27. $35 = \frac{7}{5}t$
 $\frac{5}{7} \cdot 35 = \frac{5}{7} \cdot \frac{7}{5}t$ *Multiply by $\frac{5}{7}$.*
 $25 = t$
28. $\frac{7}{3}s = 21$
 $\frac{3}{7} \cdot \frac{7}{3}s = \frac{3}{7} \cdot 21$ *Multiply by $\frac{3}{7}$.*
 $s = 9$
29. $2x = \frac{5}{3}$
 $\frac{1}{2} \cdot 2x = \frac{1}{2} \cdot \frac{5}{3}$ *Multiply by $\frac{1}{2}$.*
 $x = \frac{5}{6}$
30. $4y = \frac{1}{3}$
 $\frac{1}{4} \cdot 4y = \frac{1}{4} \cdot \frac{1}{3}$ *Multiply by $\frac{1}{4}$.*
 $y = \frac{1}{12}$
31. $3p = \frac{5}{12}$
 $\frac{1}{3} \cdot 3p = \frac{1}{3} \cdot \frac{5}{12}$ *Multiply by $\frac{1}{3}$.*
 $p = \frac{5}{36}$
32. $\frac{3}{4} = 9a$
 $\frac{1}{9} \cdot \frac{3}{4} = \frac{1}{9} \cdot 9a$ *Multiply by $\frac{1}{9}$.*
 $\frac{1}{12} = a$
33. $7b + 9 = 37$
 $7b + 9 - 9 = 37 - 9$ *Subtract 9.*
 $7b = 28$
 $\frac{7b}{7} = \frac{28}{7}$ *Divide by 7.*
 $b = 4$
34. $4x + 12 = 75$
 $4x + 12 - 12 = 75 - 12$ *Subtract 12.*
 $4x = 63$
 $\frac{4x}{4} = \frac{63}{4}$ *Divide by 4.*
 $x = 15\frac{3}{4} = 15.75$

35. $7y - 23 = 58$
 $7y - 23 + 23 = 58 + 23$ Add 23.
 $7y = 81$
 $\frac{7y}{7} = \frac{81}{7}$ Divide by 7.
 $y = \frac{81}{7} = 11\frac{4}{7}$

36. $12r - 60 = 100$
 $12r - 60 + 60 = 100 + 60$ Add 60.
 $12r = 160$
 $\frac{12r}{12} = \frac{160}{12}$ Divide by 12.
 $r = \frac{40}{3} = 13\frac{1}{3}$

37. $6p + 41.5 = 69.4$
 $6p + 41.5 - 41.5 = 69.4 - 41.5$ Subtract 41.5.
 $6p = 27.9$
 $\frac{6p}{6} = \frac{27.9}{6}$ Divide by 6.
 $p = 4.65$

38. $12.2s + 13.8 = 47.96$
 $12.2s + 13.8 - 13.8 = 47.96 - 13.8$ Subtract 13.8.
 $12.2s = 34.16$
 $\frac{12.2s}{12.2} = \frac{34.16}{12.2}$ Divide by 12.2.
 $s = 2.8$

39. $6c + \frac{3}{4} = 8$
 $6c + \frac{3}{4} - \frac{3}{4} = 8 - \frac{3}{4}$ Subtract $\frac{3}{4}$.
 $6c = \frac{29}{4}$
 $\frac{1}{6} \cdot 6c = \frac{1}{6} \cdot \frac{29}{4}$ Multiply by $\frac{1}{6}$.
 $c = \frac{29}{24} = 1\frac{5}{24}$

40. $5z + \frac{2}{3} = 2$
 $5z + \frac{2}{3} - \frac{2}{3} = 2 - \frac{2}{3}$ Subtract $\frac{2}{3}$.
 $5z = \frac{4}{3}$
 $\frac{1}{5} \cdot 5z = \frac{1}{5} \cdot \frac{4}{3}$ Multiply by $\frac{1}{5}$.
 $z = \frac{4}{15}$

41. $7q - \frac{2}{3} = 4$
 $7q - \frac{2}{3} + \frac{2}{3} = 4 + \frac{2}{3}$ Add $\frac{2}{3}$.
 $7q = \frac{14}{3}$
 $\frac{1}{7} \cdot 7q = \frac{1}{7} \cdot \frac{14}{3}$ Multiply by $\frac{1}{7}$.
 $q = \frac{2}{3}$

42. $7a - \frac{5}{4} = \frac{9}{4}$
 $7a - \frac{5}{4} + \frac{5}{4} = \frac{9}{4} + \frac{5}{4}$ Add $\frac{5}{4}$.
 $7a = \frac{7}{2}$
 $\frac{1}{7} \cdot 7a = \frac{1}{7} \cdot \frac{7}{2}$ Multiply by $\frac{1}{7}$.
 $a = \frac{1}{2}$

43. $5.2z - 4 = 1.2$
 $5.2z - 4 + 4 = 1.2 + 4$ Add 4.
 $5.2z = 5.2$
 $\frac{5.2z}{5.2} = \frac{5.2}{5.2}$ Divide by 5.2.
 $z = 1$

44. $3.6m + 2 = 6.32$
 $3.6m + 2 - 2 = 6.32 - 2$ Subtract 2.
 $3.6m = 4.32$
 $\frac{3.6m}{3.6} = \frac{4.32}{3.6}$ Divide by 3.6.
 $m = 1.2$
45. $27.85 = 3 + 7.1p$
 $27.85 - 3 = 3 - 3 + 7.1p$ Subtract 3.
 $24.85 = 7.1p$
 $\frac{24.85}{7.1} = \frac{7.1p}{7.1}$ Divide by 7.1.
 $3.5 = p$
46. $0.9 = 4t - 3.5$
 $0.9 + 3.5 = 4t - 3.5 + 3.5$ Add 3.5.
 $4.4 = 4t$
 $\frac{4.4}{4} = \frac{4t}{4}$ Divide by 4.
 $1.1 = t$
47. $7m + 4m - 5m = 78$
 $6m = 78$ Combine like terms.
 $\frac{6m}{6} = \frac{78}{6}$ Divide by 6.
 $m = 13$
48. $13r - 7r + 3r = 81$
 $9r = 81$ Combine like terms.
 $\frac{9r}{9} = \frac{81}{9}$ Divide by 9.
 $r = 9$
49. $2s + s + 3s = 12$
 $6s = 12$ Combine like terms.
 $\frac{6s}{6} = \frac{12}{6}$ Divide by 6.
 $s = 2$
50. $3.5k + k + k = 11.55$
 $5.5k = 11.55$ Combine like terms.
 $\frac{5.5k}{5.5} = \frac{11.55}{5.5}$ Divide by 5.5.
 $k = 2.1$
51. $5y + 2 = 3(y + 4)$
 $5y + 2 = 3y + 12$ Distribute.
 $5y + 2 - 2 = 3y + 12 - 2$ Subtract 2.
 $5y = 3y + 10$
 $5y - 3y = 3y - 3y + 10$ Subtract 3y.
 $2y = 10$
 $\frac{2y}{2} = \frac{10}{2}$ Divide by 2.
 $y = 5$
52. $4z + 2 = 2(z + 2)$
 $4z + 2 = 2z + 4$ Distribute.
 $4z + 2 - 2 = 2z + 4 - 2$ Subtract 2.
 $4z = 2z + 2$
 $4z - 2z = 2z - 2z + 2$ Subtract 2z.
 $2z = 2$
 $\frac{2z}{2} = \frac{2}{2}$ Divide by 2.
 $z = 1$
53. $3(m - 4) = m + 2$
 $3m - 12 = m + 2$ Distribute.
 $3m - 12 + 12 = m + 2 + 12$ Add 12.
 $3m = m + 14$
 $3m - m = m - m + 14$ Subtract m.
 $2m = 14$
 $\frac{2m}{2} = \frac{14}{2}$ Divide by 2.
 $m = 7$
54. $s + 8 = 3(s - 6)$
 $s + 8 = 3s - 18$ Distribute.
 $s + 8 + 18 = 3s - 18 + 18$ Add 18.
 $s + 26 = 3s$
 $s - s + 26 = 3s - s$ Subtract s.
 $26 = 2s$
 $\frac{26}{2} = \frac{2s}{2}$ Divide by 2.
 $13 = s$

$$\begin{aligned}
 55. \quad & 4(y+8) = 3(y+14) \\
 & 4y+32 = 3y+42 \quad \text{Distribute.} \\
 4y+32-32 &= 3y+42-32 \quad \text{Subtract 32.} \\
 4y &= 3y+10 \\
 4y-3y &= 3y-3y+10 \quad \text{Subtract 3y.} \\
 y &= 10
 \end{aligned}$$

$$\begin{aligned}
 56. \quad & 7(z-5) = 4(z+8) \\
 7z-35 &= 4z+32 \quad \text{Distribute.} \\
 7z-35+35 &= 4z+32+35 \quad \text{Add 35.} \\
 7z &= 4z+67 \\
 7z-4z &= 4z-4z+67 \quad \text{Subtract 4z.} \\
 3z &= 67 \\
 \frac{3z}{3} &= \frac{67}{3} \quad \text{Divide by 3.} \\
 z &= 22\frac{1}{3}
 \end{aligned}$$

$$\begin{aligned}
 57. \quad & \frac{3}{4}s + \frac{1}{5}s = \frac{4}{5} \\
 \frac{15}{20}s + \frac{4}{20}s &= \frac{4}{5} \\
 \frac{19}{20}s &= \frac{4}{5} \quad \text{Combine like terms.} \\
 \frac{20}{19} \cdot \frac{19}{20}s &= \frac{20}{19} \cdot \frac{4}{5} \quad \text{Multiply by } \frac{20}{19}. \\
 s &= \frac{16}{19}
 \end{aligned}$$

$$\begin{aligned}
 58. \quad & \frac{3}{4}q - \frac{1}{9} = \frac{1}{3} + \frac{1}{4}q \\
 \frac{3}{4}q - \frac{1}{9} + \frac{1}{9} &= \frac{1}{3} + \frac{1}{9} + \frac{1}{4}q \quad \text{Add } \frac{1}{9}. \\
 \frac{3}{4}q &= \frac{3}{9} + \frac{1}{9} + \frac{1}{4}q \\
 \frac{3}{4}q &= \frac{4}{9} + \frac{1}{4}q \\
 \frac{3}{4}q - \frac{1}{4}q &= \frac{4}{9} + \frac{1}{4}q - \frac{1}{4}q \quad \text{Subtract } \frac{1}{4}q. \\
 \frac{1}{2}q &= \frac{4}{9} \\
 \frac{2}{1} \cdot \frac{1}{2}q &= \frac{2}{1} \cdot \frac{4}{9} \quad \text{Multiply by } \frac{2}{1}. \\
 q &= \frac{8}{9}
 \end{aligned}$$

$$\begin{aligned}
 59. \quad & \frac{3}{8}y + \frac{1}{4} = \frac{9}{8}y - \frac{1}{4} \\
 \frac{3}{8}y + \frac{1}{4} + \frac{1}{4} &= \frac{9}{8}y - \frac{1}{4} + \frac{1}{4} \quad \text{Add } \frac{1}{4}. \\
 \frac{3}{8}y + \frac{1}{2} &= \frac{9}{8}y \\
 \frac{3}{8}y - \frac{3}{8}y + \frac{1}{2} &= \frac{9}{8}y - \frac{3}{8}y \quad \text{Subtract } \frac{3}{8}y. \\
 \frac{1}{2} &= \frac{3}{4}y \\
 \frac{4}{3} \cdot \frac{1}{2} &= \frac{4}{3} \cdot \frac{3}{4}y \quad \text{Multiply by } \frac{4}{3}. \\
 \frac{2}{3} &= y
 \end{aligned}$$

$$\begin{aligned}
 60. \quad & 3(2p-1) = 4(2.2-p) \\
 6p-3 &= 8.8-4p \quad \text{Distribute.} \\
 6p-3+3 &= 8.8+3-4p \quad \text{Add 3.} \\
 6p &= 11.8-4p \\
 6p+4p &= 11.8-4p+4p \quad \text{Add 4p.} \\
 10p &= 11.8 \\
 \frac{10p}{10} &= \frac{11.8}{10} \quad \text{Divide by 10.} \\
 p &= 1.18
 \end{aligned}$$

$$\begin{aligned}
 61. \quad & 2(y+1) = 4(4-2.5y) \\
 2y+2 &= 16-10y \quad \text{Distribute.} \\
 2y+10y+2 &= 16-10y+10y \quad \text{Add 10y.} \\
 12y+2 &= 16 \\
 12y+2-2 &= 16-2 \quad \text{Subtract 2.} \\
 12y &= 14 \\
 \frac{12y}{12} &= \frac{14}{12} \quad \text{Divide by 12.} \\
 y &= 1\frac{2}{12} = 1\frac{1}{6}
 \end{aligned}$$

$$\begin{aligned}
 62. \quad & 9.1765y + 0.3284y = 6.65343 \\
 9.5049y &= 6.65343 \\
 & \text{Combine like terms.} \\
 \frac{9.5049y}{9.5049} &= \frac{6.65343}{9.5049} \\
 & \text{Divide by 9.5049.} \\
 y &= 0.7
 \end{aligned}$$

63. $0.7452(3k-1) = 3.94956$
 $2.2356k - 0.7452 = 3.94956$
Distribute.
 $2.2356k - 0.7452 + 0.7452 = 3.94956 + 0.7452$
Add 0.7452.
 $2.2356k = 4.69476$

$$\frac{2.2356k}{2.2356} = \frac{4.69476}{2.2356}$$

Divide by 2.2356.
 $k = 2.1$

64. $0.3255(1 + 7.5s) = 6.67275$
 $0.3255 + 2.44125s = 6.67275$
Distribute.
 $0.3255 - 0.3255 + 2.44125s = 6.67275 - 0.3255$
Subtract 0.3255.
 $2.44125s = 6.34725$

$$\frac{2.44125s}{2.44125} = \frac{6.34725}{2.44125}$$

Divide by 2.44125.
 $s = 2.6$

65. $1.2(2 + 3r) = 0.8(2r + 5)$
 $2.4 + 3.6r = 1.6r + 4$ *Distribute.*
 $2.4 - 2.4 + 3.6r = 1.6r + 4 - 2.4$ *Subtract 2.4.*
 $3.6r = 1.6r + 1.6$
 $3.6r - 1.6r = 1.6r - 1.6r + 1.6$ *Subtract 1.6r.*
 $2r = 1.6$

$$\frac{2r}{2} = \frac{1.6}{2}$$
 Divide by 2.
 $r = 0.8$

66. Answers will vary.

67. Answers will vary.

68. Answers will vary.

2.2 Applications of Equations

1. 27 plus a number
 $27 + x$

2. the sum of a number and $16\frac{1}{2}$
 $x + 16\frac{1}{2}$

3. a number added to 22
 $22 + x$

4. 6.8 added to a number
 $6.8 + x$

5. 4 less than a number
 $x - 4$

6. 12 fewer than a number
 $x - 12$

7. subtract $3\frac{1}{2}$ from a number
 $x - 3\frac{1}{2}$

8. subtract a number from 5.4
 $5.4 - x$

9. triple a number
 $3x$

10. the product of a number and 9
 $9x$

11. three-fifths of a number
 $\frac{3}{5}x$

12. four-thirds of a number
 $\frac{4}{3}x$

13. the quotient of 9 and a number
 $\frac{9}{x}$

14. the quotient of a number and 11
 $\frac{x}{11}$