Chapter 1 Even Solutions

Section 1.1

- **2.** B is a function of A. The domain is 10, 10.5, 13, 15, 16, 20}. The range is {3, 4, 9, 13, 23}.
- **4.** B is a function of A. The domain is {2, 4, 6, 8, 10, 12}. The range is {3}.
- **6.** f(2) = 9; if f(x) = 2, then x is 0 or 1.
- **8.** f(2) = 2; if f(x) = 2, then x is -4, -1, 0, 2, 10 or 17.
- 10. (a) Cost is a function of age because each age is associated with only one cost.
- **(b)** Age is not a function of cost because costs \$45 and \$90 are associated with more than one age.
- **12.** (a) For the given height, BMI is a function of weight in pounds because each weight input has only one BMI output.
- **(b)** For the given height, weight in pounds is a function of BMI because each BMI input has only one weight output.

Section 1.2

2.

B is not a function of A because the input 5 has two output values; two points lie on the same vertical line.

- **4.** The graph does not represent a function because the input 4 has 6 different output values
- **6.** The graph represents a function each input value has only one output value. The domain is [-4, 4], and the range is [0, 16].
- **8.** f(2) = -1; if f(x) = 2, then x is 0 or 3.
- **10.** f(2) = 1; there is no value of x for which f(x) = 2.
- **12.** Length of growing season is a function of latitude, because each latitude has only one length of growing season.

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- **14.** (a) The domain (in years) is [0, 25].
- **(b)** The range (in thousands of dollars) is [1.8, 43.4].

- (c) The price of a 10-year-old Corvette is about \$15 thousand.
- (d) A Corvette that costs 10 thousand dollars is about 12 years old.
- **16.** (a) The domain (in calendar years) is [1985, 2003].
- **(b)** The range (in millions of cases) is approximately [200, 380].
- (c) 250 million cases were sold in 2001 or 2002.
- (d) In 1994 about 310 million cases were sold.

Section 1.3

- **2.** The independent variable is u; the dependent variable is T. In function notation we have T(u) = 4u 7.
- **4.** The independent variable is e; the dependent variable is V. In function notation we have $V(e) = e^3$.
- **6.** y is a function of x because number of hamburgers has only one cost.
- **8.** y is a function of x because each real number x has only one square.
- **10.** *y* is a function of *x* because each real number *x* is associated with only one value of *y*.
- **12.** $f(-1) = (-1)^2 + 1 = 2$; $f(0.5) = (0.5)^2 + 1 = 1.25$; $f(\sqrt{2}) = (\sqrt{2})^2 + 1 = 3$.
- **14.** $f(-1) = \sqrt{(-1)^2 + 2} = \sqrt{3}$; $f(0.5) = \sqrt{(0.5)^2 + 2} = 1.5$; $f(\sqrt{2}) = \sqrt{(\sqrt{2})^2 + 2} = 2$.
- **16.** $\sqrt{5x+4} = 13 \rightarrow 5x+4=169 \rightarrow 5x=165 \rightarrow x=33$.
- **18.** Both the domain and the range of h(x) are the set of real numbers.
- **20.** The domain is the set of real numbers; the range is $[7, \infty]$.
- **22.** (a) E(d) = 0.820150d
- **(b)** $E(475) = 0.820150 \cdot 475 = 389.571$ Euros.
- (c) $0.820150d = 492.09 \rightarrow d = 600$ dollars.
- (d) Domain = Range = $[0, \infty]$.

- **24.** (a) Postage rate is a function of weight because each weight is associated with only one postage rate.
- (b) Both 6.9 and 7 ounces letters cost $\$0.37 + 6 \cdot \$0.23 = \$1.75$. A 7.1-ounce letter costs an additional \$0.23, or \$1.98.
- (c) \$1.06 \$0.37 = \$0.69, so the letter weighs up to 3 "additional" ounces. The letter weighs over 3 ounces, but not more than 4 ounces.

$$R(w) = \begin{cases} \$0.37 \text{ if } 0 < w \le 1 \\ \$0.60 \text{ if } 1 < w \le 2 \\ \$0.83 \text{ if } 2 < w \le 3 \\ \$1.06 \text{ if } 3 < w \le 4 \\ \$1.29 \text{ if } 4 < w \le 5 \\ \$1.52 \text{ if } 5 < w \le 6 \end{cases}$$
$$\$1.75 \text{ if } 6 < w \le 7 \\ \$1.98 \text{ if } 7 < w \le 8 \\ \$2.21 \text{ if } 8 < w \le 9 \\ \$2.44 \text{ if } 9 < w \le 10 \\ \$2.67 \text{ if } 10 < w \le 11 \\ \$2.90 \text{ if } 11 < w \le 12 \\ \$3.13 \text{ if } 12 < w \le 13 \end{cases}$$

(e) The domain (in ounces) is (0, 13]; the range (in dollars) is {0.37, 0.60, 0.83, 1.06, 1.29, 1.52, 1.75, 1.98, 2.21, 2.44, 2.67, 2.90, 3.13}.

Section 1.4

- **2.** The function is increasing on [-6, 5]; the function is not decreasing.
- **4.** The function is increasing on [0, 4], and decreasing on [4, 8].

6.		
х	f(x)	Δf
		Δx
0	25	1
5	30	0.8
10	34	-0.2
15	33	-0.2
20	32	

The average rate of change is decreasing on [0, 10] and constant on [10, 20].

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х	f(x)	Δf
		Δx
-1	18	-3
0	15	-1.5
4	9	-1.286 *
11	0	-1
23	-12	

^{*}correct to 3 decimal places

The average rate of change is decreasing on [-1, 23].

10. The function is on increasing [1995, 1999] and [2001, 2003]; the function is constant on [1993, 1995] and [1999, 2001].

12. The average rate of change is shown in the table below.

Year	Number	$\Delta Number$
		$\Delta Year$
1997	878	43
1998	921	58
1999	979	125
2000	1104	109
2001	1213	91
2002	1304	45
2003	1349	7
2004	1356	

- (a) The number of new cases is increasing at an increasing on [1997, 2000].
- (d) The number of new cases is increasing at a decreasing on [2000, 2004].