CHAPTER 1 WHOLE NUMBERS

1.1 Reading and Writing Whole Numbers

1.1 Margin Exercises

1. **(a)** 342

4 is in the tens place.

(b) 714

4 is in the *ones* place.

(c) 479

4 is in the *hundreds* place.

2. The place value of each digit:

(a) 14,218; ones: 8; tens: 1; hundreds: 2;

thousands: 4; ten-thousands: 1

(b) 460,329; ones: 9; tens: 2; hundreds: 3;

thousands: 0; ten-thousands: 6;

hundred-thousands: 4

3. The digits in each period (group) of 3,251,609,328:

- (a) 3 is in the billions period.
- **(b)** 251 is in the millions period.
- (c) 609 is in the thousands period.
- (d) 328 is in the ones period.
- **4. (a)** 18 is eighteen.
 - **(b)** 36 is thirty-six.
 - (c) 418 is four hundred eighteen.
 - (d) 902 is nine hundred two.
- **5.** (a) 3104 is three <u>thousand</u>, one <u>hundred</u> four.
 - **(b)** 95,372 is ninety-five <u>thousand</u>, three hundred seventy-two.
 - **(c)** 100,075,002 is one hundred million, seventy-five thousand, two.
 - **(d)** 11,022,040,000 is eleven billion, twenty-two million, forty thousand.
- **6. (a)** One thousand, four hundred thirty-seven is 1437.
 - **(b)** Nine hundred seventy-one thousand, six is 971,006.
 - **(c)** Eighty-two million, three hundred twenty-five is 82,000,325.

- 7. (a) The U.S. population in the 2010 column is 309 million and is written in digits as 309,000,000.
 - **(b)** The estimated U.S. population in the 2020 column is 338 million and is written in digits as 338,000,000.
 - **(c)** The household income in 1990 was \$42,936 and is written in words as forty-two thousand, nine hundred thirty-six dollars.
 - **(d)** The estimated average yearly salary in 2020 is \$32,080 and is written in words as thirty-two thousand, eighty dollars.

1.1 Section Exercises

- 1. The digit in the hundreds place in the whole number 3065 is 0. Choice C
- 2. The digit in the ten-thousands place in the whole number 134,681 is 3. Choice **B**
- **3.** 18,015; ten-thousands: 1; hundreds: 0
- **4.** 86,332; ten-thousands: 8; ones: 2
- **5.** 7,62<u>8,592,183; millions: 8; thousands: 2</u>
- **6.** $\underline{1},70\underline{0},225,016$; billions: 1; millions: 0
- 7. The digits in the thousands period in the whole number 552,687,318 are 687.
- **8.** The digits in the millions period in the whole number 974,321,876,528 are 321.
- **9.** 3,561,435; millions: 3; thousands: 561; ones: 435
- **10.** <u>100,258,100,006</u>; billions: 100; millions: 258; thousands: 100; ones: 6
- **11.** Evidence suggests that this is true. It is common to count using fingers.
- **12.** No doubt there is a relationship here. One answer might be that people could count using their fingers and toes and, therefore, thought of them as numbers or digits.
- **13.** 23,115 is twenty-three thousand, one hundred fifteen. The statement is *false* (no "and").
- **14.** 37,886 is thirty-seven thousand, eight hundred eighty-six. The statement is *true*.
- **15.** 346,009 is three hundred forty-six thousand, nine.
- **16.** 218,033 is two hundred eighteen <u>thousand</u>, thirty-three.
- **17.** 25,756,665 is twenty-five million, seven hundred fifty-six thousand, six hundred sixty-five.
- **18.** 999,993,000 is nine hundred ninety-nine million, nine hundred ninety-three thousand.

- 19. Sixty-three thousand, one hundred sixty-three is 63,163.
- **20.** Ninety-five thousand, one hundred eleven is 95,111.
- **21.** Ten million, two hundred twenty-three is 10,000,223.
- **22.** One hundred million, two hundred is 100,000,200.
- **23.** Three million, two hundred thousand in digits is 3,200,000.
- **24.** Two hundred forty-three thousand in digits is 243,000.
- **25.** Fifty million, fifty-one thousand, five hundred seven in digits is 50,051,507.
- **26.** One hundred forty-six billion, three hundred eighty-five million in digits is 146,385,000,000.
- **27.** Fifty-four million, seven hundred fifty thousand in digits is 54,750,000.
- **28.** Two hundred twenty-one thousand in digits is 221,000.
- **29.** Eight hundred trillion, six hundred twenty-one million, twenty thousand, two hundred fifteen in digits is 800,000,621,020,215.
- **30.** 2,153,896,448 is two billion, one hundred fifty-three million, eight hundred ninety-six thousand, four hundred forty-eight.
- **31.** The least used method of transportation is public transportation. 6,069,589 in words is six million, sixty-nine thousand, five hundred eighty-nine.
- **32.** From the table, "drive alone" is the method of transportation most used. 84,215,298 written out is eighty-four million, two hundred fifteen thousand, two hundred ninety-eight.
- **33.** The number of people who walk to work or work at home is 7,894,911. In words, 7,894,911 is written as seven million, eight hundred ninety-four thousand, nine hundred eleven.
- **34.** From the table, the number of people who carpool is 15,377,634. Written in words, 15,377,634 is fifteen million, three hundred seventy-seven thousand, six hundred thirty-four.

1.2 Adding Whole Numbers

1.2 Margin Exercises

- 1. (a) 2+6=8; 6+2=8
 - **(b)** 9+5=14; 5+9=14

- (c) 4+7=11; 7+4=11
- (d) 6+9=15; 9+6=15
- **2.** (a) 3

$$8 \quad 3 + 8 = 11$$

$$5 \quad 11 + 5 = 16$$

$$4 \quad 16 + 4 = 20$$

$$\frac{+6}{26}$$
 $20+6=26$

(b) 5

$$6 \quad 5+6=11$$

$$3 \quad 11 + 3 = 14$$

$$2 \quad 14 + 2 = 16$$

$$\frac{+4}{20} \ 16 + 4 = 20$$

(c) 9

$$6 \quad 9+6=15$$

$$8 \quad 15 + 8 = 23$$

$$7 \quad 23 + 7 = 30$$

$$\frac{+3}{33} \ 30 + 3 = 33$$

(d) 3

$$8 \quad 3 + 8 = 11$$

$$6 \quad 11 + 6 = 17$$

$$4 \quad 17 + 4 = 21$$

$$\frac{+8}{29}$$
 21 + 8 = 29

3. **(a)** 26 + 73

(b) 534

$$\frac{+265}{799}$$

(c) 42,305

$$+11,563$$

53,868

4. (a)
$$\frac{1}{66}$$
 $+ 27$ 6 ones and 7 ones = 13 ones

(b) $\frac{1}{5}8$

$$\frac{+33}{91}$$
 8 ones and 3 ones = 11 ones

(c) $\frac{1}{5}$

$$\frac{+37}{93}$$
 6 ones and 7 ones = 13 ones

(d)
$$\frac{1}{34}$$

+ 49 4 ones and 9 ones = 13 ones

5. (a)
$$\begin{array}{r}
121 \\
162 \\
4271 \\
372 \\
+8976 \\
\hline
13,781
\end{array}$$

(b)
$$\begin{array}{c} 2 & 21 \\ 7 & 821 \\ 435 \\ 72 \\ 305 \\ \underline{+1693} \\ 10,326 \end{array}$$

(b)
$$15,829$$
 765
 78
 15
 9
 7
 $+13,179$
 $29,882$

- 7. The shortest route from Lake Buena Vista to Conway is as follows:
 - 4 Lake Buena Vista to Resort Area
 - 6 Resort Area to Pine Castle
 - 3 Pine Castle to Belle Isle
 - + $\underline{6}$ Belle Isle to Conway
 - 19 miles
- **8.** The next shortest route from Orlando to Clear Lake is as follows:
 - 5 Orlando to Pine Hills
 - 8 Pine Hills to Altamonte Springs
 - 5 Altamonte Springs to Casselberry
 - 6 Casselberry to Bertha
 - 7 Bertha to Winter Park
 - +7 Winter Park to Clear Lake miles

The amount of fencing needed is 1646 feet, which is the perimeter of (distance around) the project.

1.2 Section Exercises

1.
$$43 + 54 \over 97$$

2.
$$18 + 11 \over 29$$

4.
$$83 + 15 \over 98$$

5.
$$317 + 572 \over 889$$

6.
$$574 \\
+ 325 \\
\hline
899$$

798

14. Line up:
$$3241$$
 1513
 $+2014$
 6768 correct

15. Line up:
$$12,142$$

$$43,201$$

$$+ 23,103$$

$$\overline{78,446}$$

19. Line up:
$$38,204 \\ +21,020 \\ \hline 59,224$$

22.
$$19$$
+ 92
111 (101 is incorrect.)

24.
$$\begin{array}{r} \frac{1}{37} \\ +85 \\ \hline 122 \text{ (132 is incorrect.)} \end{array}$$

25.
$$\frac{1}{47}$$
 $+ 74$
 $121 \text{ (111 is incorrect.)}$

26.
$$\begin{array}{r} 1\\ 97\\ +79\\ \hline 176 \end{array}$$

27.
$$\begin{array}{r} 1 \\ 67 \\ +78 \\ \hline 145 \end{array}$$

28.
$$\begin{array}{r} \frac{1}{96} \\ +47 \\ \hline 143 \end{array}$$

29.
$$\begin{array}{r} \frac{1}{73} \\ +29 \\ \hline 102 \end{array}$$

30.
$$\begin{array}{r} \frac{1}{68} \\ +37 \\ \hline 105 \end{array}$$

31.
$$7\overset{1}{4}6$$

$$+905$$

$$1651$$

32.
$$6\frac{1}{21}$$
 $+359$
 $\overline{980}$

33.
$$306$$
 $+848$
 1154

34.
$$798$$
 $+206$
 1004

35.
$$\begin{array}{r}
11 \\
278 \\
+135 \\
\hline
413
\end{array}$$

36.
$$172$$
 $+156$
 328

37.
$$9\frac{1}{28}$$
 $+843$
 1771

38.
$$\begin{array}{r}
11 \\
686 \\
+726 \\
\hline
1412
\end{array}$$

39.
$$\begin{array}{r} \frac{11}{526} \\ +884 \\ \hline 1410 \end{array}$$

40.
$$116$$
 $+897$
 1013

41.
$$\begin{array}{r} \frac{1}{3}5\frac{1}{7}4\\ +2817\\ \hline 6391 \end{array}$$

43.
$$7896$$
 $+ 3728$
 $11,624$

44.
$$9\frac{1}{3}82$$
 $+ 7586$ $16,968$

45.
$$\begin{array}{r}
 111 \\
 9625 \\
 + 7986 \\
 \hline
 17,611
\end{array}$$

46.
$$\begin{array}{r}
1 & 1 \\
5 & 718 \\
5 & 623 \\
+ & 7 & 436 \\
\hline
18,777
\end{array}$$

47.
$$9 \overset{22}{056}$$

$$78$$

$$6 089$$

$$+ 731$$

$$15,954$$

49.
$$\begin{array}{r}
112\\
708\\
9286\\
+636\\
\hline
10,648
\end{array}$$

50.
$$\begin{array}{r}
211\\
1708\\
321\\
61\\
+8926\\
\hline
11,016
\end{array}$$

52.
$$6 \stackrel{12}{505}$$
 173
 7044
 $+ 168$
 $13,890$

54.
$$\begin{array}{c} 212\\ 7631\\ 5983\\ 7\\ 36\\ +505\\ \hline 14,162\\ \end{array}$$

55.
$$\begin{array}{r}
1129 \\
63 \\
16 \\
3 \\
+ 9887 \\
\hline
12,078
\end{array}$$

56.
$$\begin{array}{r}
113\\
322\\
6508\\
93\\
745\\
18\\
+2005\\
\hline
9691
\end{array}$$

57.
$$233 \\
97 \\
2772 \\
437 \\
63 \\
+ 328 \\
\hline
4250$$

58.
$$\begin{array}{r}
223\\
3187\\
810\\
527\\
76\\
2665\\
+317\\
\hline
7582
\end{array}$$

59.
$$\begin{array}{r}
2 & 1 & 2 \\
4 & 1 & 3 \\
8 & 5 \\
9 & 9 & 1 & 9 \\
6 & 0 & 2 \\
3 & 1 \\
+ & 1 & 2 & 1 & 8 \\
\hline
12,268 & 3
\end{array}$$

$$\begin{array}{c} \textbf{60.} & \begin{array}{r} 3\,32\\ 5\,76\\ 7\,934\\ 60\\ 7\,81\\ 5\,968\\ \underline{+\quad371}\\ 15,690 \end{array}$$

61. Add up to check addition.

62. Add up to check addition.

63. Add up to check addition.

64. Add up to check addition.

65. Add up to check addition.

66. Add up to check addition.

11,583
3628
72
564
+7319
11,583 correct

67. Add up to check addition.

```
11,577

678

7 952

56

718

+ 2 173

11,377 incorrect; should be 11,577
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68. Add up to check addition.

```
11,212

516

8 760

24

189

+ 1 723

11,212 correct
```

69. Add up to check addition.

14,332	
4714	
27	
77	
8878	
+636	
14,332	correct

70. Add up to check addition.

71. Changing the order in which numbers are added does not change the sum. You can add from bottom to top when checking addition.

72. Grouping the addition of numbers in any order does not change the sum. You can add numbers in any order. For example, you can add pairs of numbers that add to 10.

73. The shortest route between Southtown and Rena is through Thomasville.

74. The shortest route from Elk Hill to Oakton is through Thomasville.

75. The shortest route between Thomasville and Murphy is through Rena and Austin.

76. The shortest route from Murphy to Thomasville is through Austin and Rena.

77. \$3482 flea market +12,860 annual auction \$16,342 total amount raised

$$\begin{array}{c|cccc} \textbf{78.} & 185 & \textit{hot dogs} \\ & +129 & \textit{hamburgers} \\ \hline & 314 & \textit{total items sold} \end{array}$$

80.
$$283$$
 employees $+218$ employees 501 total employees

$$\begin{array}{ccc} \textbf{81.} & 13,786 & \textit{on-campus day} \\ & 3\,497 & \textit{on-campus night} \\ & + 2\,874 & \textit{on-line} \\ \hline & 20,157 & \textit{total students} \end{array}$$

83. To find the perimeter, add the lengths of the 4 sides in any order.



970 feet is the total distance around the lot.

84. To find the perimeter, add the lengths of the 4 sides in any order.

Maria will need 160 feet of gutters.

85. To find the perimeter, add the lengths of the 3 sides in any order.

$$\begin{array}{r}
30 \\
24 \\
+ 18 \\
\hline
72
\end{array}$$
 feet

Martin will need 72 feet of lumber.

86. To find the perimeter, add the lengths of the 4 sides in any order.

$$\begin{array}{r}
 465 \\
 573 \\
 498 \\
 + 573 \\
 \hline
 2109 \quad \text{meters}
 \end{array}$$

2109 meters of fencing will be needed.

Relating Concepts (Exercises 87–94)

- 87. The largest four-digit number possible, using the digits 4, 1, 9, and 2 each once, will begin with the largest digit in the thousands place and the remaining digits will descend in size until the smallest digit is in the ones place. Therefore, the largest four-digit number possible is 9421.
- **88.** The smallest four-digit number possible, using the digits 4, 1, 9, and 2 each once, will begin with the smallest digit in the thousands place and the remaining digits will ascend in size until the largest digit is in the ones place. Therefore, the smallest four-digit number possible is 1249.
- **89.** The largest five-digit number possible, using the digits 6, 2, and 7 at least once, will use the largest digit in the ten-thousands, thousands, and hundreds

- place and the remaining digits will descend in size until the smallest digit is in the ones place. Therefore, the largest five-digit number possible is 77,762.
- 90. The smallest five-digit number possible, using the digits 6, 2, and 7 at least once, will use the smallest digit in the ten-thousands, thousands, and hundreds place and the remaining digits will ascend in size until the largest digit is in the ones place. Therefore, the smallest five-digit number possible is 22,267.
- **91.** The largest seven-digit number possible is 9,994,433.
- **92.** The smallest seven-digit number possible is 3,334,499.
- **93.** To write the largest seven-digit number possible, using the digits 4, 3, and 9, and using each digit at least twice, write the largest digits on the left, and use the smaller digits as you move right.
- **94.** To write the smallest seven-digit number possible, using the digits 4, 3, and 9, and using each digit at least twice, write the smallest digits on the left, and use the larger digits as you move right.

1.3 Subtracting Whole Numbers

1.3 Margin Exercises

1. (a) 8+2=10:

$$10 - \underline{2} = 8$$
 or $10 - \underline{8} = \underline{2}$

(b) 7+4=11:

$$11 - 7 = 4$$
 or $11 - 4 = 7$

(c) 15 + 22 = 37:

$$37 - 15 = 22$$
 or $37 - 22 = 15$

(d) 23 + 55 = 78:

$$78 - 55 = 23$$
 or $78 - 23 = 55$

2. (a) 7-5=2:

$$7 = 5 + 2$$
 or $7 = 2 + 5$

(b) 9 - 4 = 5:

$$9 = 4 + 5$$
 or $9 = 5 + 4$

(c) 21 - 15 = 6:

$$21 = 15 + 6$$
 or $21 = 6 + 15$

(d) 58 - 42 = 16:

$$58 = 42 + 16$$
 or $58 = 16 + 42$

3. (a) 74 4 ones - 3 ones = 1 one-43 7 tens - 4 tens = 3 tens

(b)
$$68 \quad 8 \text{ ones} - 4 \text{ ones} = 4 \text{ ones}$$

 $-24 \quad 6 \text{ tens} - 2 \text{ tens} = 4 \text{ tens}$

(c)
$$429$$

$$-318$$

$$111$$

(d)
$$3927$$

$$-2614$$

$$1313$$

4. (a)
$$76$$
 45 -45 Subtraction $+31$ Addition 76 problem

Match: 31 is correct.

Not a match: 21 is incorrect.

Rework.

Match: 31 is correct.

Not a match: 113 is incorrect.

Rework.

Match: 123 is correct.

Match: 3230 is correct.

5. **(a)**
$$5.8 \\ -1.9 \\ \hline 3.9$$

(b)
$$\begin{array}{c} 716 \\ 86 \\ -38 \\ \hline 48 \end{array}$$

(d)
$$863$$
 -47 816

(e)
$$76\frac{512}{2}$$

$$-157$$

$$605$$

6. (a)
$$927$$

$$-43$$

$$884$$

(b)
$$\begin{array}{c} 51615 \\ 67 \\ \hline 589 \\ \end{array}$$

(c)
$$\begin{array}{r} 31617 \\ 477 \\ \hline -389 \\ \hline 88 \end{array}$$

(d)
$$\begin{array}{c} 0131017 \\ 1417 \\ - 988 \\ \hline 429 \end{array}$$

(e)
$$\begin{array}{r}
71613 \\
8739 \\
-3892 \\
\hline
4847
\end{array}$$

7. (a)
$$\begin{array}{c} 1\ \cancel{0}\ 16 \\ 2\ \cancel{0}\ \cancel{6} \\ \hline -1\ 7\ 7 \\ \hline 2\ 9 \end{array}$$

8. (a)
$$\begin{array}{c} 2\frac{9}{1018} \\ 308 \\ -159 \\ \hline 149 \end{array}$$

(b)
$$5 7 0 0 - 368 \over 202$$

(c)
$$\begin{array}{r}
0.141610 \\
1.570 \\
-0.983 \\
\hline
5.87
\end{array}$$

9. (a)
$$357$$
 168 -168 $+189$ 357 357

Match: 189 is correct.

Not a match: 252 is incorrect.

Rework.

Match: 242 is correct.

Match: 5887 is correct.

10. (a)
$$\$54,861$$
 Associate of Arts degree $-33,435$ Not a high school graduate

(b)
$$\$82,197$$
 Bachelor's degree
 $-54,861$ Associate of Arts degree
 $\$27,336$ More earnings

1.3 Section Exercises

1.
$$48$$
 Check 16 -32 $+32$ 48

2.
$$17$$
 Check $\frac{4}{-13}$ $\frac{+13}{17}$

3. 86 Check 53
$$\frac{-53}{33}$$
 $\frac{+33}{86}$

4.
$$78$$
 Check $\frac{35}{43}$ $\frac{+43}{78}$

5. 77 Check 60
$$\frac{-60}{17}$$
 $\frac{+17}{77}$

6. 87 Check 63
$$\frac{-63}{24}$$
 $\frac{+24}{87}$

7.
$$335$$
 Check 213 -122 213 335

8.
$$602$$
 Check 301 -301 301 602 602

10. 888 **Check** 215
$$-215$$
 -673 -888

11.
$$7352$$
 Check 241 -241 7111 7352

$$\begin{array}{ccccc} \textbf{12.} & 4420 & \textbf{Check} & 4110 \\ & -310 & & +310 \\ \hline & 4110 & & 4420 \end{array}$$

14.
$$1875$$
 Check 1362

$$-1362 + 513$$

$$513 - 1875$$

15.
$$6259$$
 Check 4148

$$-4148$$

$$2111$$

$$6259$$

$$6259$$

16. 9654 Check 4323
$$-4323$$
 $+5331$ 9654

17.
$$24,392$$
 Check $13,160$ $-11,232$ $+11,232$ $24,392$

19.
$$46,253$$
 Check $41,110$

$$-5143$$

$$41,110$$

$$46,253$$

$$46,253$$

21.
$$54$$
 Check 42 -42 12 54 correct

22.
$$87$$
 Check 43 -43 44 87 correct

23. 89 Check 63
$$\frac{-27}{63}$$
 $\frac{+27}{90}$ incorrect

Rework.

$$\begin{array}{ccc}
89 & \text{Check} & 62 \\
-27 & & +27 \\
\hline
62 & & 89 & \text{correct}
\end{array}$$

24.
$$\begin{array}{ccc} 47 & \text{Check} & 13 \\ -35 & & +35 \\ \hline 13 & & 48 & \text{incorrect} \end{array}$$

Rework.

Rework.

26.
$$754$$
 Check 342

$$-342$$

$$412$$

$$-754$$
 correct

27.
$$4683$$
 Check 3542

$$-3542$$

$$1141$$

$$+1141$$

$$4683$$
 correct

Rework.

29.
$$8643$$
 Check 7212

$$-1421$$

$$7212$$

$$8633$$
 incorrect

Rework.

Rework.

- **31.** In subtraction, regrouping is necessary when the digit in the <u>minuend</u> has less value than the digit in the subtrahend, which is directly <u>below</u> it.
- **32.** Subtraction problems **B** and **D** will require regrouping since they have a digit in the subtrahend that is greater than the digit above it in the minuend.

33.
$$75$$
 $\frac{615}{75}$ $\frac{-37}{38}$

34.
$$\begin{array}{r} 716 \\ 86 \\ \hline -28 \\ \hline 58 \end{array}$$

35.
$$9\frac{4}{4}$$

36.
$$6 \%$$
 8% $\frac{-39}{29}$

37.
$$5\%$$

38.
$$4\%$$

$$-29$$
1.8

39.
$$\begin{array}{r} 712 \\ 828 \\ -547 \\ \hline 281 \end{array}$$

40.
$$\begin{array}{c} 81016 \\ 916 \\ -618 \\ \hline 298 \end{array}$$

41.
$$7 \% 1$$
 $-25 2$
 $\overline{519}$

42.
$$\begin{array}{r}
81613 \\
97 3 \\
-788 \\
\hline
185
\end{array}$$

43.
$$\begin{array}{r}
 41218 \\
 7538 \\
 \hline
 -479 \\
 \hline
 7059
\end{array}$$

44.
$$\begin{array}{r}
 71513 \\
 5863 \\
 -1295 \\
 \hline
 4568
\end{array}$$

45.
$$\begin{array}{r}
998718 \\
9988 \\
-2399 \\
\hline
7589
\end{array}$$

46.
$$\begin{array}{r}
215616 \\
3576 \\
-1658 \\
\hline
1918
\end{array}$$

47.
$$\begin{array}{c} 710 \\ 80 \\ \hline -73 \\ \hline 7 \end{array}$$

50.
$$\begin{array}{c} 9 \\ 5 \% 10 \\ 6 \% \% \\ -5 9 9 \\ \hline 1 \end{array}$$

51.
$$\begin{array}{c} 310\ 311 \\ 4\ \emptyset\ 4\ I \\ \hline -12\ 0\ 8 \\ \hline 2\ 8\ 3\ 3 \end{array}$$

53.
$$9305$$

$$-1530$$

$$7775$$

54.
$$7 \stackrel{0}{\cancel{1}} \stackrel{1110}{\cancel{2}} \stackrel{0}{\cancel{0}}$$

$$-6033 \stackrel{1087}{\cancel{0}}$$

55.
$$15 \% \%$$

$$-107 7$$

$$50.3$$

56.
$$\begin{array}{r} 210 \\ 3068 \\ -2105 \\ \hline 963 \end{array}$$

58.
$$\begin{array}{r}
 71111013 \\
 8203 \\
 \hline
 -5365 \\
 \hline
 2838
\end{array}$$

60.
$$7050 \ -6045 \ 1005$$

61.
$$\begin{array}{c}
714\sqrt{0}13 \\
8503 \\
-2816 \\
\hline
5687
\end{array}$$

63.
$$\begin{array}{r}
710 & 61015 \\
80, 705 \\
-61, 667 \\
\hline
19038
\end{array}$$

64.
$$\begin{array}{c} 710 & 10 & 10 & 10 \\ 8 & 1 & 0 & 0 & 0 \\ \hline & -55, 456 \\ \hline & 25, 544 \end{array}$$

67.
$$\begin{array}{c}
 \begin{array}{c}
 9 & 9 \\
 1 & 0 & 0 & 1710 \\
 2 & 0 & 0 & 8 & 0 \\
 \hline
 -1 & 3 & 4 & 9 & 6 \\
 \hline
 6 & 5 & 8 & 4
\end{array}$$

- **68.** To avoid errors when solving math problems, it's a good idea to check your work.
- **69.** When checking the accuracy of an answer to an addition problem, you can use <u>subtraction</u>.
- **70.** An answer to a subtraction problem may be checked using <u>addition</u>.

71.
$$9428$$
 4509 -4509 $+4919$ 9428 correct

72.
$$1671$$
 1325 -1325 1346 2671 incorrect

Rework.

73.
$$2548$$
 2278 -2278 $+270$ 2548 correct

74.
$$5274$$
 4144 -1130 $+1130$ 3274 correct

75.
$$93,758$$
 $52,869$ $-52,869$ $+40,889$ 93.758 correct

Rework.

77.
$$36,778$$
 $19,373$ $-17,405$ $19,373$ $+17,405$ correct

78.
$$\begin{array}{ccc} 34,821 & 17,735 \\ -17,735 & +17,735 \\ \hline 17,735 & 35,470 & incorrect \end{array}$$

Rework.

79. Possible answers are:

3+2=5 could be changed to 5-2=3 or 5-3=2.

6-4=2 could be changed to 2+4=6 or 4+2=6.

- **80.** No, you cannot. Numbers must be subtracted in the order given. The difference found in subtracting is the result of subtracting the subtrahend from the minuend. Changing the order of the minuend and subtrahend *does* change the answer.
- 81. 187 calories man burns
 140 calories woman burns
 47 fewer calories woman burned

A woman burns 47 fewer calories.

82. 403 calories man burns

- 302 calories woman burns

101 more calories man burned

A man burns 101 more calories.

83. 612 new record -543 old record difference in numbers

There are 69 more tornadoes in the new record.

84. 747 deaths in April 1925

- 327 deaths in April 2011

420 difference

There were 420 more deaths in the deadliest tornado outbreak than in the tornado outbreak of April 2011.

The roadway is 246 feet above the water.

There were 11,016 more Ford Explorers sold.

87.
$$6970$$
 jobs six years ago -3700 jobs that remain 3270 jobs eliminated

There were 3270 jobs eliminated.

The increase in price is \$25,565.

There are 9539 flags that remain unsold.

In the district, 8477 students have not received eye exams.

They will pay \$263 more per month if they buy a house.

The monthly increase is \$89.

The first trip is 141 miles longer than the second.

Based on these predictions, the shortage in the number of nurses will be 1,010,000.

This year, there were 138,888 hip replacement procedures were done in the United States on patients under age 65.

96.
$$555,800$$
 knee surgeries this year $-328,900$ knee surgeries six years ago $226,900$ difference

There were 226,900 more knee surgeries this year than six years ago.

100. The sandwich with the least calories is the Veggie Delite and the sandwich with the most calories is the Sweet Onion Chicken Teriyaki.

1.4 Multiplying Whole Numbers

1.4 Margin Exercises

1. (a) 8 factor
$$\times 5$$
 factor $\overline{40}$ product

(b)
$$6$$
 factor $\times 4$ factor 24 product

(c)
$$7$$
 factor $\times 6$ factor 42 product

(d)
$$3$$
 factor $\times 9$ factor 27 product

2. (a)
$$7 \times 4 = 28$$

(b)
$$0 \times 9 = 0$$

(c)
$$8(5) = 40$$

(d)
$$6 \cdot 5 = 30$$

(e)
$$(1)(8) = 8$$

3. (a)
$$3 \times 2 \times 5 = (3 \times 2) \times 5 = 6 \times 5 = 30$$

(b)
$$4 \cdot 7 \cdot 1 = (4 \cdot 7) \cdot 1 = 28 \cdot 1 = 28$$

(c)
$$(8)(3)(0) = 24(0) = 0$$

4. (a)
$$53 \times 5 \over 265$$

(c)
$$\begin{array}{r} 46 \\ 758 \\ \times 8 \\ \hline 6064 \end{array}$$

(d)
$$\begin{array}{c} 52 \\ 2831 \\ \times 7 \\ \hline 19,817 \end{array}$$

(e)
$$\begin{array}{r} 513 \\ 4714 \\ \times 8 \\ \hline 37,712 \end{array}$$

5. (a)
$$63 \times 10 = 630$$
 Attach 0.

(b)
$$305 \times 100 = 30{,}500$$
 Attach 00.

(c)
$$714 \times 1000 = 714{,}000$$
 Attach 000.

6. (a)
$$17 \times 50$$

$$\begin{array}{c}
17 \\
\times 5 \\
\hline
85 \\
17 \times 50 = 850 \\
\text{Attach } 0.
\end{array}$$

(b)
$$73 \times 400$$

$$73$$
 $\times 4$
 292
 $73 \times 400 = 29,200$ Attach 00.

(c)
$$180 \times 30$$

$$\begin{array}{c|c}
 18 \\
 \times 3 \\
\hline
 \hline
 180 \times 30 = 5400 \quad Attach 00.
 \end{array}$$

(d)
$$4200 \times 80$$

$$\begin{array}{c} 42 \\ \times 8 \\ \hline 336 \\ \end{array}$$
 $\begin{array}{c} 4200 \times 80 = 336,000 \\ \end{array}$ Attach 000.

(e)
$$800 \times 600$$

$$\begin{array}{c} 8 \\ \times 6 \\ \hline 48 & 800 \times 600 = 480,000 \ \textit{Attach } 0000. \end{array}$$

7. (a)
$$35 \times 54 = 140 = 175 \quad Add$$

(b)
$$\begin{array}{r} 76 \\ \times 49 \\ \hline 684 \\ \hline 304 \\ \hline 3724 \\ \end{array}$$

(b)
$$81$$
 $\times 49$
 $729 \leftarrow 9 \times 81$
 $324 \leftarrow 4 \times 81$
 3969

(c)
$$234$$
 $\times 73$
 $\overline{702} \leftarrow 3 \times 234$
 $\underline{1638} \leftarrow 7 \times 234$
 $\underline{17,082}$

(d)
$$835$$

 $\times 189$
 $7515 \leftarrow 9 \times 835$
 $6680 \leftarrow 8 \times 835$
 $835 \leftarrow 1 \times 835$
 $157,815$

9. (a)
$$28$$

$$\times 60$$

$$00$$

$$168$$

$$1680$$

(b)
$$728 \times 50 \over 36,400$$

(c)
$$562$$
 $\times 109$
 $\hline 5058$
 $\hline 61,258$
 $1 \times 562 = 562$ Insert 0

(d)
$$3526$$

 $\times 6002$
 $\overline{7052}$
 2115600 $6 \times 3526 = 21,156$ Insert 00
 $\overline{21,163,052}$

10. (a)
$$314$$
 $\times 14$
 1256
 314

The total cost of 314 garden sprayers is \$4396.

(b)
$$139 \times 64 = 556 \times 834 = 8896$$

The total cost of 64 tires is \$8896.

(c)
$$28,300$$
 $\times 12$
 $\overline{56600}$
 28300
 $\overline{339,600}$

The total cost of 12 delivery vans is \$339,600.

1.4 Section Exercises

- 1. In a chain multiplication, if you multiply by the largest number first, rather than the smallest number first, the product will always be the same.
- **2.** The property described in Exercise 1 is the <u>commutative</u> property of multiplication.
- **3.** When you multiply any number by zero, the answer is always <u>zero</u>.
- **4.** When you multiply a whole number by 10, by 100, or by 1000, you can get the answer by attaching one, two, or three <u>zeros</u>, respectively, to the <u>right</u> of the whole number.

5.
$$2 \times 6 \times 2 = (2 \times 6) \times 2 = 12 \times 2 = 24$$

or $2 \times (6 \times 2) = 2 \times 12 = 24$.

6.
$$8 \times 6 \times 1 = (8 \times 6) \times 1 = 48 \times 1 = 48$$

or $8 \times (6 \times 1) = 8 \times 6 = 48$.

7.
$$7 \cdot 8 \cdot 0 = (7 \cdot 8) \cdot 0 = 56 \cdot 0 = 0$$

or $7 \cdot (8 \cdot 0) = 7 \cdot 0 = 0$.

The product of any number and 0 is 0.

8.
$$9 \cdot 0 \cdot 5 = (9 \cdot 0) \cdot 5 = 0 \cdot 5 = 0$$

or $9 \cdot (0 \cdot 5) = 9 \cdot 0 = 0$.

The product of any number and 0 is 0.

9.
$$4 \cdot 1 \cdot 6 = (4 \cdot 1) \cdot 6 = 4 \cdot 6 = 24$$

or $4 \cdot (1 \cdot 6) = 4 \cdot 6 = 24$.

10.
$$1 \cdot 5 \cdot 7 = (1 \cdot 5) \cdot 7 = 5 \cdot 7 = 35$$
 or $1 \cdot (5 \cdot 7) = 1 \cdot 35 = 35$.

11.
$$(4)(5)(2) = [(4)(5)](2) = 20(2) = 40$$
 or $(4)[(5)(2)] = (4)(10) = 40$.

12.
$$(4)(1)(9) = [(4)(1)](9) = 4(9) = 36$$
 or $(4)[(1)(9)] = (4)(9) = 36$.

- 13. Factors may be multiplied in any order to get the same answer. The commutative properties of addition and multiplication are similar since with either you may add or multiply numbers in any order.
- **14.** You may shift the parentheses in a multiplication problem. Just as in addition, the different grouping results in the same answer.

15.
$$\begin{array}{r} 3 \\ 35 \\ \times 6 \\ \hline 210 \end{array}$$

 $6 \cdot 5 = 30$ Write 0, carry 3 tens. $6 \cdot 3 = 18$ Add 3 to get 21. Write 21.

16.
$$\begin{array}{c} 2\\ 53\\ \times 7\\ \hline 371 \end{array}$$

 $7 \cdot 3 = 21$ Write 1, carry 2 tens.

 $7 \cdot 5 = 35$ Add 2 to get 37. Write 37.

17.
$$\begin{array}{r} 2\\ 34\\ \times 7\\ \hline 238 \end{array}$$

 $7 \cdot 4 = 28$ Write 8, carry 2 tens.

 $7 \cdot 3 = 21$ Add 2 to get 23. Write 23.

18.
$$\begin{array}{r} 3 \\ 76 \\ \times 5 \\ \hline 380 \end{array}$$

 $5 \cdot 6 = 30$ Write 0, carry 3 tens.

 $5 \cdot 7 = 35$ Add 3 to get 38. Write 38.

19.
$$\begin{array}{r} 21 \\ 642 \\ \times 5 \\ \hline 3210 \end{array}$$

 $5 \cdot 2 = 10$ Write 0, carry 1 ten.

 $5 \cdot 4 = 20$ Add 1 to get 21. Write 1, carry 2.

 $5 \cdot 6 = 30$ Add 2 to get 32. Write 32.

20.
$$\begin{array}{r} 272 \\ \times 4 \\ \hline 1888 \end{array}$$

 $4 \cdot 2 = 8$ Write 8.

 $4 \cdot 7 = 28$ Write 8, carry 2.

 $4 \cdot 4 = 16$ Add 2 to get 18. Write 18.

21.
$$6\overset{1}{24}$$
 $\times 3$
 1872

 $3 \cdot 4 = 12$ Write 2, carry 1 ten.

 $3 \cdot 2 = 6$ Add 1 to get 7. Write 7.

 $3 \cdot 6 = 18$ Write 18.

22. $\begin{array}{r} 31 \\ 852 \\ \times 7 \\ \hline 5964 \\ \end{array}$

 $7 \cdot 2 = 14$ Write 4, carry 1 ten.

 $7 \cdot 5 = 35$ Add 1 to get 36. Write 6, carry 3.

 $7 \cdot 8 = 56$ Add 3 to get 59. Write 59.

23. $2\overset{21}{153}$ $\times 4$ 8612

 $4 \cdot 3 = 12$ Write 2, carry 1 ten.

 $4 \cdot 5 = 20$ Add 1 to get 21. Write 1, carry 2.

 $4 \cdot 1 = 4$ Add 2 to get 6. Write 6.

 $4 \cdot 2 = 8$ Write 8.

24. 1137 $\times 3$

 $3 \cdot 7 = 21$ Write 1, carry 2 tens.

 $3 \cdot 3 = 9$ Add 2 to get 11. Write 1, carry 1.

 $3 \cdot 1 = 3$ Add 1 to get 4. Write 4.

 $3 \cdot 1 = 3$ Write 3.

25. $\begin{array}{c} 2521 \\ \times 4 \\ \hline 10,084 \end{array}$

 $4 \cdot 1 = 4$ Write 4.

 $4 \cdot 2 = 8$ Write 8.

 $4 \cdot 5 = 20$ Write 0, carry 2.

 $4 \cdot 2 = 8$ Add 2 to get 10. Write 10.

26. $\begin{array}{c}
111 \\
2544 \\
\times 3
\end{array}$

 $\frac{\times 3}{7632}$

 $3 \cdot 4 = 12$ Write 2, carry 1 ten.

 $3 \cdot 4 = 12$ Add 1 to get 13. Write 3, carry 1.

 $3 \cdot 5 = 15$ Add 1 to get 16. Write 6, carry 1.

 $3 \cdot 2 = 6$ Add 1 to get 7. Write 7.

27. $\begin{array}{r} 44 \\ 2561 \\ \times 8 \\ \hline 20.488 \end{array}$

 $8 \cdot 1 = 8$ Write 8.

 $8 \cdot 6 = 48$ Write 8, carry 4.

 $8 \cdot 5 = 40$ Add 4 to get 44. Write 4, carry 4.

 $8 \cdot 2 = 16$ Add 4 to get 20. Write 20.

28. $\begin{array}{r} 113 \\ 7326 \\ \times 5 \\ \hline 36,630 \end{array}$

 $5 \cdot 6 = 30$ Write 0, carry 3 tens.

 $5 \cdot 2 = 10$ Add 3 to get 13. Write 3, carry 1.

 $5 \cdot 3 = 15$ Add 1 to get 16. Write 6, carry 1.

 $5 \cdot 7 = 35$ Add 1 to get 36. Write 36.

29.
$$\begin{array}{r}
46 & 1 \\
36,921 \\
\times & 7 \\
\hline
258,447
\end{array}$$

 $7 \cdot 1 = 7$ Write 7.

 $7 \cdot 2 = 14$ Write 4, carry 1.

 $7 \cdot 9 = 63$ Add 1 to get 64. Write 4, carry 6.

 $7 \cdot 6 = 42$ Add 6 to get 48. Write 8, carry 4.

 $7 \cdot 3 = 21$ Add 4 to get 25. Write 25.

30.
$$\begin{array}{r} 3 \\ 28,116 \\ \times 4 \\ \hline 112,464 \end{array}$$

 $4 \cdot 6 = 24$ Write 4, carry 2 tens.

 $4 \cdot 1 = 4$ Add 2 to get 6. Write 6.

 $4 \cdot 1 = 4$ Write 4.

 $4 \cdot 8 = 32$ Write 2, carry 3.

 $4 \cdot 2 = 8$ Add 3 to get 11. Write 11.

- 31. You can use multiples of 10 to multiply 86×200 . First, multiply 86×2 to get 172. Then, attach two zeros to the right of this number for a final answer of 17,200.
- **32.** You can use multiples of 10 to multiply 7800×450 . First, multiply 78×45 to get 3510. Then, attach three zeros to the right of this number for a final answer of 3,510,000.

34.
$$70$$
 7 70 $\times 5$ $\times 5$ $\times 5$ $\times 5$ Attach 0.

35.
$$740$$
 74 740 $\times 3$ \times

 $970 \cdot 50 = 48,500$ Attach 00.

48.
$$730 \cdot 40$$
 73×4 292

 $730 \cdot 40 = 29,200$ Attach 00.

 $800 \cdot 900 = 720,000$ Attach 0000.

 $850 \cdot 700 = 595{,}000$ Attach 000.

 $9700 \cdot 200 = 1,940,000$ Attach 0000.

 $10,050 \cdot 300 = 3,015,000$ Attach 000.

53.
$$28$$
 $\times 17$
 $196 \leftarrow 7 \times 28$
 $28 \leftarrow 1 \times 28$
 476

54.
$$\begin{array}{c} 16 \\ \times 34 \\ \hline 64 \\ \leftarrow 4 \times 16 \\ \hline 48 \\ \hline 544 \\ \end{array}$$

55.
$$75$$
 $\times 32$
 $150 \leftarrow 2 \times 75$
 $225 \leftarrow 3 \times 75$
 2400

56.
$$82$$
 $\times 32$
 $164 \leftarrow 2 \times 82$
 $246 \leftarrow 3 \times 82$
 2624

57.
$$83$$
 $\times 45$
 $\overline{415} \leftarrow 5 \times 83$
 $332 \leftarrow 4 \times 83$
 $\overline{3735}$

58.
$$(75)(21)$$
 $\begin{array}{c} 75 \\ \times 21 \\ \hline 75 \\ \underline{150} \\ \end{array} \leftarrow 1 \times 75 \\ \underline{1575}$

59.
$$(58)(41)$$
 58 $\times 41$ $\times 41$ $\times 58$ $\times 232$ $\times 4 \times 58$ $\times 4 \times 58$ $\times 4 \times 58$

61.
$$(67)(92)$$
 67
 $\times 92$
 $\hline 134 \leftarrow 2 \times 67$
 $\hline 603 \leftarrow 9 \times 67$

62.
$$(26)(33)$$
 $\begin{array}{c} 26 \\ \times 33 \\ \hline 78 \leftarrow 3 \times 26 \\ \hline 78 \leftarrow 3 \times 26 \\ \hline \hline 858 \end{array}$

63.
$$(28)(564)$$
 564
 $\times 28$
 $\overline{4512} \leftarrow 8 \times 564$
 $\underline{1128} \leftarrow 2 \times 564$
 $\overline{15,792}$

64.
$$(58)(312)$$
 312

$$\times 58$$

$$\hline 2496 \leftarrow 8 \times 312$$

$$\underline{1560} \leftarrow 5 \times 312$$

$$\hline 18,096$$

66.
$$(681)(47)$$
 681

$$\times 47$$

$$\overline{4767} \leftarrow 7 \times 681$$

$$\underline{2724} \leftarrow 4 \times 681$$

$$\overline{32,007}$$

67.
$$(55)(286)$$
 286

$$\times 55$$

$$\hline 1430 \leftarrow 5 \times 286$$

$$\underline{1430} \leftarrow 5 \times 286$$

$$\underline{15,730}$$

68.
$$286$$
 $\times 574$
 $1144 \leftarrow 4 \times 286$
 $2002 \leftarrow 7 \times 286$
 $1430 \leftarrow 5 \times 286$
 164.164

69.
$$735$$
 $\times 112$
 $1470 \leftarrow 2 \times 735$
 $735 \leftarrow 1 \times 735$
 $735 \leftarrow 1 \times 735$
 $82,320$

70. 621

$$\times 415$$

 $\hline
3105 \leftarrow 5 \times 621$
 $621 \leftarrow 1 \times 621$
 $2484 \leftarrow 4 \times 621$
 $\hline
257,715$

72.
$$\begin{array}{c} 3228 \\ \times 751 \\ \hline 3228 \\ + 1 \times 3228 \\ \hline 16140 \\ \times 5 \times 3228 \\ \hline 22596 \\ \hline 2,424,228 \\ \end{array}$$

73.
$$\begin{array}{c} 9352 \\ \times 264 \\ \hline 37408 \leftarrow 4 \times 9352 \\ 56112 \leftarrow 6 \times 9352 \\ \underline{18704} \leftarrow 2 \times 9352 \\ \hline 2,468,928 \end{array}$$

74.
$$528$$
 $\times 106$
 $\hline
3168 \leftarrow 6 \times 528$
 $5280 \leftarrow 10 \times 528$
 $\hline
55,968$

75.
$$215$$
 $\times 307$
 $1505 \leftarrow 7 \times 215$
 $6450 \leftarrow 30 \times 215$
 $66,005$

76.
$$\begin{array}{c} 218 \\ \times 106 \\ \hline 1308 \\ \underline{2180} \\ \hline 23,108 \end{array} \leftarrow 6 \times 218$$

77.
$$428$$

$$\times 201$$

$$428 \leftarrow 1 \times 428$$

$$8560 \leftarrow 20 \times 428$$

$$86,028$$

78.
$$3706$$
 $\times 208$
 $29648 \leftarrow 8 \times 3706$
 $74120 \leftarrow 20 \times 3706$
 770.848

79.
$$\begin{array}{c} 6310 \\ \times 3078 \\ \hline 50480 & \leftarrow 8 \times 6310 \\ 44170 & \leftarrow 7 \times 6310 \\ \hline 189300 & \leftarrow 30 \times 6310 \\ \hline 19,422,180 \end{array}$$

80.
$$\begin{array}{r} 3533 \\ \times 5001 \\ \hline 3533 \\ \leftarrow 1 \times 3533 \\ \hline 1766500 \\ \hline 17,668,533 \end{array} \leftarrow 500 \times 3533$$

81.
$$2195$$
 $\times 1038$
 $17560 \leftarrow 8 \times 2195$
 $6585 \leftarrow 3 \times 2195$
 $21950 \leftarrow 10 \times 2195$
 $2,278,410$

82.
$$\begin{array}{r}
1502 \\
\times 2009 \\
\hline
13518 \leftarrow 9 \times 1502 \\
300400 \leftarrow 200 \times 1502
\end{array}$$
3,017,518

83. To multiply by 10, 100, or 1000, just attach one, two, or three zeros, respectively, to the number you are multiplying and that's your answer.

$$\begin{array}{c|cccc} \textbf{84.} & 291 & 291 \\ & \times 307 & \times 307 \\ \hline 2037 & 2037 \\ & 000 & 8730 \\ \hline 873 & 89,337 \\ \hline \end{array}$$

85.
$$300$$
 cartons
 $\times 10$ balls per carton
 3000 balls

3000 balls were purchased.

86. 500 tablets per bottle

$$\frac{\times 30}{15,000}$$
 bottles tablets

15,000 tablets are in the medical supply house.

87. 194 cost per night

$$\begin{array}{c} \times & 12 \\ \hline 388 \\ \hline 194 \\ \hline 2328 & cost \end{array}$$

The cost of a 12-night stay is \$2328.

88. 45 million per year

$$\frac{\times 4}{180}$$
 years million

The total amount of her earnings on this contract is \$180 million (or \$180,000,000).

89. 365 days per year

$$\frac{\times 66}{2190}$$
 gallons per day $\frac{2190}{2190}$

24,090 gallons per year

The average person in the United States uses 24,090 gallons of water in one year.

90. 27 fishing boats

$$\times 40$$
 tons of squid per boat 1080 tons

The total catch for the night was 1080 tons.

91. 75 first-aid kits at \$8 per kit

$$\begin{array}{r}
75 \\
\times 8 \\
\hline
600
\end{array}$$

The total cost is \$600.

92. 27 days of child care at \$82 per day

$$\begin{array}{r}
 82 \\
 \times 27 \\
 \hline
 574 \\
 \hline
 164 \\
 \hline
 2214
\end{array}$$

The total cost is \$2214.

93. 65 rebuilt alternators at \$24 per alternator

$$\begin{array}{r}
 65 \\
 \times 24 \\
\hline
 260 \\
\hline
 130 \\
\hline
 1560
\end{array}$$

The total cost is \$1560.

94. 62 wheelchair cushions at \$44 per cushion

$$62 \times 44 = 248 = 2728$$

The total cost is \$2728.

95. 206 laptop computers at \$548 per computer

$$\begin{array}{r}
548 \\
\times 206 \\
\hline
3288 \\
10960 \\
\hline
112,888
\end{array}$$

The total cost is \$112,888.

96. 520 printers at \$219 per printer

$$\begin{array}{r}
520 \\
\times 219 \\
\hline
4680 \\
520 \\
\underline{1040} \\
\$113.880
\end{array}$$

The total cost is \$113,880.

97.
$$21 \cdot 43 \cdot 56 = (21 \cdot 43) \cdot 56$$

= $903 \cdot 56$
= 50.568

98.
$$(600)(8)(75)(40) = [(600)(8)](75)(40)$$

= $[(4800)(75)](40)$
= $360,000(40)$
= $14,400,000$

99. 450 trees per acre

$$\begin{array}{c} \times & 85 \\ \hline 2250 \\ \hline 3600 \\ \hline 38,250 \end{array} \text{ trees}$$

38,250 trees are needed to plant 85 acres.

100.
$$15,225$$
 $\times 28$
 121800
 30450
 $426,300$

The blue whale weighs 426,300 pounds.

101. 8,391,881 population of New York City

- 645,169 population of Boston

7,746,712 more people

7,746,712 more people live in New York City than in Boston.

2,616,438 more people live in Los Angeles than in Dallas.

- - $\begin{array}{cc} 315 & cost\ per\ printer \\ \times\ 8 & number\ of\ printers \\ \hline 2520 & total\ cost\ of\ printers \end{array}$

The total cost is the sum of these values:

$$11,640 + 2520 = 14,160$$

104. 954 millions of pounds of food in 17 years
+ 77 millions of pounds of food last year
1031 total

In 18 years, the total amount of food collected was 1031 million pounds (or 1,031,000,000 pounds).

Relating Concepts (Exercises 105–114)

- **105.** (a) 189 + 263 = 452
 - **(b)** 263 + 189 = 452

106. commutative

107. (a) (65 + 81) + 135 = 146 + 135 = 281

(b)
$$65 + (81 + 135) = 65 + 216 = 281$$

108. associative

- **109.** (a) $220 \times 72 = 15,840$
 - **(b)** $72 \times 220 = 15,840$
- 110. commutative
- **111.** (a) $(26 \times 18) \times 14 = 468 \times 14 = 6552$
 - **(b)** $26(18 \times 14) = 26 \times 252 = 6552$
- 112. associative
- 113. No. Some examples are
 - 1. 7 5 = 2, but 5 7 does not equal 2.
 - 2. 12 6 = 6, but 6 12 does not equal 6.
 - 3. (8-2)-5=1, but 8-(2-5) does not equal 1.

- 114. No. Some examples are
 - 1. $10 \div 2 = 5$, but $2 \div 10$ does not equal 5.
 - 2. $(16 \div 8) \div 2 = 1$, but $16 \div (8 \div 2)$ does not equal 1.

1.5 Dividing Whole Numbers

1.5 Margin Exercises

- 1. (a) $24 \div 6 = 4$: $6 | \frac{4}{24}$ or $\frac{24}{6} = 4$
 - **(b)** $9\frac{4}{36}$: $36 \div 9 = 4$ or $\frac{36}{9} = 4$
 - (c) $48 \div 6 = 8$: $\frac{8}{6 \cdot 48}$ or $\frac{48}{6} = 8$
 - **(d)** $\frac{42}{6} = 7$: $42 \div 6 = 7$ or $6 | \frac{7}{42} |$
- 2. (a) $15 \div 3 = 5$ dividend: 15; divisor: 3; quotient: 5
 - **(b)** $18 \div 6 = 3$ dividend: 18; divisor: 6; quotient: 3
 - (c) $\frac{28}{7} = 4$

dividend: 28; divisor: 7; quotient: 4

(d) $\frac{3}{9 | 27}$

dividend: 27; divisor: 9; quotient: 3

- 3. (a) $0 \div 5 = 0$
 - **(b)** $\frac{0}{9} = 0$
 - (c) $\frac{0}{24} = 0$
 - (d) $\frac{0}{37}$
- **4.** (a) $\frac{3}{5\sqrt{15}}$; $5 \cdot 3 = \underline{15}$ or $\underline{3} \cdot 5 = \underline{15}$
 - **(b)** $\frac{32}{4} = 8$; $4 \cdot 8 = 32$ or $8 \cdot 4 = 32$
 - (c) $45 \div 9 = 5$; $9 \cdot 5 = 45$ or $5 \cdot 9 = 45$
- 5. (a) $\frac{4}{0}$; undefined
 - **(b)** $\frac{0}{4} = 0$
 - (c) $0\overline{\smash{)}36}$; undefined

(d)
$$\frac{0}{36}$$

(e) $100 \div 0$; undefined

(f)
$$0 \div 100 = 0$$

6. (a)
$$8 \div 8 = 1$$

(b)
$$\frac{1}{15}$$

(c)
$$\frac{37}{37} = 1$$

7. (a)
$$9 \div 1 = 9$$

(b)
$$1 | 18$$

(c)
$$\frac{43}{1} = 43$$

8. (a)
$$\frac{12}{2\sqrt{24}}$$
 $\frac{2}{2} = 1$, $\frac{4}{2} = 2$

(b)
$$\frac{31}{93}$$
 $\frac{9}{3} = 3$, $\frac{3}{3} = 1$

(c)
$$\frac{22}{488}$$
 $\frac{8}{4} = 2$, $\frac{8}{4} = 2$

(d)
$$\frac{312}{624}$$
 $\frac{6}{2} = 3$, $\frac{2}{2} = 1$, $\frac{4}{2} = 2$

(b)
$$\frac{71}{3}$$
 $\frac{\mathbf{R}2}{215}$ $\frac{21}{3} = 7$, $\frac{5}{3} = 1$ $\mathbf{R}2$

(c)
$$\frac{1}{4} \frac{3}{5} \frac{4}{3} \frac{\mathbf{R}2}{8}$$
 $\frac{5}{4} = 1 \,\mathbf{R}1$, $\frac{13}{4} = 3 \,\mathbf{R}1$, $\frac{18}{4} = 4 \,\mathbf{R}2$

(d)
$$\frac{819}{5}$$

$$\frac{1}{5} \frac{6}{8} \frac{3}{1} \frac{\mathbf{R}4}{9} \quad \frac{8}{5} = 1 \,\mathbf{R}3, \ \frac{31}{5} = 6 \,\mathbf{R}1,$$
$$\frac{19}{5} = 3 \,\mathbf{R}4$$

10. (a)
$$4 \overline{)5 \, {}^{1}3 \, {}^{1}0}$$
 R2

(b)
$$\frac{7 \ 3}{7 \ 51^2 5}$$
 R4

(c)
$$\frac{62 \ 8}{3188^25}$$
 R1

(d)
$$\frac{2\ 3\ 5}{614^21^35}$$
 R5

11. (a)
$$\frac{32}{265}$$
 R1

The answer is correct.

(b)
$$\frac{83}{7586}$$
 R4

Rework.

$$\frac{8}{7}\frac{3}{58}\frac{\mathbf{R}5}{6}$$
 Now check:

The correct answer is 83 R5.

(c)
$$\frac{407}{3}$$
 R2

The answer is correct.

(d)
$$\frac{476}{5} \frac{\text{R}3}{2383}$$

The answer is correct.

- **12.** (a) 258: ends in 8, divisible by 2
 - **(b)** 307: ends in 7, not divisible by 2
 - **(c)** 4216: ends in 6, divisible by 2
 - (d) 73,000: ends in 0, divisible by 2
- **13.** (a) 743: 7+4+3=14

14 is *not* divisible by 3.

So, 743 is not divisible by 3.

(b) $5325: 5 + 3 + 2 + 5 = \underline{15}$

15 is divisible by 3.

So, 5325 is divisible by 3.

- (c) 374,214: 3+7+4+2+1+4=21
- 21 is divisible by 3.

So, 374,214 is divisible by 3.

(d) 205,633: 2+0+5+6+3+3=19

19 is *not* divisible by 3.

So, 205,633 is *not* divisible by 3.

- **14.** (a) 180: ends in 0, divisible by 5
 - **(b)** 635: ends in 5, divisible by 5
 - (c) 8364: does not end in 0 or 5, not divisible by 5
 - (d) 206,105: ends in 5, divisible by 5
- **15.** (a) 270: ends in 0, divisible by 10
 - **(b)** 495: does not end in 0, not divisible by 10
 - (c) 5030: ends in 0, divisible by 10
 - (d) 14,380: ends in 0, divisible by 10

1.5 Section Exercises

1. Three common symbols used to indicate multiplication are

$$\times$$
 ; ()(); and •(dot).

2. Three common symbols used to indicate division are

$$\div$$
 ; \square ; and — (fraction bar).

- 3. $24 \div 4 = 6$: $4 \overline{\smash{\big)} 24}$ or $\frac{24}{4} = 6$
- **4.** $36 \div 3 = 12$: $3\frac{12}{36}$ or $\frac{36}{3} = 12$
- 5. $\frac{45}{9} = 5 : 9\frac{5}{45}$ or $45 \div 9 = 5$
- **6.** $\frac{56}{8} = 7 : \frac{7}{8 | 56}$ or $56 \div 8 = 7$
- 7. $\frac{8}{2\sqrt{16}}$: $16 \div 2 = 8$ or $\frac{16}{2} = 8$

- 8. $\frac{6}{8\sqrt{48}}$: $48 \div 8 = 6$ or $\frac{48}{8} = 6$
- **9.** When a number is divided by 1, the answer is always the <u>number</u> itself.
- **10.** When zero is divided by a number, the answer is always $\underline{0}$.
- 11. $9 \div 9 = 1$

Any nonzero number divided by itself is 1.

- 12. $36 \div 9 = 4$
- 13. $\frac{14}{2} = 7$
- 14. $\frac{10}{0}$ is undefined
- 15. $22 \div 0$; When 0 is the divisor, write <u>undefined</u> as the answer.
- **16.** $6 \div 6 = 1$. When a number is divided by itself, write 1 as the answer.
- 17. $\frac{24}{1} = 24$
- 18. $\frac{12}{1} = 12$
- 19. $\frac{0}{15 | 0}$; When dividing 0 by a nonzero number, the answer is $\underline{0}$.
- **20.** $\frac{0}{12} = 0$; When dividing 0 by a nonzero number, the answer is 0.
- 21. $0\overline{43}$ is undefined
- 22. $\frac{8}{0}$ is undefined
- **23.** 8670 ends in 0, so it is divisible by 2, 5, and 10. The sum of its digits, 21, is divisible by 3, so 8670 is divisible by 3.
- **24.** 13,785 ends in 5, so it is divisible by 5, but not divisible by 2 or 10. The sum of its digits, 24, is divisible by 3, so 13,785 is divisible by 3.
- **25.** 9,221,784 ends in 4, so it is divisible by 2, but not divisible by 5 or 10. The sum of its digits, 33, is divisible by 3, so 9,221,784 is divisible by 3.
- **26.** 5,409,720 ends in 0, so it is divisible by 2, 5, and 10. The sum of its digits, 27, is divisible by 3, so 5,409,720 is divisible by 3.

27.
$$\frac{2}{3} \frac{5}{7^{1}5}$$
 Check $\frac{25}{\times 3}$ $\frac{3}{75}$

28.
$$5\frac{1}{8}\frac{7}{35}$$
 Check $5 \times 17 = 85$

29.
$$7 \overline{\smash{\big|}\, 12^{\, 5}6}$$
 Check 18 $\times 7$ 126

30.
$$\frac{2\ 8}{616^{4}8}$$
 Check $6 \times 28 = 168$

32.
$$\frac{4 \ 61}{5 23^{3}05}$$
 Check $5 \times 461 = 2305$

33.
$$\frac{6\ 2\ 7}{425^{1}0^{2}9}$$
 R1

Check
$$4 \times 627 + 1 = 2508 + 1 = 2509$$

34.
$$8 \overline{13^{5}3^{5}5}$$
 R7

Check
$$8 \times 166 + 7 = 1328 + 7 = 1335$$

35.
$$6 \frac{1}{9} \frac{5}{31} \frac{2}{13} \frac{2}{7}$$

Check
$$6 \times 1522 + 5 = 9132 + 5 = 9137$$

$$36. \quad 9 \frac{9 \ 30}{83^2 71} \mathbf{R}$$

Check
$$9 \times 930 + 1 = 8370 + 1 = 8371$$

37.
$$\frac{309}{61854}$$

Check
$$6 \times 309 = 1854$$

38.
$$\frac{10.7}{8 \times 85^{5}6}$$
 Check $8 \times 107 = 856$

39.
$$12,020 \div 4$$
 $\begin{array}{c} 3 \ 005 \\ 4 \ 12 \ 020 \end{array}$

Check
$$4 \times 3005 = 12,020$$

40.
$$8012 \div 4$$

$$\frac{200 \ 3}{4 \ 801^{1}2}$$

Check
$$4 \times 2003 = 8012$$

Check
$$6 \times 5006 = 30,036$$

42.
$$32,008 \div 8$$
 $8 \overline{\smash{\big)} 32,008}$

Check
$$8 \times 4001 = 32,008$$

43.
$$2434 \div 3$$
 $811 \text{ R1} \\ 32434$

Check
$$3 \times 811 + 1 = 2433 + 1 = 2434$$

Check
$$7 \times 856 + 1 = 5992 + 1 = 5993$$

Check
$$5 \times 2589 + 2 = 12,945 + 2 = 12,947$$

46.
$$33,285 \div 9$$

$$\frac{3 \ 6 \ 9 \ 8}{9 33,^{6}2^{8}8^{7}5} \mathbf{R}^{3}$$

Check
$$9 \times 3698 + 3 = 33,282 + 3 = 33,285$$

47.
$$\frac{21,040}{8}$$
 $\frac{2 \cdot 6 \cdot 30}{8 \cdot 21, \cdot 50^{2} \cdot 40}$

Check
$$8 \times 2630 = 21,040$$

48.
$$\frac{8199}{9}$$
 $\frac{911}{98199}$

Check
$$9 \times 911 = 8199$$

49.
$$\frac{74,751}{6}$$
 $\frac{1}{6}$ $\frac{2}{6}$ $\frac{1}{7}$ $\frac{2}{4}$ $\frac{5}{5}$ $\frac{8}{1}$ $\frac{8}{1}$

Check
$$6 \times 12,458 + 3 = 74,748 + 3 = 74,751$$

50.
$$\frac{72,543}{5}$$
 $\frac{1}{5}$ $\frac{4}{7}$ $\frac{50}{2}$, $\frac{8}{5}$ $\frac{1}{7}$ $\frac{4}{2}$, $\frac{50}{4}$ $\frac{8}{3}$

Check
$$5 \times 14,508 + 3 = 72,540 + 3 = 72,543$$

51.
$$\frac{71,776}{7}$$
 $\frac{10, 253}{7[71, {}^{1}7]^{3}7} \frac{1}{6}$

Check
$$7 \times 10,253 + 5 = 71,771 + 5 = 71,776$$

52.
$$\frac{77,621}{3}$$
 $\frac{2 \ 5, \ 8 \ 7 \ 3}{3 \ 7^{\ 17, \ 26 \ 22 \ 11}}$ R2

Check
$$3 \times 25,873 + 2 = 77,619 + 2 = 77,621$$

53.
$$\frac{128,645}{7}$$
 $\frac{1}{7}$ $\frac{1}{12}$ $\frac{8}{58}$, $\frac{3}{6}$ $\frac{7}{54}$ $\frac{7}{5}$

Check
$$7 \times 18,377 + 6 = 128,639 + 6 = 128,645$$

54.
$$\frac{172,255}{4}$$
 $\frac{4\ 3,0\ 6\ 3}{417^{1}2,2^{2}5^{1}5}$ R3

Check
$$4 \times 43,063 + 3 = 172,252 + 3 = 172,255$$

55.
$$\frac{375}{51877}$$
 R2

Check
$$5 \times 375 + 2 = 1875 + 2 = \underline{1877}$$
 correct

56.
$$\frac{427}{31282}$$
 R1

Check
$$3 \times 427 + 1 = 1281 + 1 = 1282$$
 correct

57.
$$\frac{1908}{35725}$$
 R2

Check
$$3 \times 1908 + 2 = 5724 + 2 = 5726$$
 incorrect

Rework.

Check
$$3 \times 1908 + 1 = 5724 + 1 = 5725$$

58.
$$\frac{432}{52158}$$
 R3

Check
$$5 \times 432 + 3 = 2160 + 3 = 2163$$
 incorrect

Rework.

$$\frac{4 \ 31}{5 21^{1}58} \mathbf{R}^{3}$$

Check
$$5 \times 431 + 3 = 2155 + 3 = 2158$$
 correct

59.
$$\frac{650}{74692}$$
 R2

Check
$$7 \times 650 + 2 = 4550 + 2 = 4552$$
 incorrect

Rework.

$$\frac{670}{746^{4}92}$$
 R2

Check
$$7 \times 670 + 2 = 4690 + 2 = 4692$$
 correct

60.
$$\frac{663}{95974}$$
 R5

Check
$$9 \times 663 + 5 = 5967 + 5 = 5972$$
 incorrect

Rework.

$$\frac{6 \ 6 \ 3}{9 59^{5}7^{3}4} \mathbf{R}^{7}$$

Check
$$9 \times 663 + 7 = 5967 + 7 = 5974$$
 correct

61.
$$\frac{3568}{621,409}$$
 R2

Check
$$6 \times 3568 + 2 = 21,408 + 2 = 21,410$$
 incorrect

Rework.

Check
$$6 \times 3568 + 1 = 21,408 + 1 = 21,409$$

62.
$$6\overline{3192}$$

Check
$$6 \times 532 = 3192$$
 correct

63.
$$8\overline{\smash{\big|}\,16,019}^{\,2\,002}$$
 R3

Check
$$8 \times 2002 + 3 = 16,016 + 3 = 16,019$$
 correct

64.
$$8\overline{\smash{\big)}\,3\,3\,6\,6\,4}$$

Check
$$8 \times 4208 = 33,664$$
 correct

65.
$$669,140$$
 R2

Check
$$6 \times 11,523 + 2 = 69,138 + 2 = 69,140$$
 correct

66.
$$3\frac{27,532}{82,598}$$
R1

Check
$$3 \times 27,532 + 1 = 82,596 + 1 = 82,597$$
 incorrect

Rework.

$$\frac{2}{8} \frac{7}{8} \frac{532}{2} \frac{\mathbf{R}2}{1598}$$

Check
$$3 \times 27,532 + 2 = 82,596 + 2 = 82,598$$

67.
$$9 628 R7$$
 $9 86,655$

Check
$$9 \times 9628 + 7 = 86,652 + 7 = 86,659$$
 incorrect

Rework.

$$9 \quad 6 \quad 2 \quad 8 \quad \mathbf{R}^{3}$$

$$9 \quad 8 \quad 6, \quad {}^{5} 6 \quad {}^{2} 5 \quad {}^{7} 5$$

Check
$$9 \times 9628 + 3 = 86,652 + 3 = 86,655$$

68.
$$\frac{7258}{750,809}$$
 R4

Check
$$7 \times 7258 + 4 = 50,806 + 4 = 50,810$$
 incorrect

Rework.

Check
$$7 \times 7258 + 3 = 50,806 + 3 = 50,809$$

69.
$$8\overline{222,576}$$

Check $8 \times 27,822 = 222,576$ *correct*

70.
$$\frac{77,804}{4311,216}$$

Check $4 \times 77,804 = 311,216$ *correct*

- **71.** Multiply the quotient by the divisor and add any remainder. The result should be the dividend.
- **72.** Answers will vary. Three choices might be:

A number is divisible by 2 if it ends in a 0, 2, 4, 6, or 8;

A number is divisible by 5 if it ends in 0 or 5; A number is divisible by 10 if it ends in 0.

73.
$$8 \overline{)26^{2}2^{6}4}$$

328 tables can be set.

Each school will receive 135 books.

75.
$$9600$$
 $876,4800$

9600 drumsticks are produced each hour.

83,000,000 or 83 million Tootsie Rolls are produced each day.

77.
$$9\overline{4\ 3^{\ 7}6, {}^{4}500}$$

Each employee received \$48,500.

78.
$$\frac{3 \ 4 \ 3 \ 5}{517,^{2}1^{1}7^{2}5}$$

 $3435\ 5\text{-pound}$ bags of flour can be filled.

79.
$$4 \frac{6^{2} 6^{2}}{6^{2} 6^{2}}$$

There are 165 locations in this area.

80.
$$5 | 8^{3}5$$

The average number of Wiis sold in the first five years was 17 million (or 17,000,000).

81.
$$6\frac{1,1}{6,8}\frac{3}{2}\frac{7}{45}\frac{500}{300}$$
 (or use a calculator)

Each person received \$1,137,500.

82.
$$8\frac{5, 625,000}{45, {}^{5}0{}^{2}0{}^{4}0,000}$$
 (or use a calculator)

Each payment is \$5,625,000.

83.
$$862,500$$
 $86,9^{5}0^{2}0,^{4}000$

The number of blueberries picked each hour was 862,500.

84.
$$\frac{5, 4 \ 8 \ 4, 3 \ 7 \ 5}{4 \ 21, {}^{1}9 \ {}^{3}3 \ {}^{1}7, {}^{1}5 \ {}^{3}0 \ {}^{2}0}$$

Assuming the salary each year was the same, the salary was \$5,484,375.

- **85.** 60 ends in 0, so it is divisible by 2, 5, and 10. The sum of its digits, 6, is divisible by 3, so 60 is divisible by 3.
- **86.** 35 ends in 5, so it is divisible by 5, but not divisible by 2 or 10. The sum of its digits, 8, is not divisible by 3, so 35 is not divisible by 3.
- **87.** 92 ends in 2, so it is divisible by 2, but not divisible by 5 or 10. The sum of its digits, 11, is not divisible by 3, so 92 is not divisible by 3.
- **88.** 96 ends in 6, so it is divisible by 2, but not divisible by 5 or 10. The sum of its digits, 15, is divisible by 3, so 96 is divisible by 3.
- **89.** 445 ends in 5, so it is divisible by 5, but not divisible by 2 or 10. The sum of its digits, 13, is not divisible by 3, so 445 is not divisible by 3.
- **90.** 897 ends in 7, so it is not divisible by 2, 5, or 10. The sum of its digits, 24, is divisible by 3, so 897 is divisible by 3.
- **91.** 903 ends in 3, so it is not divisible by 2, 5, or 10. The sum of its digits, 12, is divisible by 3, so 903 is divisible by 3.
- **92.** 500 ends in 0, so it is divisible by 2, 5, and 10. The sum of its digits, 5, is not divisible by 3, so 500 is not divisible by 3.
- 93. 5166 ends in 6, so it is divisible by 2, but not divisible by 5 or 10. The sum of its digits, 18, is divisible by 3, so 5166 is divisible by 3.
- **94.** 8302 ends in 2, so it is divisible by 2, but not divisible by 5 or 10. The sum of its digits, 13, is not divisible by 3, so 8302 is not divisible by 3.
- **95.** 21,763 ends in 3, so it is not divisible by 2, 5, or 10. The sum of its digits, 19, is not divisible by 3, so 21,763 is not divisible by 3.
- **96.** 32,472 ends in 2, so it is divisible by 2, but not divisible by 5 or 10. The sum of its digits, 18, is divisible by 3, so 32,472 is divisible by 3.

1.6 Long Division

1.6 Margin Exercises

1. (a)
$$82 \over 28 \overline{\smash)2296} \over 224 \leftarrow 8 \times 28 \over \overline{56} \leftarrow 2 \times 28$$

(b)
$$\begin{array}{c} 64 \\ 16 \overline{\smash{\big|}\ 1024} \\ \underline{96} \\ \underline{64} \\ \underline{64} \\ \underline{0} \end{array} \leftarrow 6 \times 16$$

(c)
$$\begin{array}{r}
1 & 4 & 4 \\
61 \overline{\smash)8784} \\
\underline{61} \\
2 & 6 & 8
\end{array}$$

$$\underline{26} \\
244 \\
\underline{244} \\
4 \\
\underline{244} \\
0
\end{array}$$
 $\leftarrow 4 \times 61$

(d)
$$\begin{array}{c} 29\\ 93 \overline{\smash)2697}\\ \underline{186}\\ \underline{837}\\ \underline{837} \leftarrow 9 \times 93 \end{array}$$

2. (a)
$$56$$
 $24\overline{\smash{\big|}\, 1344}$
 $\underline{120} \leftarrow 5 \times 24$
 $\underline{144} \leftarrow 6 \times 24$

(b)
$$\begin{array}{c} 62 \\ 72 \overline{\smash)4472} \\ \underline{432} \\ 152 \\ \underline{144} \\ 4 \end{array} \leftarrow 6 \times 72$$

(c)
$$\begin{array}{r} 83 \\ 65 \overline{\smash)5416} \\ \underline{520} \\ 216 \\ \underline{195} \\ 21 \end{array} \leftarrow 8 \times 65$$

(d)
$$\begin{array}{c} 7 \ 4 \\ 89 \overline{\smash{\big)}\ 6 \ 6 \ 4 \ 9} \\ \underline{ 6 \ 2 \ 3 }_{4 \ 1 \ 9} \\ \underline{ 3 \ 5 \ 6 }_{6 \ 3} \leftarrow 4 \times 89 \end{array}$$

3. (a)
$$1 \ \underline{0} \ 7$$
 $R4 \ \underline{17 \ | 1823}$ $\leftarrow 1 \times 17$ $\underline{123}$ $\leftarrow 1 \times 17$ $\underline{119} \leftarrow 7 \times 17$

(b)
$$\begin{array}{c} 2\ 0\ 8 \\ 23 \overline{)4\ 7\ 9\ 1} \\ \underline{4\ 6} \\ 1\ 9\ 1 \\ \underline{1\ 8\ 4} \\ -6\ \times 23 \end{array}$$

(d)
$$\begin{array}{c} 3\ 0\ 0 \\ 78 \overline{\smash)2\ 3,\ 4\ 6\ 2} \\ \underline{2\ 3\ 4} \\ 6\ 2 \end{array} \leftarrow 3 \times 78 \\ \end{array}$$

4. (a)
$$70 \div 10 = 7$$

One zero is dropped.

(b)
$$2600 \div 100 = 26$$

Two zeros are dropped.

(c)
$$505,000 \div 1000 = 505$$

Three zeros are dropped.

5. (a) $50\overline{6250}$

Drop 1 zero from the divisor and the dividend.

$$\begin{array}{c|c}
1 & 2 & 5 \\
5 & 6 & 2 & 5 \\
\hline
5 & 1 & 2 \\
1 & 0 & 2 & 5 \\
\hline
2 & 5 & 0
\end{array}$$

The quotient is 125.

Drop 1 zero from the divisor and the dividend.

$$\begin{array}{r}
1 & 0 & 0 & 8 \\
13 & 1 & 3 & 1 & 0 & 4 \\
\underline{1 & 3} & & \\
1 & 0 & 4 \\
\underline{1 & 0 & 4} & & \\
0
\end{array}$$

The quotient is 1008.

(c) 3400 190,400

Drop 2 zeros from the divisor and the dividend.

$$\begin{array}{r}
5 6 \\
34 \overline{\smash{\big)}\ 1904} \\
\underline{170} \\
204 \\
\underline{204} \\
0
\end{array}$$

The quotient is 56.

The result does not match the dividend. **Rework.**

$$\begin{array}{r}
45\\
426 \overline{\smash) 19,170}\\
\underline{1704}\\
2130\\
\underline{2130}\\
0
\end{array}$$

A check shows that 45 is correct.

$$\begin{array}{c} 514 \ \textit{Multiply the} \\ \times \quad 57 \ \textit{quotient and} \\ \hline 3598 \ \textit{the divisor.} \\ \hline 2570 \\ \hline 29,298 \\ + \quad 18 \ \textit{Add the remainder} \\ \hline 29,316 \ \leftarrow \textit{correct} \\ \end{array}$$

1.6 Section Exercises

1.
$$\frac{5}{50 \cdot 2650}$$
 5; 53; 530

5 goes over the 5, because $\frac{265}{50}$ is about 5. The answer must then be a two-digit number or 53.

2.
$$\frac{3}{14\sqrt{476}}$$
 3; 34; 304

3 goes over the 7, because $\frac{47}{14}$ is about 3. The answer must then be a two-digit number or 34

3.
$$\frac{2}{18 \sqrt{4500}}$$
 2; 25; 250

2 goes over the 5, because $\frac{45}{18}$ is about 2. The answer must then be a three-digit number or 250.

4.
$$\frac{1}{35|5600}$$
 16; 160; 1600

1 goes over the 6, because $\frac{56}{35}$ is about 1. The answer must then be a three-digit number or 160.

5.
$$\frac{1}{86 | 10,327}$$
 12; 120 **R**7; 1200

1 goes over the 3, because $\frac{103}{86}$ is about 1. The answer must then be a three-digit number or 120 **R**7

6.
$$\frac{5}{46 \times 24,026}$$
 5; 52; 522 **R**14

5 goes over the 0, because $\frac{240}{46}$ is about 5. The answer must then be a three-digit number or $522 \, \mathbf{R} 14$.

7.
$$\frac{1}{26[28,735]}$$
 11; 110; 1105 **R**5

1 goes over the 8, because $\frac{28}{26}$ is about 1. The answer must then be a four-digit number or $1105~{\bf R}5$.

8.
$$\frac{9}{12 \overline{116,953}}$$
 974 **R**2; 9746 **R**1; 97,460

9 goes over the 6, because $\frac{116}{12}$ is about 9. The answer must then be a four-digit number or $9746 \, \mathbf{R}1$.

9.
$$\frac{7}{21 \overline{\smash{\big)}\, 149,826}}$$
 71; 713; 7134 **R**12

7 goes over the 9, because $\frac{149}{21}$ is about 7. The answer must then be a four-digit number or 7134 **R**12.

10.
$$\frac{3}{64\sqrt{208,138}}$$
 325 **R**2; 3252 **R**10; 32,521

3 goes over the 8, because $\frac{208}{64}$ is about 3. The answer must then be a four-digit number or $3252 \, \mathbf{R} 10$.

11.
$$\frac{9}{523 \overline{\smash{\big)}\,470,800}}$$
 9 R100; 90 R100; 900 R100

9 goes over the 8, because $\frac{4708}{523}$ is about 9. The answer must then be a three-digit number or $900 \, \mathbf{R} 100$.

12.
$$\frac{1}{230 | 253,230}$$
 11; 110; 1101

1 goes over the 3, because $\frac{253}{230}$ is about 1. The answer must then be a four-digit number or 1101

15.
$$476 \text{ R}15 \text{ Check}$$
 $476 \\ 23 10, 963 \\ \underline{92} \\ 176 \\ \underline{161} \\ 153 \\ \underline{138} \\ 15$ Check $476 \\ \times 23 \\ \underline{1428} \\ 952 \\ \underline{10,948} \\ + 15 \\ \underline{10,963}$

22.
$$87 \text{ Check}$$
 308 $308 | 26,796$ $\times 87$ 2464 2156 2464 2156 $26,796$

25.
$$\frac{101}{35}$$
 R4 Check $101 \times 35 = 35 = 303 = 3535 = 4 = 4 = 3539 incorrect$

Rework.

$$\begin{array}{c|c}
 & 1 & 0 & 1 \\
35 & 3 & 5 & 4 & 9 \\
\hline
 & 3 & 5 \\
\hline
 & 0 & 4 & 9 \\
 & 3 & 5 \\
\hline
 & 1 & 4
\end{array}$$

The correct answer is 101 **R**14.

Rework.

$$\begin{array}{r}
4 \ 2 \\
64 \overline{\smash)2\ 7\ 1\ 2} \\
\underline{2\ 5\ 6} \\
1\ 5\ 2 \\
\underline{1\ 2\ 8} \\
2\ 4
\end{array}$$

The correct answer is $42 \, \mathbf{R} 24$.

Rework.

$$\begin{array}{r}
 658 \\
 28 \overline{\smash{\big)}\ 18,424} \\
 \underline{168} \\
 162 \\
 \underline{140} \\
 \underline{224} \\
 \underline{0}
\end{array}$$

The correct answer is 658.

Rework.

$$\begin{array}{r} & 6\ 2 \\ 614 \overline{\smash{\big|}\,3\ 8,\ 0\ 6\ 8} \\ \underline{3\ 6\ 8\ 4} \\ \hline 1\ 2\ 2\ 8 \\ \underline{1\ 2\ 2\ 8} \\ 0 \end{array}$$

The correct answer is 62.

31. Divide. (We could drop one zero.)

$$\begin{array}{r}
1 & 1 & 7 \\
720 & 8 & 4, 2 & 4 & 0 \\
\hline
7 & 2 & 0 \\
\hline
1 & 2 & 2 & 4 \\
\hline
7 & 2 & 0 \\
\hline
5 & 0 & 4 & 0 \\
\hline
5 & 0 & 4 & 0 \\
\hline
0 & 0
\end{array}$$

There were 117 episodes filmed each season.

32. Divide to find the number of containers for one tower. (We could drop one zero.)

$$\begin{array}{r}
3 & 7 & 5 & 0 \\
160 & 6 & 0 & 0 & 0 & 0 \\
\underline{4 & 8 & 0} \\
1 & 2 & 0 & 0 \\
\underline{1 & 1 & 2 & 0} \\
8 & 0 & 0 \\
\underline{8 & 0 & 0} \\
0
\end{array}$$

Now multiply by two to find the number of containers for *both* towers.

$$2 \times 3750 = 7500$$

33. First, add the number of wall and table clocks.

Subtract the sum from the total number of clocks.

He worked on 56 floor clocks this year.

We could also arrange our work as follows:

24,000,000 total businesses
 7 000 larger businesses
 23,993,000 remaining

There are 23,993,000 small to mid-size businesses.

35. Divide. (or use a calculator)

$$\begin{array}{r}
3 55 \\
96 \overline{\smash)34,080} \\
\underline{288} \\
5 28 \\
\underline{480} \\
480 \\
\underline{0}
\end{array}$$

Judy's monthly payment is \$355.

36. Divide. (or use a calculator)

$$\begin{array}{r} & 88 \\ 225 \overline{\smash{\big|}\, 19,800} \\ \underline{1800} \\ \underline{1800} \\ \underline{1800} \\ \underline{0} \end{array}$$

The consultant charged \$88 per hour.

37. If one ring is sold each minute, then 60 rings are sold each hour.

There are 43,200 diamond rings sold in 30 days.

38. If he ate one Twinkie each day, then he ate 365 Twinkies each year.

He ate 21,900 Twinkies in 60 years.

39. (a) Divide. 6 4 8
39 2 5, 2 7 2
2 3 4
1 8 7
1 5 6
3 1 2
3 1 2

He has eaten an average of 648 Big Macs a year for the last 39 years.

(b) We could divide 648 by 365, but it is fairly easy to see that this division result is between 1 and 2, so the answer to the problem is less than 2 Big Macs per day.

40.
$$\frac{220,020}{30} = \frac{22,002}{3} \text{ (Drop 1 zero.)}$$

$$3 | 22,002 | 2 | 21 | 0 | 9$$

Each team used 7334 baseballs.

Relating Concepts (Exercises 41–48)

- 41. $\frac{\$0}{3} = \0 Each person will receive \$0.
- **42.** When 0 is divided by any nonzero number, the result is 0.
- **43.** $8 \div 0$ is undefined.
- **44.** It is <u>impossible</u>. If you have 6 cookies, it is not possible to divide them among zero people.
- **45.** (a) $14 \div 1 = 14$
 - **(b)** 1 7 1 7

(c)
$$\frac{38}{1} = 38$$

- **46.** Yes. Some examples are $18 \cdot 1 = 18$; $26 \cdot 1 = 26$; and $43 \cdot 1 = 43$.
- 47. (a) $32,000 \div 10 = 3200$

Drop 1 zero from the dividend and 1 zero from the divisor.

(b) $32,000 \div 100 = 320$

Drop 2 zeros from the dividend and 2 zeros from the divisor.

(c) $32,000 \div 1000 = 32$

Drop 3 zeros from the dividend and 3 zeros from the divisor.

48. Drop the same number of zeros from the dividend that appear in the divisor. The result is the quotient. With a divisor of 10, drop one zero; with 100, drop two zeros; with 1000, drop three zeros.

1.7 Rounding Whole Numbers

1.7 Margin Exercises

1. (a) 373 (nearest ten)

Underline the tens place: 373

373 is closer to $3\underline{7}0$.

(b) 1482 (nearest thousand)

Underline the thousands place: <u>1</u>482

1482 is closer to <u>1</u>000.

(c) 89,512 (nearest hundred)

Underline the hundreds place: 89,512

89,512 is closer to $89,\underline{5}00$.

(d) 546,325 (nearest ten-thousand)

Underline the ten-thousands place: 546,325

546,325 is closer to 550,000.

2. (a) $\underline{6}2$

Underline the tens place. Next digit is $\underline{4}$ or less. Change the digit to the right of the underlined place to zero.

62 rounded to the nearest ten is 60.

(b) 94

Underline the tens place. Next digit is 4 or less. Change the digit to the right of the underlined place to zero.

94 rounded to the nearest ten is 90.

(c) 1<u>3</u>4

Underline the tens place. Next digit is 4 or less. Change the digit to the right of the underlined place to zero.

134 rounded to the nearest ten is 130.

(d) 7543

Underline the tens place. Next digit is 4 or less. Change the digit to the right of the underlined place to zero.

7543 rounded to the nearest ten is 7540.

3. (a) $\underline{3}683$ Next digit is 5 or more.

Change 3 to 4. All digits to the right of the underlined place are changed to zero.

3683 rounded to the nearest thousand is 4000.

(b) $\underline{6502}$ Next digit is 5 or more.

Change 6 to 7. All digits to the right of the underlined place are changed to zero.

6502 rounded to the nearest thousand is 7000.

(c) 84,621 Next digit is 5 or more.

Change 4 to 5. All digits to the right of the underlined place are changed to zero.

84,621 rounded to the nearest thousand is 85,000.

(d) 5<u>5</u>,960 Next digit is 5 or more.

Change 5 to 6. All digits to the right of the underlined place are changed to zero.

55,960 rounded to the nearest thousand is 56,000.

4. (a) 3458 to the nearest ten

34<u>5</u>8 Next digit is 5 or more.

Change 5 to 6. All digits to the right of the underlined place are changed to zeros.

3458 rounded to the nearest ten is 3460.

(b) 6448 to the nearest hundred

6448 Next digit is 4 or less.

Leave 4 as 4.

All digits to the right of the underlined place are changed to zeros.

6448 rounded to the nearest hundred is 6400.

(c) 73,077 to the nearest hundred

73,<u>0</u>77 Next digit is 5 or more.

Change 0 to 1. All digits to the right of the underlined place are changed to zeros.

73,077 rounded to the nearest hundred is 73,100.

(d) 85,972 to the nearest hundred

85,972 Next digit is 5 or more.

Change 9 to 10. Write zero and carry the 1. All digits to the right of the underlined place are changed to zeros.

85,972 rounded to the nearest hundred is 86,000.

5. (a) 14,598 to the nearest ten-thousand

14,598

The ten-thousands place does not change because the digit to the right is 4 or less.

All digits to the right of the underlined place are changed to zeros.

14,598 rounded to the nearest ten-thousand is 10,000.

(b) 724,518,715 to the nearest million

724,518,715

Change 4 to 5 because the digit to the right is 5 or more.

All digits to the right of the underlined place are changed to zeros.

724,518,715 rounded to the nearest million is 725,000,000.

6. (a) To the nearest ten: $5\underline{4}9$

Next digit is 5 or more.

Tens place (4 + 1 = 5) changes.

549 rounded to the nearest ten is 550.

To the nearest hundred: 549

Next digit is 4 or less.

Hundreds place stays the same.

549 rounded to the nearest hundred is 500.

(b) To the nearest ten: 458

Next digit is 5 or more.

Tens place (5 + 1 = 6) changes.

458 rounded to the nearest ten is 460.

To the nearest hundred: 458

Next digit is 5 or more.

Hundreds place (4 + 1 = 5) changes. All digits to the right of the underlined place are changed to zeros.

458 rounded to the nearest hundred is 500.

(c) To the nearest ten: 9308

Next digit is 5 or more.

Tens place (0 + 1 = 1) changes.

9308 rounded to the nearest ten is 9310.

To the nearest hundred: 9308

Next digit is 4 or less.

Hundreds place stays the same.

9308 rounded to the nearest hundred is 9300.

7. (a) To the nearest ten: $40\underline{7}8$

Next digit is 5 or more.

Tens place (7 + 1 = 8) changes.

4078 rounded to the nearest ten is 4080.

To the nearest hundred: 4078

Next digit is 5 or more.

Hundreds place (0 + 1 = 1) changes.

4078 rounded to the nearest hundred is 4100.

To the nearest thousand: 4078

Next digit is 4 or less.

Thousands place stays the same.

4078 rounded to the nearest thousand is 4000.

(b) To the nearest ten: $46,3\underline{6}4$

Next digit is 4 or less.

Tens place stays the same.

46,364 rounded to the nearest ten is 46,360.

To the nearest hundred: 46,364

Next digit is 5 or more.

Hundreds place (3 + 1 = 4) changes.

46,364 rounded to the nearest hundred is 46,400.

To the nearest thousand: 46,364

Next digit is 4 or less.

Thousands place stays the same.

46,364 rounded to the nearest thousand is 46,000.

(c) To the nearest ten: 268,328

Next digit is 5 or more.

Tens place (2 + 1 = 3) changes.

268,328 rounded to the nearest ten is 268,330.

To the nearest hundred: 268,328

Next digit is 4 or less.

Hundreds place stays the same.

268,328 rounded to the nearest hundred is 268,300.

To the nearest thousand: 268,328

Next digit is 4 or less.

Thousands place stays the same.

268,328 rounded to the nearest thousand is 268,000.

- 8. (a) 16 20 rounded to the nearest ten 74 70 58 60 +31 +30 estimated answer
 - (b) 53 50 rounded to the nearest ten $\frac{-19}{30}$ estimated answer
 - (c) 46 $\underline{50}$ rounded to the nearest ten $\times 74$ $\underline{\times 70}$ estimated answer
- 9. (a) 358 400 rounded to the nearest
 743 700 hundred
 822 800
 + 978 + 1000
 2900 estimated answer

- (b) 842 800 rounded to the nearest -475 -500 hundred 300 estimated answer
- (c) 723 700 rounded to the nearest $\times 478$ $\times 500$ hundred 350,000 estimated answer
- 10. (a) 36 40 first digit rounded; all 3852 4000 others changed to zero $\frac{749}{+5474} = \frac{+5000}{9740}$ estimated answer
 - (b) 2583 3000 first digit rounded; all -765 -800 others changed to zero 2200 estimated answer
 - (c) 648 600 first digit rounded; all \times 67 \times 70 others changed to zero 42,000 estimated answer

1.7 Section Exercises

- 1. 624 to the nearest ten is 620.
- 2. 509 to the nearest ten is 510.
- **3.** 86,813 to the nearest hundred is 86,800.
- **4.** 17,211 to the nearest hundred is 17,200.
- **5.** 78,499 to the nearest thousand is 78,000.
- **6.** 14,314 to the nearest <u>thousand</u> is 14,000.
- 7. 12,987 to the nearest <u>ten-thousand</u> is 10,000.
- **8.** 6599 to the nearest <u>ten-thousand</u> is 10,000.
- **9.** 855 rounded to the nearest ten: 860

855 Next digit is 5 or more. Tens place changes (5+1=6). All digits to the right of the underlined place change to zero.

10. 946 rounded to the nearest ten: 950

 $9\underline{4}6$ Next digit is 5 or more. Tens place changes (4+1=5). The digit to the right of the underlined place changes to zero.

11. 6771 rounded to the nearest hundred: 6800

 $6\overline{7}71$ Next digit is 5 or more. Hundreds place changes (7+1=8). All digits to the right of the underlined place change to zero.

12. 5847 rounded to the nearest hundred: 5800

5847 Next digit is 4 or less. Hundreds place does not change. All digits to the right of the underlined place change to zero.

- 13. 28,472 rounded to the nearest hundred: 28,500 28,472 Next digit is 5 or more. Hundreds place changes (4+1=5). All digits to the right of the underlined place change to zero.
- 18,249 rounded to the nearest hundred: 18,200
 18,249 Next digit is 4 or less. Hundreds place does not change. All digits to the right of the underlined place change to zero.
- 15. 5996 rounded to the nearest hundred: 6000 $\frac{5996}{1}$ Next digit is 5 or more. Hundreds place changes (9 + 1 = 10). Write 0 and carry 1. All digits to the right of the underlined place change to
- 16. 4452 rounded to the nearest hundred: 4500 $4\underline{4}52$ Next digit is 5 or more. Hundreds place changes (4+1=5). All digits to the right of the underlined place change to zero.
- 17. 15,758 rounded to the nearest thousand: 16,000 15,758 Next digit is 5 or more. Thousands place changes (5+1=6). All digits to the right of the underlined place change to zero.
- 18. 28,465 rounded to the nearest thousand: 28,000
 28,465 Next digit is 4 or less. Thousands place does not change. All digits to the right of the underlined place change to zero.
- **19.** 7,760,058,721 rounded to the nearest billion: 8,000,000,000

7,760,058,721 Next digit is 5 or more. Billions place changes (7 + 1 = 8). All digits to the right of the underlined place change to zero.

- **20.** 4,468,523,628 rounded to the nearest billion: 4,000,000,000
 - $\underline{4}$,468,523,628 Next digit is 4 or less. Billions place does not change. All digits to the right of the underlined place change to zero.
- **21.** 595,008 rounded to the nearest ten-thousand: 600,000

 $5\underline{9}5,008$ Next digit is 5 or more. Ten-thousands place changes (9+1=10). Write 0 and carry 1. All digits to the right of the underlined place change to zero.

- **22.** 725,182 rounded to the nearest ten-thousand: 730,000
 - $7\underline{2}5,182$ Next digit is 5 or more. Ten-thousands place changes (2+1=3). All digits to the right of the underlined place change to zero.

23. 4,860,220 rounded to the nearest million: 5,000,000

 $\underline{4}$,860,220 Next digit is 5 or more. Millions place changes (4 + 1 = 5). All digits to the right of the underlined place change to zero.

24. 13,713,409 rounded to the nearest million: 14,000,000

13,713,409 Next digit is 5 or more. Millions place changes (3 + 1 = 4). All digits to the right of the underlined place change to zero.

25. To the nearest ten: 4476

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 7. 4480

To the nearest hundred: 4476

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. **4500**

To the nearest thousand: $\underline{4}476$

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 4 as 4. **4000**

26. To the nearest ten: $64\underline{8}3$

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 8 as 8. **6480**

To the nearest hundred: 6483

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. **6500**

To the nearest thousand: 6483

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 6 as 6. 6000

27. To the nearest ten: 3374

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 7 as 7. 3370

To the nearest hundred: $3\underline{3}74$

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 3. **3400**

To the nearest thousand: 3374

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 3 as 3. 3000

28. To the nearest ten: 7632

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 3 as 3. **7630**

To the nearest hundred: $7\underline{6}32$

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 6 as 6. **7600**

To the nearest thousand: $\underline{7}632$

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 7. **8000**

29. To the nearest ten: $60\underline{4}8$

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. **6050**

To the nearest hundred: 6048

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 0 as 0. **6000**

To the nearest thousand: 6048

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 6 as 6. 6000

30. To the nearest ten: 7065

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 6. **7070**

To the nearest hundred: $7\underline{0}65$

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 0. **7100**

To the nearest thousand: 7065

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 7 as 7. **7000**

31. To the nearest ten: $53\underline{4}3$

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 4 as 4. **5340**

To the nearest hundred: 5343

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 3 as 3. **5300**

To the nearest thousand: 5343

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 5 as 5. 5000

32. To the nearest ten: 7456

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 5. **7460**

To the nearest hundred: 7456

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. **7500**

To the nearest thousand: 7456

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 7 as 7. **7000**

33. To the nearest ten: 19,539

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 3. **19.540**

To the nearest hundred: 19,539

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 5 as 5. 19,500

To the nearest thousand: 19,539

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 9. Write 0 and carry 1. **20,000**

34. To the nearest ten: 59,806

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 0. **59.810**

To the nearest hundred: 59,806

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 8 as 8. **59.800**

To the nearest thousand: 59,806

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 9. Write 0 and carry 1. **60,000**

35. To the nearest ten: 26,292

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 9 as 9. **26,290**

To the nearest hundred: 26,292

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 2. **26.300**

To the nearest thousand: 26,292

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 6 as 6. **26,000**

36. To the nearest ten: 78,519

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 1. **78,520**

To the nearest hundred: $78,\underline{5}19$

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 5 as 5. **78,500**

To the nearest thousand: 78,519

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 8. **79,000**

37. To the nearest ten: 93,706

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 0. **93,710**

To the nearest hundred: 93,706

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 7 as 7. **93,700**

To the nearest thousand: 93,706

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 3. **94.000**

38. To the nearest ten: 84,639

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 3. **84.640**

To the nearest hundred: 84,639

Next digit is 4 or less. All digits to the right of the underlined place are changed to zero. Leave 6 as 6. **84,600**

To the nearest thousand: 84,639

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. **85,000**

39. *Step 1* Locate the place to be rounded and underline it.

Step 2 Look only at the next digit to the right. If this digit is 5 or more, increase the underlined digit by 1.

Step 3 Change all digits to the right of the underlined place to zeros.

40. Step 1 Locate the place to be rounded and underline it.

Step 2 Look only at the next digit to the right. If this digit is 4 or less, do not change the underlined digit.

Step 3 Change all digits to the right of the underlined place to zeros.

44. Estimate: Exact:
$$\begin{array}{c} 60 & 57 \\ -20 & -24 \\ \hline \end{array}$$

45. Estimate: Exact:
$$\begin{array}{ccc}
70 & 67 \\
\times 30 & \times 34 \\
\hline
2100 & 268 \\
\underline{201} \\
2278
\end{array}$$

6.	Estimate:	Exact:
	50	53
	$\times 80$	× 75
	4000	265
		371
		3975

47.	Estimate:	Exact:
	900	863
	700	735
	400	438
	+800	+792
	2800	2828

4

$$\begin{array}{ccc} \textbf{49.} & \textit{Estimate:} & \textit{Exact:} \\ & 900 & 883 \\ & \underline{-400} & \underline{-448} \\ \hline & 500 & 435 \end{array}$$

$$\begin{array}{ccc} \textbf{57.} & \textit{Estimate:} & \textit{Exact:} \\ & 900 & 939 \\ & \times 30 & \times 29 \\ \hline 27,000 & 8451 \\ & & 1878 \\ \hline & 27,231 \\ \end{array}$$

$$\begin{array}{ccc} \textbf{58.} & \textit{Estimate:} & \textit{Exact:} \\ & 900 & 864 \\ & \times 70 & \times 74 \\ \hline & 63,000 & \hline & 3456 \\ & \underline{6048} \\ \hline & 63,936 & \hline \end{array}$$

- **59.** Perhaps the best explanation is that 3492 is closer to 3500 than 3400, but 3492 is closer to 3000 than to 4000.
- **60.** Rounding numbers usually allows for faster calculation and results in an estimated answer prior to getting an exact answer. One example is:

61. <u>7</u>6,000,000 Next digit is 5 or more. Change digit to the right of the underlined place to zero. Add 1 to 7. **80 million people**

3<u>1</u>1,000,000 Next digit is 4 or less. Change digit to the right of the underlined place to zero.

310 million people

62. 22,3<u>6</u>2,180 Next digit is 4 or less. Change digits to the right of the underlined place to zeros.

22,360,000 hot dogs

22,362,180 Next digit is 5 or more. Change digits to the right of the underlined place to zeros. Add 1 to 3. **22,400,000 hot dogs**

63. 348,900 Next digit is 5 or more. Change digit to the right of the underlined place to zero. Add 1 to 8. **349,000 streets**

 $3\underline{4}8,900$ Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. **350,000 streets**

64. 95 Next digit is 5 or more, so add 1 to 9. Change digit to the right of the underlined place to zero.100 streets

<u>2</u>7 Next digit is 5 or more, so add 1 to 2. Change digit to the right of the underlined place to zero. **30 streets**

65. To the nearest ten-thousand: 39,836,000

Next digit is 5 or more, so add 1 to 3. Change digits to the right of the underlined place to zeros.

39,840,000 tickets

To the nearest hundred-thousand: 39,836,000

Next digit is 4 or less. Hundred-thousands place doesn't change. All digits to the right of the underlined place are changed to zero.

39.800.000 tickets

To the nearest million: 39,836,000

Next digit is 5 or more, so add 1 to 9. Change digits to the right of the underlined place to zeros.

40,000,000 tickets

66. To the nearest ten-million: 57,4<u>6</u>3,625,000

Next digit is 4 or less. Ten-millions place doesn't change. All digits to the right of the underlined place are changed to zero. \$57,460,000,000

To the nearest hundred-million: 57,463,625,000

Next digit is 5 or more. All digits to the right of the underlined place are changed to zero. Add 1 to 4. \$57,500,000,000

To the nearest billion: 57,463,625,000

Next digit is 4 or less. Billions place doesn't change. All digits to the right of the underlined place are changed to zero. \$57,000,000,000

67. To the nearest thousand: 19,265,780

Next digit is 5 or more, so add 1 to 5. Change digits to the right of the underlined place to zeros.

19,266,000 players

To the nearest ten-thousand: $19,2\underline{6}5,780$

Next digit is 5 or more, so add 1 to 6. Change digits to the right of the underlined place to zeros.

19,270,000 players

To the nearest hundred-thousand: 19,265,780

Next digit is 5 or more, so add 1 to 2. Change digits to the right of the underlined place to zeros.

19,300,000 players

68. To the nearest ten: 221,543

Next digit is 4 or less. Tens place doesn't change. All digits to the right of the underlined place are changed to zero. **221,540 cars**

To the nearest hundred: 221,543

Next digit is 4 or less. Hundreds place doesn't change. All digits to the right of the underlined place are changed to zero. **221,500 cars**

To the nearest thousand: 221,543

Next digit is 5 or more, so add 1 to 1. Change digits to the right of the underlined place to zeros. **222,000 cars**

Relating Concepts (Exercises 69–75)

- **69.** 71,499 would round to 71,000, so the smallest whole number it could have been is 71,500.
- **70.** 72,500 would round to 73,000, so the largest whole number it could have been is 72,499.
- 71. 7500 is the smallest possible whole number that will round to 8000 using front end rounding.
- **72.** 8499 is the largest possible whole number that will round to 8000 using front end rounding.

73.	Exact:	Rounding to the nearest ten:
	3925	3930
	11,243	11,240
	15,974	15,970
	17,916	17,920
	534,883	534,880
	2,788,000	2,788,000

74.	Exact:	Front end rounded:
	3925	4000
	11,243	10,000
	15,974	20,000
	17,916	20,000
	534,883	500,000
	2,788,000	3,000,000

- **75.** (a) When using front end rounding, all digits are 0 except the first digit. These numbers are easier to work with when estimating answers.
 - **(b)** Sometimes when using front end rounding, the estimated answer can vary greatly from the exact answer.

1.8 Exponents, Roots, and Order of Operations

1.8 Margin Exercises

1. (a) 4^2 : exponent is 2; base is 4.

$$4^2 = 4 \times 4 = 16$$

(b) 5^3 : exponent is 3; base is 5.

$$5^3 = 5 \times 5 \times 5 = 125$$

(c) 3^4 : exponent is 4; base is 3.

$$3^4 = 3 \times 3 \times 3 \times 3 = 81$$

(d) 2^6 : exponent is 6; base is 2.

$$2^6 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 64$$

- **2.** (a) Because $2^2 = 4$, $\sqrt{4} = 2$.
 - **(b)** Because $5^2 = 25$, $\sqrt{25} = 5$.
 - (c) Because $6^2 = 36$, $\sqrt{36} = 6$.
 - (d) Because $15^2 = 225$, $\sqrt{225} = 15$.
 - (e) Because $1^2 = 1$, $\sqrt{1} = 1$.
- 3. (a) $4+5+2^2$ Evaluate exponent. $4+5+2\cdot 2$ Multiply. $4+5+\underline{4}$ Add from left to right. $9+\underline{4}=\underline{13}$
 - **(b)** $3^2 + 2^3$ Evaluate exponent. $3 \cdot 3 + 2 \cdot 2 \cdot 2$ Multiply from left to right. 9 + 8 = 17 Add.
 - (c) $60 \div \sqrt{36} \div 2$ Square root $60 \div 6 \div 2$ Divide left to right. $10 \div 2 = 5$ Divide.
 - (d) $8+6(14 \div 2)$ Work inside parentheses. 8+6(7) Multiply. 8+42=50 Add.
- **4.** (a) $12-6+4^2$ Evaluate exponent. $12-6+\underline{4}\cdot\underline{4}$ Multiply. 12-6+16 Subtract left to right. 6+16=22 Add.
 - (b) $2^3 + 3^2 (5 \cdot 3)$ Work inside parentheses. $2^3 + 3^2 - 15$ Evaluate exponents. 8 + 9 - 15 Add left to right. 17 - 15 = 2 Subtract.
 - (c) $20 \div 2 + (7 5)$ Work inside parentheses. $20 \div 2 + 2$ Divide. 10 + 2 = 12 Add.
 - (d) $15 \cdot \sqrt{9} 8 \cdot \sqrt{4}$ Square roots $15 \cdot 3 8 \cdot 2$ Multiply. 45 16 = 29 Subtract.

1.8 Section Exercises

- 1. 3^2 : exponent is 2, base is 3.
- 2. 2^3 : exponent is 3, base is 2.
- 3. 5^2 : exponent is 2, base is 5.
- 4. 4^2 : exponent is 2, base is 4.

5. 8^2 : exponent is 2, base is 8.

$$8^2 = 8 \cdot 8 = 64$$

6. 10^3 : exponent is 3, base is 10.

$$10^3 = 10 \cdot 10 \cdot 10 = 100 \cdot 10 = 1000$$

7. 15^2 : exponent is 2, base is 15.

$$15^2 = 15 \cdot 15 = 225$$

8. 11^3 : exponent is 3, base is 11.

$$11^3 = 11 \cdot 11 \cdot 11 = 121 \cdot 11 = 1331$$

- **9.** From the table, $4^2 = 16$, so $\sqrt{16} = 4$.
- **10.** From the table, $5^2 = 25$, so $\sqrt{25} = 5$.
- 11. From the table, $8^2 = 64$, so $\sqrt{64} = 8$.
- **12.** From the table, $6^2 = 36$, so $\sqrt{36} = 6$.
- 13. From the table, $10^2 = 100$, so $\sqrt{100} = 10$.
- **14.** From the table, $7^2 = 49$, so $\sqrt{49} = 7$.
- **15.** From the table, $12^2 = 144$, so $\sqrt{144} = 12$.
- **16.** From the table, $15^2 = 225$, so $\sqrt{225} = 15$.
- 17. False: 5^2 means that 5 is used as a factor 2 times, so $5^2 = 5 \cdot 5 = 25$.
- **18.** False: $4^2 = 4 \cdot 4 = 16$.
- **19.** False: 1 raised to any power is 1. Here, $1^3 = 1 \cdot 1 \cdot 1 = 1$.
- **20.** False: a number raised to the first power is the number itself, so $6^1 = 6$.
- **21.** $6^2 = 36$, so $\sqrt{36} = 6$.
- **22.** $9^2 = 81$, so $\sqrt{81} = 9$.
- **23.** $25^2 = 625$, so $\sqrt{625} = 25$.
- **24.** $50^2 = 2500$, so $\sqrt{2500} = 50$.
- **25.** $100^2 = \underline{10,000}$, so $\sqrt{10,000} = 100$.
- **26.** $60^2 = 3600$, so $\sqrt{3600} = 60$.
- 27. A perfect square is the square of a whole number. The number 25 is the square of 5 because $5 \cdot 5 = 25$.

The number 50 is not a perfect square. There is no whole number that can be squared to get 50.

- **28.** (1) Do all operations inside parentheses or other grouping symbols.
 - (2) Simplify any expressions with exponents and find any square roots.
 - (3) Multiply or divide, proceeding from left to right.
 - (4) Add or subtract, proceeding from left to right.

29.
$$3^2 + 8 - 5$$
 Exponent $9 + 8 - 5$ Add. $17 - 5 = 12$ Subtract. **TRUE**

30.
$$5^2 + 5 - 6$$
 Exponent $25 + 5 - 6$ Add. $30 - 6 = 24$ Subtract. TRUE

31.
$$6 + 8 \div 2$$
 Divide. $6 + 4 = 10$ *Add*.

The given statement is *false*. Multiplications and divisions are performed from *left* to *right*, then additions and subtractions.

32.
$$4 + 5(6 - 4)$$
 Parentheses $4 + 5(2)$ Multiply. $4 + 10 = 14$ Add.

The given statement is *false*. A common error is adding 4 to 5 first and then multiplying by 2. Follow the order of operations.

33.
$$3^2 + 8 - 5$$
 Exponent $9 + 8 - 5$ Add. $17 - 5 = 12$ Subtract.

34.
$$5^2 + 5 - 6$$
 Exponent $25 + 5 - 6$ Add. $30 - 6 = 24$ Subtract.

35.
$$25 \div 5(8-4)$$
 Parentheses $25 \div 5(4)$ Divide. $5(4) = 20$ Multiply.

36.
$$36 \div 18(7-3)$$
 Parentheses $36 \div 18 \cdot 4$ Divide. $2 \cdot 4 = 8$ Multiply.

37.
$$5 \cdot 3^2 + \frac{0}{8}$$
 Exponent
 $5 \cdot 9 + \frac{0}{8}$ Multiply.
 $45 + \frac{0}{8}$ Divide.
 $45 + 0 = 45$ Add.

38.
$$8 \cdot 3^2 - \frac{10}{2}$$
 Exponent $8 \cdot 9 - \frac{10}{2}$ Multiply. $72 - \frac{10}{2}$ Divide. $72 - 5 = 67$ Subtract.

39.
$$4 \cdot 1 + 8(9-2) + 3$$
 Parentheses $4 \cdot 1 + 8 \cdot 7 + 3$ Multiply. $4 + 56 + 3$ Add. $60 + 3 = 63$ Add.

40.
$$3 \cdot 2 + 7(3+1) + 5$$
 Parentheses $3 \cdot 2 + 7 \cdot 4 + 5$ Multiply. $6 + 28 + 5$ Add. $34 + 5 = 39$ Add.

41.
$$2^2 \cdot 3^3 + (20 - 15) \cdot 2$$
 Parentheses $2^2 \cdot 3^3 + 5 \cdot 2$ Exponents $4 \cdot 27 + 5 \cdot 2$ Multiply. $108 + 10 = 118$ Add.

42.
$$4^2 \cdot 5^2 + (20 - 9) \cdot 3$$
 Parentheses $4^2 \cdot 5^2 + 11 \cdot 3$ Exponents $16 \cdot 25 + 11 \cdot 3$ Multiply. $400 + 33 = 433$ Add.

43.
$$5 \cdot \sqrt{36} - 2(4)$$
 Square root $5 \cdot 6 - 2(4)$ Multiply. $30 - 8 = 22$ Subtract.

44.
$$2 \cdot \sqrt{100} - 3(4)$$
 Square root $2 \cdot 10 - 3(4)$ Multiply. $20 - 12 = 8$ Subtract.

45.
$$8(2) + 3 \cdot 7 - 7$$
 Multiply. $16 + 21 - 7$ *Add.* $37 - 7 = 30$ *Subtract.*

46.
$$10(3) + 6 \cdot 5 - 20$$
 Multiply. $30 + 30 - 20$ Add. $60 - 20 = 40$ Subtract.

47.
$$2^3 \cdot 3^2 + 3(14 - 4)$$
 Parentheses $2^3 \cdot 3^2 + 3(10)$ Exponents $8 \cdot 9 + 3(10)$ Multiply. $72 + 30 = 102$ Add.

48.
$$3^2 \cdot 4^2 + 2(15 - 6)$$
 Parentheses $3^2 \cdot 4^2 + 2(9)$ Exponents $9 \cdot 16 + 2(9)$ Multiply. $144 + 18 = 162$ Add.

49.
$$7 + 8 \div 4 + \frac{0}{7}$$
 Divide.
 $7 + 2 + \frac{0}{7}$ Divide.
 $7 + 2 + 0$ Add.
 $9 + 0 = 9$ Add.

50.
$$6+8 \div 2 + \frac{0}{8}$$
 Divide. $6+4+\frac{0}{8}$ Divide. $6+4+0$ Add. $10+0=10$ Add.

51.
$$3^2 + 6^2 + (30 - 21) \cdot 2$$
 Parentheses $3^2 + 6^2 + 9 \cdot 2$ Exponents $9 + 36 + 9 \cdot 2$ Multiply. $9 + 36 + 18$ Add. $45 + 18 = 63$ Add.

52.
$$4^2 + 5^2 + (25 - 9) \cdot 3$$
 Parentheses $4^2 + 5^2 + 16 \cdot 3$ Exponents $16 + 25 + 16 \cdot 3$ Multiply. $16 + 25 + 48$ Add. $41 + 48 = 89$ Add.

- 53. $7 \cdot \sqrt{81} 5 \cdot 6$ Square root $7 \cdot 9 5 \cdot 6$ Multiply. 63 30 = 33 Subtract.
- **54.** $6 \cdot \sqrt{64} 6 \cdot 5$ Square root $6 \cdot 8 6 \cdot 5$ Multiply. 48 30 = 18 Subtract.
- **55.** $8 \cdot 2 + 5(3 \cdot 4) 6$ Parentheses $8 \cdot 2 + 5(12) 6$ Multiply. 16 + 60 6 Add. 76 6 = 70 Subtract.
- **56.** $5 \cdot 2 + 3(5+3) 6$ Parentheses $5 \cdot 2 + 3(8) 6$ Multiply. 10 + 24 6 Add. 34 6 = 28 Subtract.
- **57.** $4 \cdot \sqrt{49} 7(5 2)$ Parentheses $4 \cdot \sqrt{49} 7 \cdot 3$ Square root $4 \cdot 7 7 \cdot 3$ Multiply. 28 21 = 7 Subtract.
- **58.** $3 \cdot \sqrt{25} 6(3 1)$ Parentheses $3 \cdot \sqrt{25} 6 \cdot 2$ Square root $3 \cdot 5 6 \cdot 2$ Multiply. 15 12 = 3 Subtract.
- **59.** $7(4-2) + \sqrt{9}$ Parentheses $7(2) + \sqrt{9}$ Square root 7(2) + 3 Multiply. 14 + 3 = 17 Add.
- 60. $5(4-3) + \sqrt{9}$ Parentheses $5(1) + \sqrt{9}$ Square root 5(1) + 3 Multiply. 5+3=8 Add.
- 61. $7^2 + 3^2 8 + 5$ Exponents 49 + 9 - 8 + 5 Add. 58 - 8 + 5 Subtract. 50 + 5 = 55 Add.
- 62. $3^2 2^2 + 3 2$ Exponents 9 - 4 + 3 - 2 Subtract. 5 + 3 - 2 Add. 8 - 2 = 6 Subtract.
- **63.** $5^2 \cdot 2^2 + (8-4) \cdot 2$ Parentheses $5^2 \cdot 2^2 + 4 \cdot 2$ Exponents $25 \cdot 4 + 4 \cdot 2$ Multiply. 100 + 8 = 108 Add.

- **64.** $5^2 \cdot 3^2 + (30 20) \cdot 2$ Parentheses $5^2 \cdot 3^2 + 10 \cdot 2$ Exponents $25 \cdot 9 + 10 \cdot 2$ Multiply. 225 + 20 = 245 Add.
- 65. $5+9 \div 3+6 \cdot 3$ Divide. $5+3+6 \cdot 3$ Multiply. 5+3+18 Add. 8+18=26 Add.
- **66.** $8+3 \div 3+6 \cdot 3$ Divide. $8+1+6 \cdot 3$ Multiply. 8+1+18 Add. 9+18=27 Add.
- 67. $8 \cdot \sqrt{49} 6(9 4)$ Parentheses $8 \cdot \sqrt{49} 6(5)$ Square root $8 \cdot 7 6(5)$ Multiply. 56 30 = 26 Subtract.
- **68.** $8 \cdot \sqrt{49} 6(5+3)$ Parentheses $8 \cdot \sqrt{49} 6(8)$ Square root $8 \cdot 7 6(8)$ Multiply. 56 48 = 8 Subtract.
- 69. $5^2 4^2 + 3 \cdot 6$ Exponent $25 - 16 + 3 \cdot 6$ Multiply. 25 - 16 + 18 Subtract. 9 + 18 = 27 Add.
- **70.** $3^2 + 6^2 5 \cdot 8$ Exponent $9 + 36 5 \cdot 8$ Multiply. 9 + 36 40 Add. 45 40 = 5 Subtract.
- 71. $8+8 \div 8+6+\frac{5}{5}$ Divide. 8+1+6+1 Add. 9+6+1 Add. 15+1=16 Add.
- 72. $3+14 \div 2+7+\frac{8}{8}$ Divide. 3+7+7+1 Add. 10+7+1 Add. 17+1=18 Add.
- 73. $6 \cdot \sqrt{25} 7(2)$ Square root $6 \cdot 5 7 \cdot 2$ Multiply. 30 14 = 16 Subtract.
- 74. $8 \cdot \sqrt{36} 4(6)$ Square root $8 \cdot 6 4(6)$ Multiply. 48 24 = 24 Subtract.
- **75.** $9 \cdot \sqrt{16} 3 \cdot \sqrt{25}$ Square roots $9 \cdot 4 3 \cdot 5$ Multiply. 36 15 = 21 Subtract.

- **76.** $6 \cdot \sqrt{81} 3 \cdot \sqrt{49}$ Square roots $6 \cdot 9 3 \cdot 7$ Multiply. 54 21 = 33 Subtract.
- 77. $7 \div 1 \cdot 8 \cdot 2 \div (21 5)$ Parentheses $7 \div 1 \cdot 8 \cdot 2 \div 16$ Divide. $7 \cdot 8 \cdot 2 \div 16$ Multiply. $56 \cdot 2 \div 16$ Multiply. $112 \div 16 = 7$ Divide.
- **78.** $12 \div 4 \cdot 5 \cdot 4 \div (15 13)$ Parentheses $12 \div 4 \cdot 5 \cdot 4 \div 2$ Divide. $3 \cdot 5 \cdot 4 \div 2$ Multiply. $15 \cdot 4 \div 2$ Multiply. $60 \div 2 = 30$ Divide.
- **79.** $15 \div 3 \cdot 2 \cdot 6 \div (14 11)$ Parentheses $15 \div 3 \cdot 2 \cdot 6 \div 3$ Divide. $5 \cdot 2 \cdot 6 \div 3$ Multiply. $10 \cdot 6 \div 3$ Multiply. $60 \div 3 = 20$ Divide.
- **80.** $9 \div 1 \cdot 4 \cdot 2 \div (11 5)$ Parentheses $9 \div 1 \cdot 4 \cdot 2 \div 6$ Divide. $9 \cdot 4 \cdot 2 \div 6$ Multiply. $36 \cdot 2 \div 6$ Multiply. $72 \div 6 = 12$ Divide.
- **81.** $6 \cdot \sqrt{25} 4 \cdot \sqrt{16}$ Square roots $6 \cdot 5 4 \cdot 4$ Multiply. 30 16 = 14 Subtract.
- **82.** $10 \cdot \sqrt{49} 4 \cdot \sqrt{64}$ Square roots $10 \cdot 7 4 \cdot 8$ Multiply. 70 32 = 38 Subtract.
- **83.** $5 \div 1 \cdot 10 \cdot 4 \div (17 9)$ Parentheses $5 \div 1 \cdot 10 \cdot 4 \div 8$ Divide. $5 \cdot 10 \cdot 4 \div 8$ Multiply. $50 \cdot 4 \div 8$ Multiply. $200 \div 8 = 25$ Divide.
- **84.** $15 \div 3 \cdot 8 \cdot 9 \div (12 8)$ Parentheses $15 \div 3 \cdot 8 \cdot 9 \div 4$ Divide. $5 \cdot 8 \cdot 9 \div 4$ Multiply. $40 \cdot 9 \div 4$ Multiply. $360 \div 4 = 90$ Divide.
- **85.** $8 \cdot 9 \div \sqrt{36} 4 \div 2 + (14 8)$ Parentheses $8 \cdot 9 \div \sqrt{36} 4 \div 2 + 6$ Square root $8 \cdot 9 \div 6 4 \div 2 + 6$ Multiply. $72 \div 6 4 \div 2 + 6$ Divide. 12 2 + 6 Subtract. 10 + 6 = 16 Add.

- **86.** $3-2+5\cdot 4\cdot \sqrt{144} \div \sqrt{36}$ Square roots $3-2+5\cdot 4\cdot 12\div 6$ Multiply. $3-2+20\cdot 12\div 6$ Multiply. $3-2+240\div 6$ Divide. 3-2+40 Subtract. 1+40=41 Add.
- **87.** $2+1-2 \cdot \sqrt{1}+4 \cdot \sqrt{81}-7 \cdot 2$ Square roots $2+1-2 \cdot 1+4 \cdot 9-7 \cdot 2$ Multiply. 2+1-2+36-14 Add. 3-2+36-14 Subtract. 1+36-14 Add. 37-14=23 Subtract.
- **88.** $6-4+2\cdot 9-3\cdot \sqrt{225} \div \sqrt{25}$ Square roots $6-4+2\cdot 9-3\cdot 15\div 5$ Multiply. $6-4+18-45\div 5$ Divide. 6-4+18-9 Subtract. 2+18-9 Add. 20-9=11 Subtract.
- **89.** $5 \cdot \sqrt{36} \cdot \sqrt{100} \div 4 \cdot \sqrt{9} + 8$ Square roots $5 \cdot 6 \cdot 10 \div 4 \cdot 3 + 8$ Multiply. $30 \cdot 10 \div 4 \cdot 3 + 8$ Multiply. $300 \div 4 \cdot 3 + 8$ Divide. $75 \cdot 3 + 8$ Multiply. 225 + 8 = 233 Add.
- **90.** $9 \cdot \sqrt{36} \cdot \sqrt{81} \div 2 + 6 3 5$ Square roots $9 \cdot 6 \cdot 9 \div 2 + 6 3 5$ Multiply. $54 \cdot 9 \div 2 + 6 3 5$ Multiply. $486 \div 2 + 6 3 5$ Divide. 243 + 6 3 5 Add. 249 3 5 Subtract. 246 5 = 241 Subtract.

1.9 Reading Pictographs, Bar Graphs, and Line Graphs

1.9 Margin Exercises

- 1. (a) The Rock and Roll/Rhythm and Blues stamp had the second greatest number (4) of sales since that row has the second most stamp symbols.
 - **(b)** There is about one more stamp in the Rock and Roll/Rhythm and Blues row than in the Art of Disney Romance row. Since one stamp represents 20 million stamps, there were about 20,000,000 more Rock and Roll/Rhythm and Blues stamps sold.
- 2. (a) Secret account or card: 27 out of 100
 - **(b)** Misrepresented purchased price: 39 out of 100
 - (c) Hid purchases: 42 out of 100
 - (d) Hid debt: 26 out of 100
 - (e) Did not tell credit score: 12 out of 100

- **3. (a)** For the year 2050, the dot is very close to the horizontal line marked <u>4</u>, so the predicted population is about 400,000,000 people in 2050.
 - **(b)** About 475,000,000 people in 2075
 - (c) About 575,000,000 people in 2100

1.9 Section Exercises

- The number of pictures or symbols for the Walgreens retail stores is 8. Since each symbol represents 500 stores, Walgreens has 8 500 = 4000 stores.
- 2. The number of pictures or symbols for the CVS retail stores is $8\frac{1}{2}$. Since each symbol represents $\underline{500}$ stores, CVS has $8\frac{1}{2} \cdot \underline{500} = \underline{4250}$ stores.
- 3. There are 9 symbols, so the number of retail stores for Family Dollar is about $9 \cdot 500 = 4500$ stores.
- 4. There are $10\frac{1}{2}$ symbols, so the number of retail stores for 7-Eleven is about

$$(10 \cdot 500) + \frac{1}{2} \cdot 500 = 5000 + 250 = 5250.$$

5. From the pictograph, Dollar General has the greatest number of retail stores. There are $11\frac{1}{2}$ symbols, so the number of retail

stores for Dollar General is about
$$11 \cdot 500 + \frac{1}{2} \cdot 500 = 5500 + 250 = 5750.$$

 According to the pictograph, the two companies that have the least number of retail stores are Rite-Aid and Walmart.

There are 7 symbols, so the number of retail stores for Rite-Aid and Walmart is about $7 \cdot 500 = 3500$.

7. Using the results from Exercises 3 and 5, we see that Family Dollar has about

$$5750 - 4500 = 1250$$
 fewer stores

than does Dollar General.

- **8.** Walgreens has one more symbol than Walmart, so Walgreens has 500 more stores than Walmart.
- **9.** The number of working adults who were surveyed is 100 (see the directions above the chart).
- **10.** The number of career paths that were included in the survey is 7 (see the horizontal labels in the chart).
- **11.** From the bar graph, 9 people out of 100 found their career as a result of training for a job.
- **12.** From the bar graph, 18 people out of 100 found their careers because they studied for the career in school.

- **13. (a)** According to the bar graph, the greatest number of people found their job by seeing an ad.
 - **(b)** From the bar graph, <u>25 people</u> out of 100 found their career as a result of seeing an ad.
- **14.** (a) From the bar graph, the least number of people found their career by being promoted from within.
 - **(b)** From the bar graph, <u>6 people</u> out of 100 found their career as a result of being promoted from within.
- 15. According to the bar graph, 18 9 = 9 more people out of 100 found their career as a result of "Studied in school" than "Luck or chance."
- 16. From the bar graph, 18 + 9 = 27 people out of 100 found their career as a result of either "Studied in school" or "Trained for a job."
- 17. According to the line graph, the year with the greatest number of installations is 2014, with 7000 installations.
- **18.** From the line graph, <u>2009</u> and <u>2013</u> were the two years with the least number of installations. There were <u>2500</u> installations in each of these years.
- 19. According to the line graph the increase in the number of installations from 2013 to 2014 is 7000 2500 = 4500.
- 20. 4000 installations in 2012 -2500 installations in 2013 1500 decrease in installations

The decrease in the number of installations from 2012 to 2013 is 1500.

- **21.** Possible answers are:
 - 1. shortage of units to install;
 - 2. lack of qualified workers;
 - 3. poor economy;
 - 4. less demand for solar products.
- **22.** Possible answers are:
 - 1. greater demand;
 - 2. more units available;
 - 3. many qualified workers;
 - 4. tax incentives for solar projects.

Relating Concepts (Exercises 23–27)

23. We want to insert parentheses in $7 - 2 \cdot 3 - 6$ so that it simplifies to 9. There isn't a method to use, so just use trial and error.

$$(7-2) \cdot 3 - 6 = 5 \cdot 3 - 6 = 15 - 6 = 9$$

- **24.** $(4+2) \cdot (5+1) = 6 \cdot 6 = 36$
- **25.** $36 \div (3 \cdot 3) \cdot 4 = 36 \div 9 \cdot 4 = 4 \cdot 4 = 16$

26.
$$56 \div (2 \cdot 2 \cdot 2) + \frac{0}{6} = 56 \div 8 + \frac{0}{6}$$

= $7 + \frac{0}{6}$
= $7 + 0 = 7$

27. (a) Start with the top and work counterclockwise:

$$7920 + 1320 + 2640 + (5280 - 1320 - 1320) + 2640 + 1320 + 7920 + 5280$$

(b) (5280 - 1320 - 1320) = 2640, so we can add as follows:

So 31,680 feet are needed for one strand and thus, $3 \times 31,680 = 95,040$ feet are needed for a threestrand barbed wire fence.

(c) Divide the answer from part (b) by 5280.

$$\begin{array}{r}
 18 \\
5280 \overline{\smash)95,040} \\
 \underline{5280} \\
 42240 \\
 \underline{42240} \\
 0
\end{array}$$

18 miles of barbed wire are needed for the fence.

1.10 Solving Application Problems

1.10 Margin Exercises

1. (a) A grocery clerk's hourly wage: \$1.40 is eliminated (too low) \$140 is eliminated (too high) \$14 is most reasonable

\$1.40; \$14; \$140

(b) The total length of five sports-utility vehicles: One vehicle is at least 10 feet, so five vehicles measure at least 50 feet. Only 80 feet is reasonable.

8 feet; 18 feet; 80 feet; 800 feet

- (c) The cost of heart bypass surgery: \$1000; \$100,000; \$10,000,000
- (a) Step 1 The total number of fossils is given, 2. and the number each person receives must be found.

Step 2 "Divided equally" indicates division should be used.

Step 3 80 fossils divided equally among 4 people gives an estimate of 20 fossils per person.

Step 4
$$\frac{21}{484}$$

Step 5 Each person receives 21 fossils.

Step 6 21 amount received by each person \times 4 number of people 84 total fossils; matches

- **(b)** *Step 1* The total number of children and the number of children assigned to each counselor is given. The number of counselors needed must be
- **Step 2** "12 children are assigned to *each* camp counselor" indicates division should be used.

Step 3 If we replace 408 and 12 with 400 and 10, our estimate is $400 \div 10 = 40$.

- There are 34 counselors needed.
- Step 6 34 counselors imes 12 children per counselor 408 total children: matches
- (a) Step 1 The number of points on 3. examinations and quizzes is given. The total number of points must be found.
 - Step 2 "Her total points" indicates addition should be used.
 - Step 3 Rounding each score to the nearest ten gives 90, 80, 80, 100, 20, 10, 20, and 10. The sum of these scores gives an estimate of 410 points.

Step 5 Her total is 410 points.

- **Step 6** The answer is the same as the estimate, so it is reasonable. Add the numbers again to check.
- **(b)** *Step 1* The customer contacts for each day are given. The total number of contacts for the week must be found.
- **Step 2** Adding the daily numbers to find the weekly total seems reasonable.
- **Step 3** Rounding each day's contacts to the nearest ten gives 80, 60, 120, 100, and 200. The sum gives an estimate of 560 customer contacts.

- **Step 5** Stephanie had 558 customer contacts for the week.
- **Step 6** The answer is reasonable. A check shows that the answer is correct.
- **4. (a)** *Step 1* The areas in square miles of two states is given. The difference must be found.
 - Step 2 "Difference" indicates subtraction should be used.
 - **Step 3** Rounding each number of square miles to the nearest thousand gives 663,000 269,000 = 394,000 square miles.

- **Step 5** The difference in the number of square miles is 394,687 square miles.
- **Step 6** The answer is reasonable.

$$\begin{array}{c} \textbf{Check} & 268{,}580 \\ & +394{,}687 \\ \hline & 663{,}267 \end{array} \ \, \textit{matches}$$

- **(b)** *Step 1* We know the beginning balance and the check amount, and need to find the new balance.
- **Step 2** Subtracting the numbers seems reasonable.
- **Step 3** Using the values \$14,900 and \$1200 in place of \$14,863 and \$1180 gives us \$14,900 \$1200 = \$13,700 as an estimate.

- **Step 5** The amount remaining in the club account is \$13,683.
- **Step 6** The answer is reasonable.

- **5. (a)** *Step 1* The amount per camera, number of cameras, and total rebate are given. The final cost is to be found.
 - **Step 2** Use multiplication to find the cost for all cameras, and then use subtraction to find the final cost.
 - **Step 3** An estimate would be $320 \cdot \$130 \$2500 = \$41,600 \$2500 = \$39,100.$

Step 4
 \$129
 \$41,022

$$\times$$
 318
 -2470

 \$41,022
 \$38,552

- Step 5 The final cost of the cameras is \$38,552.
- **Step 6** The answer is close to the estimate, so it is reasonable. Check by adding the rebate to the final cost and then dividing by 318. \$38,552 + \$2470 = \$41,022

$$\begin{array}{c}
1 & 2 & 9 \\
318 \overline{\smash)4\ 1,022} \\
\underline{318} \\
9 & 2 & 2 \\
\underline{636} \\
2862 \\
\underline{2862} \\
0
\end{array}$$
 $\leftarrow 1 \times 318$

- \$129 matches the amount per camera given in the problem.
- **(b)** *Step 1* The number of books sold and the number of those returned is given. The profit for each book sold is also given. The total profit on the books sold and not returned must be found.
- **Step 2** "Remaining" indicates subtraction. The number of books returned should be subtracted from the number sold and that number multiplied by the profit per book.
- **Step 3** Estimate that 13,000 books are sold, and 1000 of those are returned. A reasonable estimate of the number of books remaining after the returns is 13,000 1000 = 12,000. Each book has a profit of \$6, so $12,000 \times $6 = $72,000$.

Step 4

$$12,628$$
 $11,765$
 -863
 \times 6

 $11,765$
 $\$70,590$

- **Step 5** The total profit for the books remaining after the returns is \$70.590.
- **Step 6** The answer is reasonable since it is close to the estimate.

1.10 Section Exercises

- 1. Choice C, 25 hours, is *not* reasonable since there are only 24 hours in a day.
- **2.** Choice **B**, \$100/hour, is *not* reasonable for the hourly earnings of a part-time student employee.
- **3.** Choice **A**, \$5, is reasonable for the cost of lunch at a fast food restaurant.
- **4.** Choice **B**, 25 mpg, is reasonable for the gas mileage of your car.
- **5. Step 1** Given the number of five types of sandwiches sold, find the total number of sandwiches sold.
 - **Step 2** Addition seems reasonable since we want a total.
 - Step 3 The total number of sandwiches should be about $600 + 900 + \underline{1000} + 800 + \underline{2000} = \underline{5300}$ sandwiches.

- **Step 5** The total number of sandwiches sold is 5208.
- **Step 6** The answer is reasonably close to the estimate. Check by adding the values again.
- **6. Step 1** Given the number of five types of items manufactured, find the total.
 - Step 2 Addition seems reasonable to use.

Step 3
$$30,000 + 5000 + 2000 + 20,000 + 10,000 = 67,000$$
 units is an estimate.

- **Step 5** The total number of items manufactured is 64,788.
- **Step 6** The answer is reasonably close to the estimate. Check by adding the values again.
- 7. **Step 1** Given two prices for car rentals, find the difference.
 - **Step 2** "How much is saved" indicates subtraction could be used.
 - **Step 3** An estimate is \$300 \$200 = \$100 saved.

- Step 5 Paying ahead will save \$104.
- **Step 6** The answer is reasonably close to the estimate. **Check** \$104 + \$192 = \$296
- **8. Step 1** Given two population numbers, find the difference.
 - **Step 2** "Find the expected increase" indicates subtraction could be used.
 - **Step 3** An estimate is 500 300 = 200 million people.

Step 4 478
$$\frac{-311}{167}$$

- *Step 5* The expected increase in population is 167 million people.
- **Step 6** The answer is reasonably close to the estimate. **Check** 167 + 311 = 478
- 9. **Step 1** The number of kits packaged in one hour is given and the total number of kits packaged in 24 hours must be found.
 - **Step 2** Multiply the number of kits packaged in 1 hour by 24.
 - **Step 3** A reasonable answer would be $200 \times 20 = 4000$.

$$\begin{array}{r} \textit{Step 4} & 236 \\ \times 24 \\ \hline 944 \\ \hline 472 \\ \hline 5664 \\ \end{array}$$

- *Step 5* 5664 kits are packaged in 24 hours.
- **Step 6** The answer is reasonably close to the estimate, which is clearly low.

- **10.** *Step 1* Find the number of tickets sold in a 12-day period.
 - **Step 2** The number of tickets sold in one day is given. To find "how many in a 12-day period," multiply.
 - **Step 3** 10 times 500 gives an estimate of 5000 tickets.

- Step 5 In a 12-day period, 5400 tickets are sold.
- **Step 6** Check 4 5 0 12 5 4 0 0
- **11.** *Step 1* Find the number of toys each child will receive.
 - **Step 2** "Same number of toys to each" indicates division should be used.
 - *Step 3* 3000 divided by 700 gives an estimate of about 4 toys.

- **Step 5** Each child will receive 4 toys.
- **Step 6** $4 \times 657 = 2628$
- **12.** *Step 1* Find the amount each employee will receive.
 - Step 2 "Divide evenly" indicates division.
 - **Step 3** \$700,000 \div 1000 gives an estimate of \$700.

Step 4
$$\rightarrow 680,000$$
 $\rightarrow 1680,000$

- **Step 5** Each employee will receive \$680.
- **Step 6** Check $680 \times 1000 = 680,000$
- **13.** *Step 1* The amount saved per month and the number of months are given. Find the total amount saved.
 - Step 2 Multiply the two given values.
 - **Step 3** A reasonable answer would be $\$30 \times 5 = \150 .

Step 4
$$34$$
 $\times 5$ 170

- Step 5 \$170 could be saved.
- Step 6 The answer is reasonably close to the estimate. Check $\frac{3}{5}$ $\frac{4}{17^{20}}$
- **14.** *Step 1* The cost of tuition and fees per quarter and the number of quarters are given. Find the total amount needed for tuition and fees.
 - Step 2 Multiply the two given values.
 - **Step 3** A reasonable answer would be $\$800 \times 5 = \4000 .

- **Step 5** The total amount needed for tuition and fees is \$3925.
- **15.** *Step 1* Given two numbers, find the total.
 - **Step 2** "Find the total" indicates addition could be used.
 - Step 3 An estimate is $100,000 + 300,000 = \underline{400,000 \text{ deaths}}$.

- **Step 5** The total number of Union deaths in the Civil War was 360,222.
- **Step 6** The answer is reasonably close to the estimate. **Check** 360,222 250,152 = 110,070
- **16.** *Step 1* Given two numbers, find the total.
 - **Step 2** "Find the total" indicates addition could be used.
 - Step 3 An estimate is 90,000 + 200,000 = 290,000 deaths.

- **Step 5** The total number of Confederate deaths in the Civil War was 258,420.
- **Step 6** The answer is reasonably close to the estimate. **Check** 258,420 164,300 = 94,120
- 17. Step 1 Given two numbers, find the difference.
 - **Step 2** "How many more" indicates subtraction could be used.

- **Step 3** An estimate is 300,000 100,000 = 200,000 deaths.
- Step 4 250,152 - 110,070 140,082
- *Step 5* There were 140,082 more Union deaths that resulted from disease than from battle.
- **Step 6** The answer is reasonably close to the estimate. **Check** 140,082 + 110,070 = 250,152
- **18.** Step 1 Given two numbers, find the difference.
 - **Step 2** "How many more" indicates subtraction could be used.
 - **Step 3** An estimate is 200,000 90,000 = 110,000 deaths.

- *Step 5* There were 70,180 more Confederate deaths that resulted from disease than from battle.
- **Step 6** The answer is reasonably close to the estimate. **Check** 70,180 + 94,120 = 164,300
- **19.** *Step 1* Given four numbers, find the total.
 - **Step 2** "Find the total" indicates addition could be used.
 - **Step 3** An estimate is 100,000 + 300,000 + 90,000 + 200,000 = 690,000 deaths.

- **Step 5** The total number of deaths in the Civil War was 618,642.
- **Step 6** The answer is reasonably close to the estimate. **Check** 618,642 164,300 94,120 250,152 = 110,070
- **20.** *Step 1* Given four numbers, find the difference between the sum of the first pair and the sum of the second pair.
 - **Step 2** "How many more" indicates subtraction could be used after adding the pairs.
 - **Step 3** An estimate is 100,000 + 300,000 (90,000 + 200,000) = 110,000 deaths.

Step 4

$$110,070 + 250,152 - (94,120 + 164,300)$$

= $360,222 - (258,420)$
= 101.802

- **Step 5** There were 101,802 more Union deaths than Confederate deaths in the Civil War.
- **Step 6** The answer is reasonably close to the estimate. **Check** Using the sums of the pairs of numbers, 101,802 + 258,420 = 360,222.
- 21. Step 1 Find her monthly savings.
 - **Step 2** Her monthly take home pay and expenses are given. "Remainder" indicates subtraction may be used.
 - **Step 3** Estimate: \$2000 \$700 \$300 \$400 \$200 \$200 = \$200

- Step 5 Her monthly savings are \$350.
- Step 6 The answer seems reasonable for the given estimate. Check \$350 + \$1890 = \$2240. Re-add the expenses to check the sum of \$1890.
- **22.** *Step 1* Find the amount remaining in the bank account.
 - **Step 2** Add to find the total amount of the payments. Subtract that total from the balance in the account.
 - **Step 3** About \$300 + \$600 + \$800 = \$1700 was spent. His balance is about \$3000 \$1700 = \$1300.

- **Step 5** \$1208 remains in the account.
- **Step 6** The answer is reasonably close to the estimate. **Check** \$1208 + \$1666 = \$2874. Readd the payments to check the sum of \$1666.
- **23.** *Step 1* The square feet in one acre is given and the square feet in the given number of acres must be found.
 - **Step 2** Multiply the square feet in one acre by the total number of acres.
 - Step 3 An estimate is

$$40,000 \times 100 = 4,000,000 \text{ ft}^2$$
.

Step 5 There are 6,011,280 square feet in 138 acres. The answer is reasonable considering the rounding that was done in finding the estimate.

Step 6 Check
$$\frac{43,560}{138 | 6,011,280}$$

- **24.** *Step 1* Find the number of gallons polluted in a year.
 - *Step 2* Multiply by 365 to find the amount polluted in a year.
 - Step 3 $200,000 \times 400$ gives an estimate of 80,000,000 gallons.

- *Step 5* Each year 76,529,550 gallons are polluted.
- **Step 6** The answer is reasonably close to the estimate. **Check** $76,529,550 \div 209,670 = 365$
- **25.** *Step 1* Find the total cost of all Safety and Security Options.
 - **Step 2** Add the costs of the options to find the total cost.

- Step 5 The total cost is \$1254.
- **Step 6** The answer is reasonably close to the estimate. Check by re-adding the costs.
- **26.** *Step 1* The total cost of all Interior Options must be found.
 - **Step 2** Add the costs of the options to find the total cost.

Step 3 Estimate:
$$$300 + $50 + $300 + $1800 + $80 + $400 = $2930$$

- Step 5 The total cost is \$3001.
- **Step 6** The answer is reasonably close to the estimate. Check by re-adding the costs.
- **27. Step 1** An option package is offered. We must find how much can be saved if the customer buys the option package instead of paying for each option separately.
 - **Step 2** First, add the costs of the options. Then subtract the cost of the option package from this total.

Step 3 Estimate:
$$$300 + $70 + $400 + $200 = $970$$

 $$970 - $800 = 170

- *Step 5* Jill can save \$185 by buying the option package.
- Step 6 The answer is reasonably close to the estimate. Check \$785 + 185

$$+185$$
 \$970

- **28. Step 1** An option package is offered. We must find how much can be saved if the customer buys the option package instead of paying for each option separately.
 - **Step 2** First, add the costs of the options. Then subtract the cost of the option package from this total.

Step 5 Samuel can save \$205 by buying the option package.

Step 6 The answer is reasonably close to the estimate. **Check** \$1495

$$\frac{+205}{\$1700}$$

- **29.** *Step 1* The number and cost of wheelchairs and recorder-players are given and the total cost of all items must be found.
 - **Step 2** Find the cost of all wheelchairs and the cost of all recorder-players. Then add these costs to get the total cost.
 - **Step 3** The cost of the wheelchairs is about $$1000 \times 6 = 6000 .

The cost of the recorder-players is about $$900 \times 20 = $18,000$.

Estimate: \$6000 + \$18,000 = \$24,000

Step 4 cost of wheelchairs: \$1256

$$\frac{\times 6}{\$7536}$$

cost of recorder-players:

$$\begin{array}{r} $895 \\ \times 15 \\ \hline 4475 \\ 895 \\ \hline \$13,425 \end{array}$$

Step 5 The total cost is
$$$13,425 + $7536 = $20,961$$
.

Step 6 The answer is reasonably close to the estimate. Check by repeating Step 4.

- **30.** *Step 1* Find the total cost.
 - **Step 2** To find the cost of the computers use multiplication. The cost of the printers must also be found using multiplication. Finally, the two totals must be added.

Step 3 Estimate:
$$(\$500 \times 20) + (\$500 \times 10)$$

= $\$10,000 + \$5000 = \$15,000$

Step 5 The total cost is \$14,868.

Step 6 The answer is reasonably close to the estimate. Check by repeating Step 4.

31. Possible answers are

Addition: more; total; gain of Subtraction: less; loss of; decreased by Multiplication: twice; of; product Division: divided by; goes into; per Equals: is; are

- **32.** (1) Read the problem carefully.
 - (2) Work out a plan.
 - (3) Estimate a reasonable answer.
 - (4) Solve the problem.
 - (5) State the answer.
 - (6) Check your work.
- **33.** *Step 1* The daily sales figures are given and the weekly total must be found.

Step 2 Add the daily sales figures to get the weekly total.

Step 3 Estimate:

- Step 5 The weekly total is \$20,009.
- **Step 6** The answer is reasonably close to the estimate. Check by repeating Step 4.
- **34.** *Step 1* The daily number of visitors is given and the weekly total must be found. Assume the numbers correspond to Monday through Sunday.

Step 2 Add the daily figures to get the weekly total.

Step 3 Estimate: 5000 + 5000 -

5000 + 3000 + 5000 + 2000 +4000 + 2000 + 7000 = 28,000

- Step 5 The weekly total is 28,430 visitors.
- **Step 6** The answer is reasonably close to the estimate. Check by repeating Step 4.
- 35. Step 1 Find the final weight of the car.
 - **Step 2** The second engine weighs more than the first engine. Find the difference and add it to the weight of the car.
 - **Step 3** 582 and 634 both round to 600, so the difference is 0 and an estimate of the car's weight is just its original weight, 2425 pounds.

Step 4

- Step 5 The car will weigh 2477 pounds.
- **Step 6** The answer is reasonable since it's just slightly more than the original weight.

$$\begin{array}{ccc} \textbf{Check} & 2425 & 1843 \\ & -582 & +634 \\ \hline & 1843 & 2477 \end{array}$$

- **36.** *Step 1* Find the balance in the preschool operating account.
 - **Step 2** Subtract the expenses and add the amount raised by the parents to the account balance.

Step 3

Estimate:
$$$2300 - $700 + $600 = $2200$$

- **Step 5** The balance in the account is \$2158.
- **Step 6** The answer is reasonably close to the estimate. The expenses were \$734 \$568 = \$166 more than the amount raised, so the balance is lowered. \$2324 \$166 = \$2158.
- **37.** *Step 1* The costs of two hotels are given. Find the amount saved by staying at the less expensive hotel for seven nights.
 - **Step 2** First subtract the cost of the least expensive hotel and then multiply this savings by seven.

Step 3 Estimate:
$$$100 - $50 = $50$$

 $$50 \times 7 = 350

Step 4

Multiply.
$$$54$$
 $\times 7$
 $\hline 378

- Step 5 The savings for 7 nights is \$378.
- **Step 6** The answer is reasonably close to the estimate.

Check Lake Tahoe cost:
$$7 \times \$99 = \$693$$

Reno cost: $7 \times \$45 = \315
Difference: $\$693 - \$315 = \$378$

- **38.** *Step 1* The costs of two hotels are given. Find the amount saved by staying at the least expensive hotel for four nights.
 - **Step 2** First subtract the cost of the least expensive hotel and then multiply this savings by four.

Step 3 Estimate:
$$$600 - $100 = $500$$

 $$500 \times 4 = 2000

Step 4 Subtract.
$$$645$$
 Ritz-Carlton -74 Motel 6 $$571$

- **Step 5** The savings for 4 nights is \$2284.
- **Step 6** The answer is reasonably close to the estimate.

Check Ritz-Carlton cost:
$$4 \times \$645 = \$2580$$

Motel 6 cost: $4 \times \$74 = \296
Difference: $\$2580 - \$296 = \$2284$

- **39. Step 1** Find out how much money each team received given the amount of money raised, the expenses, and the number of teams.
 - **Step 2** Subtract the expenses from the amount raised, then divide the result by the number of teams.

Step 3 Estimate:
$$$8000 - $800 = $7200$$

 $$7200 \div 20 = 360

- Step 5 Each team received \$375.
- **Step 6** The answer is reasonably close to the estimate. **Check** $18 \times \$375 = \6750 \$6750 + \$838 = \$7588
- **40.** *Step 1* Find the total number of flats needed.
 - **Step 2** Add the eggs collected in the morning to the eggs collected in the afternoon and divide the total by the number of eggs in each flat.
 - **Step 3** Estimate: 4000 + 3000 = 7000 $7000 \div 30 \approx 230$

- Step 5 204 flats are needed for packing.
- **Step 6** The answer is reasonably close to the estimate. **Check** $30 \times 204 = 6120$ 6120 2575 = 3545
- 41. *Step 1* The total seating requirement is given along with the information needed to find the number of seats on the main floor. The number of rows of seats in the balcony is given and the number of seats in each row of the balcony must be found.
 - Step 2 First, the number of seats on the main floor must be found. Next, the number of seats on the main floor must be subtracted from the total number of seats to find the number of seats in the balcony. Finally, the number of seats in the balcony must be divided by the number of rows of seats in the balcony.
 - Step 3 Seats on main floor: $30 \times 25 = 750$ Seats in balcony: 1250 - 750 = 500Seats in each row in balcony: $500 \div 25 = 20$ Since we didn't round, our estimate matches our exact answer.
 - Step 4 See the calculations in Step 3.

- **Step 5** The number of seats in each row of the balcony is 20.
- **Step 6** The answer matches the estimate, as expected.
- Check Seats in balcony: $20 \times 25 = 500$ Seats on main floor: $30 \times 25 = 750$ Total seats: 500 + 750 = 1250
- **42.** *Step 1* Find the number of boxes each store will receive.
 - Step 2 Use multiplication to find the total number of grapevine wreaths made per year. Use division to find the number of boxes used per year and the number of boxes each store receives.
 - Step 3 Estimate:

 $24 \times 40 = 960$ wreaths per year $960 \div 6 = 160$ boxes per year $160 \div 5 = 32$ boxes per store

Since we didn't round, our estimate matches our exact answer.

- Step 4 See the calculations in Step 3.
- Step 5 Each store will receive 32 boxes.
- **Step 6** The answer matches the estimate, as expected.

Check Total number of boxes: $5 \times 32 = 160$ Boxed wreaths: $6 \times 160 = 960$ Wreaths made: $24 \times 40 = 960$

Chapter 1 Review Exercises

- 1. 6,573; thousands: 6; ones: 573
- **2.** 36,215; thousands: 36; ones: 215
- **3.** 105,724; thousands: 105; ones: 724
- **4.** <u>1,768,710,618</u>; billions: 1; millions: 768; thousands: 710; ones: 618
- 5. 728 is seven hundred twenty-eight.
- **6.** 15,310 is fifteen thousand, three hundred ten.
- 7. 319,215 is three hundred nineteen thousand, two hundred fifteen.
- **8.** 62,500,005 is sixty-two million, five hundred thousand, five.
- **9.** Ten-thousand, eight is 10,008.
- **10.** Two hundred million, four hundred fifty-five is 200,000,455.
- 11. $\begin{array}{r} \frac{1}{72} \\ +38 \\ \hline 110 \end{array}$

12.
$$\begin{array}{r} 1\\ 54\\ +67\\ \hline 121 \end{array}$$

14.
$$82\overset{1}{1}5$$
 9 $+7433$ $15,657$

15.
$$\begin{array}{r}
2 \stackrel{11}{130} \\
453 \\
8 107 \\
+ 296 \\
\hline
10,986
\end{array}$$

16.
$$\begin{array}{r}
221\\
5684\\
218\\
2960\\
+983\\
\hline
9845
\end{array}$$

17.
$$\begin{array}{r}
11 & 33 \\
5 & 732 \\
11,069 \\
37 \\
1595 \\
+22,169 \\
\hline
40,602
\end{array}$$

18.
$$\begin{array}{r}
131\\
3451\\
12,286\\
43\\
1291\\
+32,784\\
\hline
49,855
\end{array}$$

19.
$$64$$
 Check 28 -28 36 -46

24.
$$\begin{array}{c} 4111010 \\ 5210 \\ -883 \\ \hline 4327 \\ \end{array}$$
 Check $\begin{array}{c} 111 \\ 4327 \\ +883 \\ \hline 5210 \\ \end{array}$

26.
$$99, 704 \atop 99, 704$$
 Check $25,866 \atop -73,838 \atop 25,866$ $99,704$

29.
$$8(4) = 32$$

30.
$$8(8) = 64$$

31.
$$(5)(9) = 45$$

32.
$$(6)(7) = 42$$

33.
$$7 \cdot 8 = 56$$

34.
$$9 \cdot 9 = 81$$

35.
$$5 \times 4 \times 2$$

 $(5 \times 4) \times 2$
 $20 \times 2 = 40$

36.
$$9 \times 1 \times 5$$

 $(9 \times 1) \times 5$
 $9 \times 5 = 45$

37.
$$4 \times 4 \times 3$$

 $(4 \times 4) \times 3$
 $16 \times 3 = 48$

38.
$$2 \times 2 \times 2$$

 $(2 \times 2) \times 2$
 $4 \times 2 = 8$

39.
$$(6)(0)(8) = 0$$
 Any number times 0 equals 0.

40.
$$(7)(1)(6)$$
 $(7 \cdot 1) \cdot 6$ $7 \cdot 6 = 42$

41.
$$6 \cdot 1 \cdot 8$$

 $(6 \cdot 1) \cdot 8$
 $6 \cdot 8 = 48$

42.
$$7 \cdot 7 \cdot 0 = 0$$
 Any number times 0 equals 0.

43.
$$\begin{array}{c} 28 \\ \times 3 \\ \hline 84 \end{array}$$

45.
$$\begin{array}{r} 7 \\ 58 \\ \times 9 \\ \hline 522 \end{array}$$

47.
$$\begin{array}{r} 24 \\ 625 \\ \times 8 \\ \hline 5000 \end{array}$$

48.
$$\begin{array}{r} 53\\ 374\\ \times 8\\ \hline 2992 \end{array}$$

49.
$$\begin{array}{r} 113 \\ 1349 \\ \times 4 \\ \hline 5396 \end{array}$$

51.
$$7\overset{1}{4}\overset{1}{5}6$$

 $\times 2$
 $14,912$

52.
$$\begin{array}{c} 65 \\ 2880 \\ \times 7 \\ \hline 20,160 \end{array}$$

53.
$$\begin{array}{r}
1\\93,105\\
\times\\
\hline
465,525
\end{array}$$

54.
$$\begin{array}{r}
16,52\\
21,873\\
\times 8\\
\hline
174,984
\end{array}$$

55.
$$35$$
 $\times 25$
 $175 \leftarrow 5 \times 35$
 $70 \leftarrow 2 \times 35$
 875

58.
$$\begin{array}{c} 68 \\ \times 75 \\ \hline 340 \\ \leftarrow 5 \times 68 \\ \hline 476 \\ \hline 5100 \\ \end{array}$$

59.
$$472$$

$$\times 33$$

$$1416 \leftarrow 3 \times 472$$

$$1416$$

$$15,576$$

61. (use a calculator)
$$4051$$

$$\times 219$$

$$887,169$$

62. (use a calculator) 1527
$$\times$$
 328 $\overline{500,856}$

65.
$$318 \text{ sets}$$

$$\times \$64 \text{ cost per set}$$

$$1272$$

$$1908$$

$$\$20,352 \text{ total cost}$$

73.
$$20 \div 4 = 5$$

74.
$$35 \div 5 = 7$$

75.
$$42 \div 7 = 6$$

76.
$$18 \div 9 = 2$$

77.
$$\frac{54}{9} = 6$$

78.
$$\frac{36}{9} = 4$$

79.
$$\frac{49}{7} = 7$$

80.
$$\frac{0}{6} = 0$$

81.
$$\frac{148}{0}$$
 is undefined.

82.
$$\frac{0}{23} = 0$$

83.
$$\frac{64}{8} = 8$$

84.
$$\frac{81}{9} = 9$$

85.
$$4 | 328 |$$
 Check 82 $\times 4 | 328 |$ 328

86.
$$3 | 29^{2}4 |$$
 Check 98 $\times 3$ 294

89.
$$2704 \div 18$$

$$\begin{array}{r}
150 \\
18 \overline{\smash)2704} \\
\underline{18} \\
90 \\
\underline{90} \\
04 \\
\underline{00} \\
4
\end{array}$$

Check
$$150 \times 18$$

 1200×150
 150×150
 150×150
 150×150

91. 817 rounded to the nearest ten: 820

 $8\underline{1}7$ Next digit is 5 or more. Tens place changes (1+1=2). The digit to the right of the underlined place changes to zero.

92. 15,208 rounded to the nearest hundred: 15,200

15,<u>2</u>08 Next digit is 4 or less. Hundreds place does not change. All digits to the right of the underlined place change to zero.

93. 20,643 rounded to the nearest thousand: 21,000

20,643 Next digit is 5 or more. Thousands place changes (0+1=1). All digits to the right of the underlined place change to zero.

94. 67,485 rounded to the nearest ten-thousand: 70,000

 $\underline{67}$,485 Next digit is 5 or more. Ten-thousands place changes (6+1=7). All digits to the right of the underlined place change to zero.

95. To the nearest ten: $34\underline{8}7$

Next digit is 5 or more. Tens place changes (8+1=9). The digit to the right of the underlined place changes to zero. **3490**

To the nearest hundred: 3487

Next digit is 5 or more. Hundreds place changes (4+1=5). All digits to the right of the underlined place are changed to zero. **3500**

To the nearest thousand: 3487

Next digit is 4 or less. Thousands place does not change. All digits to the right of the underlined place are changed to zero. **3000**

96. To the nearest ten: 20,065

Next digit is 5 or more. Tens place changes (6+1=7). The digit to the right of the underlined place changes to zero. **20,070**

To the nearest hundred: 20,065

Next digit is 5 or more. Hundreds place changes (0+1=1). All digits to the right of the underlined place are changed to zero. **20,100**

To the nearest thousand: 20,065

Next digit is 4 or less. Thousands place does not change. All digits to the right of the underlined place are changed to zero. **20,000**

97. To the nearest ten: 98,201

Next digit is 4 or less. Tens place does not change. The digit to the right of the underlined place changes to zero. **98,200**

To the nearest hundred: 98,201

Next digit is 4 or less. Hundreds place does not change. All digits to the right of the underlined place are changed to zero. **98,200**

To the nearest thousand: 98,201

Next digit is 4 or less. Thousands place does not change. All digits to the right of the underlined place are changed to zero. **98,000**

98. To the nearest ten: 352,118

Next digit is 5 or more. Tens place changes (1+1=2). The digit to the right of the underlined place changes to zero. **352,120**

To the nearest hundred: 352,118

Next digit is 4 or less. Hundreds place does not change. All digits to the right of the underlined place are changed to zero. **352,100**

To the nearest thousand: $35\underline{2},118$

Next digit is 4 or less. Thousands place does not change. All digits to the right of the underlined place are changed to zero. **352,000**

- **99.** From the table, $4^2 = 16$, so $\sqrt{16} = 4$.
- **100.** From the table, $7^2 = 49$, so $\sqrt{49} = 7$.
- **101.** From the table, $12^2 = 144$, so $\sqrt{144} = 12$.
- **102.** From the table, $14^2 = 196$, so $\sqrt{196} = 14$.
- **103.** 7^3 : exponent is 3; base is 7. $7^3 = 7 \cdot 7 \cdot 7 = 343$
- **104.** 3^6 : exponent is 6; base is 3. $3^6 = 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 = 729$
- **105.** 5^3 : exponent is 3; base is 5. $5^3 = 5 \cdot 5 \cdot 5 = 125$
- **106.** 4^5 : exponent is 5; base is 4. $4^5 = 4 \cdot 4 \cdot 4 \cdot 4 = 1024$
- **107.** $7^2 15$ Exponent 49 15 = 34 Subtract.
- **108.** $6^2 10$ Exponent 36 10 = 26 Subtract.
- **109.** $2 \cdot 3^2 \div 2$ Exponent $2 \cdot 9 \div 2$ Multiply. $18 \div 2 = 9$ Divide.
- 110.
 $9 \div 1 \cdot 2 \cdot 2 \div (11 2)$ Parentheses

 $9 \div 1 \cdot 2 \cdot 2 \div 9$ Divide.

 $9 \cdot 2 \cdot 2 \div 9$ Multiply.

 $18 \cdot 2 \div 9$ Multiply.

 $36 \div 9 = 4$ Divide.

111.
$$\sqrt{9} + 2(3)$$
 Square root $3 + 2 \cdot 3$ Multiply. $3 + 6 = 9$ Add.

112.
$$6 \cdot \sqrt{16} - 6 \cdot \sqrt{9}$$
 Square root $6 \cdot 4 - 6 \cdot 3$ Multiply. $24 - 18 = 6$ Subtract.

- 113. From the bar graph, 8 parents out of 100 nagged their children about washing hands after using the bathroom.
- **114.** From the bar graph, 5 parents out of 100 nagged their children about taking shoes off when coming inside.
- **115.** From the bar graph, the greatest number of parents, 25, nagged their children about keeping bedroom clean.
- **116.** From the bar graph, the least number of parents, 3, nagged their children about hanging up wet bath towels.

117. Estimate: 40 million
$$\times$$
 365 \times 400 \times 40 \times 16 000

 $40 \text{ million} \times 400 = 16,000 \text{ million or}$ 16,000,000,000 checks (*Attach* 000 000.)

Exact: 40 million
$$\times$$
 365 \times 40 \times 40 \times 40

 $40 \text{ million} \times 365 = 14,600 \text{ million or}$ 14,600,000,000 checks (Attach 000 000.)

The bank processes 14,600 million checks in a year.

- **118.** *Step 1* Find the total revolutions.
 - **Step 2** We know the revolutions per minute and the number of minutes.

Step 3 An estimate is $1000 \times 60 = 60,000$ revolutions.

Step 4 $1400 \times 60 = 84{,}000$ revolutions

Step 5 There were 84,000 revolutions.

Step 6 The answer is reasonably close to the estimate considering the rounding.

Check
$$84,000 \div 60 = 1400$$

- **119.** *Step 1* Find the difference in the populations of California and Texas.
 - Step 2 Difference indicates subtraction.

Step 3 An estimate is 40,000,000 - 30,000,000 = 10,000,000 people.

- *Step 5* The difference in population is 12,073,571.
- **Step 6** The answer is reasonably close to the estimate.

Check 12,073,571 + 25,268,418 = 37,341,989

- **120.** *Step 1* Find the difference in the populations of Alaska and Wyoming.
 - Step 2 Difference indicates subtraction.
 - **Step 3** An estimate is 700,000 600,000 = 100,000 people.

- Step 5 The difference in population is 153,223.
- **Step 6** The answer is reasonably close to the estimate. **Check** 153,223 + 568,300 = 721,523
- **121.** *Step 1* Find the total cost to replace her transmission.
 - **Step 2** Add the cost of the transaxle, the labor (multiply the number of hours times the hourly rate), and the sales tax.

Step 3 Estimate:

Transaxle: round \$2633 to \$3000

Labor: $8 \times \$90 = \720 Tax: round \$230 to \$200

Total: \$3000 + \$720 + \$200 = \$3920

Step 4 Exact:

Transaxle: \$2633Labor: $8 \times $90 = 720

Tax: \$230

Total: \$2633 + \$720 + \$230 = \$3583

- Step 5 The total cost is \$3583.
- **Step 6** The answer is reasonably close to the estimate. Check by repeating Step 4.
- **122.** *Step 1* Find the total cost to rent a truck.
 - **Step 2** Add the cost of the rental and the cost of the mileage (multiply the number of miles times the rate per mile).

Step 3 Estimate:

Rental: round \$55 to \$60

Mileage: round 89 to 90 and multiply by \$2,

 $90 \times \$2 = \180

Total: \$60 + \$180 = \$240

Step 4 Exact:

Rental: \$55

Mileage: $89 \times \$2 = \178 Total: \$55 + \$178 = \$233

Step 5 The total cost is \$233.

Step 6 The answer is reasonably close to the estimate. Check by repeating Step 4.

123. *Step 1* Find the total cost to buy the ovens.

Step 2 Multiply the number of baking ovens times the cost of each baking oven and the number of warming ovens times the cost of each warming oven. Add to find the total cost.

Step 3 Estimate:

Baking ovens: $30 \times \$2000 = \$60,000$ Warming ovens: $30 \times \$900 = \$27,000$ Total: \$60,000 + \$27,000 = \$87,000

Step 4 Exact:

Baking ovens: $32 \times $1538 = $49,216$ Warming ovens: $28 \times $887 = $24,836$ Total: \$49,216 + \$24,836 = \$74,052

Step 5 The total cost is \$74,052.

Step 6 The answer is reasonably close to the estimate. Check by repeating Step 4.

124. *Step 1* Find the total monthly collections.

Step 2 We know the number of daily customers and the daily rate. We know the number of weekend-only customers and the rate.

Number of customers × daily rate + number of customers × weekend rate = total collections.

Step 3 Estimate:

$$(60 \times \$20) + (20 \times \$7) = \$1200 + \$140 = \$1340$$

Step 4 Exact:

 $(62 \times \$16) + (21 \times \$7) = \$992 + \$147 = \$1139$

Step 5 The total monthly collections are \$1139.

Step 6 The answer is reasonably close to the estimate. Check by repeating Step 4.

125. *Step 1* Find the difference in the amount spent on others and the amount spent on themselves.

Step 2 Difference indicates subtraction.

Step 3 An estimate is \$600 - \$100 = \$500.

Step 4 Exact: \$620 - \$107 - \$513

Step 5 The difference in amount spent is \$513.

Step 6 The answer is reasonably close to the estimate. **Check** \$513 + \$107 = \$620

126. *Step 1* Find the new account balance.

Step 2 We know the amount of the payments and the old balance.

Old balance - payment amounts = new balance.

Step 3 Estimate:

\$2000 - \$500 - \$400 = \$1100

Step 4 Exact:

1924 - 520 - 385 = 1019

Step 5 She has \$1019 in her bank account.

Step 6 The answer is reasonably close to the estimate. Check \$1019 + \$520 + \$385 = \$1924

127. *Step 1* Find out how many pounds of pork are needed.

Step 2 We know the total number of cans and we must divide that total by 175 since each group of 175 cans requires 1 pound of pork. The number of groups \times 1 pound = total pounds.

Step 3 Estimate: $9000 \div 200 = 45$ pounds

Step 4 $\frac{8750}{175} = 50$ pounds

Step 5 50 pounds of pork are needed.

Step 6 The answer is reasonably close to the estimate. **Check**

 $(175 \text{ cans per pound}) \cdot (50 \text{ pounds}) = 8750 \text{ cans}$

128. *Step 1* Find how many hours it takes to produce all the plates.

Step 2 We know the total number of plates and we know how many are produced each hour.

 $\frac{total\ number}{number\ per\ hour} = total\ hours$

Step 3 An estimate: $30,000 \div 1000 = 30$ hours

Step 4 $\frac{32,538}{986} = 33 \text{ hours}$

Step 5 It will take 33 hours.

Step 6 The answer is reasonably close to the estimate. **Check** $33 \cdot 986 = 32,538$

129. *Step 1* Find the total number of acres fertilized.

Step 2 We know the total amount of fertilizer and how much each acre needs. Total pounds ÷ pounds needed per acre = total acres.

Step 3 Estimate: $30,000 \div 600 = 50$

Step 4 $\frac{32,500}{625} = 52 \text{ acres}$

Step 5 52 acres can be spread with 32,500 pounds of nitrogen sulfate.

Step 6 The answer is reasonably close to the estimate. **Check** $52 \times 625 = 32{,}500$

130. *Step 1* Find the number of homes that can be fenced.

Step 2 Divide the number of feet of fencing available by the number of feet needed for each home.

Step 3 Estimate: $6000 \div 200 = 30$ homes

Step 4
$$\frac{5760}{180} = 32$$
 homes

Step 5 32 homes can be fenced.

Step 6 The answer is reasonably close to the estimate. **Check**

 $(180 \text{ feet per home}) \cdot (32 \text{ homes}) = 5760 \text{ feet}$

131. [1.4]
$$4(83)$$
 $\frac{1}{83}$ $\times 4$ 332

133. [1.3]
$$\begin{array}{c} 210 \\ 309 \\ -56 \\ \hline 253 \end{array}$$

134. [1.3]
$$\begin{array}{c} 7 & 2 & 15 \\ 7 & 2 & 15 \\ 8 & 3 & 5 \\ \hline -2 & 4 & 7 \\ \hline 5 & 8 & 8 \end{array}$$

135. [1.2]
$$\begin{array}{c} 1 & 1 \\ 6 & 6 \\ 2 \\ +379 \\ \hline 1041 \end{array}$$

136. [1.2]
$$\begin{array}{r} 11\\789\\+872\\\hline 1661\end{array}$$

137. [1.3]
$$\begin{array}{c} 38, 13 & 0 \\ 3310 \\ -6078 \\ \hline 32.062 \end{array}$$
 Check
$$\begin{array}{c} 32, 062 \\ +6078 \\ \hline 38.140 \end{array}$$

139. [1.5]
$$21 \div 7 = 3$$

140. [1.5]
$$\frac{42}{6} = 7$$
 $(7 \cdot 6 = 42)$

143. [1.5]
$$\frac{9}{0}$$
 is undefined.

144. [1.5]
$$\frac{7}{1} = 7$$
 $(7 \cdot 1 = 7)$

145. [1.5]
$$27,600 \div 4 = 6900$$

$$4 \overline{\smash{\big)}\ 27^{3}6} \quad \textit{Attach } 00.$$

146. [1.5]
$$18,480 \div 8$$

$$\begin{array}{r} 2 \ 3 \ 10 \\ 8 \overline{18,^{2}480} \end{array}$$

147. [1.4]
$$\begin{array}{r} 8 & 430 \\ \times & 128 \\ \hline \hline 67 & 440 & \leftarrow 8 \times 8430 \\ 168 & 60 & \leftarrow 2 \times 8430 \\ \hline 843 & 0 \\ \hline \hline 1,079,040 \end{array}$$

148. [1.4]
$$\begin{array}{r}
14, & 1 \\
21, & 702 \\
\times & 6 \\
\hline
130, & 212
\end{array}$$

149. [1.6] Use a calculator to show that

$$34 \overline{)3672} = 108.$$

150. [1.6] Use a calculator to show that

$$68 \overline{14, 076} = 207.$$

- **151. [1.1]** 376,853 is three hundred seventy-six thousand, eight hundred fifty-three in words.
- **152.** [1.1] 408,610 is four hundred eight thousand, six hundred ten in words.

- 153. [1.7] 8749 rounded to the nearest hundred: 8749 Next digit is 4 or less. Hundreds place doesn't change. All digits to the right of the underlined place are changed to zero. 8700
- **154. [1.7]** 400,503 rounded to the nearest thousand: 400,503

Next digit is 5 or more. Thousands place changes (0+1=1). All digits to the right of the underlined place are changed to zero. **401,000**

- **155.** [1.8] From the table, $8^2 = 64$, so $\sqrt{64} = 8$.
- **156.** [1.8] From the table, $9^2 = 81$, so $\sqrt{81} = 9$.
- 157. [1.4] \$308 cost per pair $\times 18 pairs$ $\hline 2464$ $\hline 308$ $\hline $5544 total cost$
- 158. [1.4] \$370 cost per dishwasher

 × 84 dishwashers

 1480

 2960

 \$31.080 total cost
- 159. [1.4] 208 baseball hats \times \$11 cost of hat 208 208 82288 total cost
- 160. [1.4] $607 \ boxes \ of \ avocados$ $\times \$26 \ cost \ per \ box$ $\hline 3642$ $\hline 1214$ $\hline \$15,782 \ total \ cost$

There are 468 cards in nine decks.

162. [1.4] 1700 volunteers $\times 31$ pounds per volunteer $\overline{52,700}$ pounds

There were 52,700 pounds of fruits and vegetables picked by the volunteers.

A "push-type" mower costs \$280.

164. [1.3]
$$\begin{array}{c} \$21\$,4\$10 \\ -\$103,815 \\ \hline \$114,635 \end{array}$$
 Amount needed
Amount raised

\$114,635 more needs to be raised.

165. [1.10] Multiply the number of rentals times the sum of the rental fee and the launch fee.

$$\begin{array}{lll} \text{4-person} & 6 \times (\$28 + \$2) = 6(\$30) & \$180 \\ \text{6-person} & 15 \times (\$38 + \$2) = 15(\$40) & 600 \\ 10\text{-person} & 10 \times (\$70 + \$2) = 10(\$72) & 720 \\ 12\text{-person} & 3 \times (\$75 + \$2) = 3(\$77) & 231 \\ 16\text{-person} & 2 \times (\$85 + \$2) = 2(\$87) & + 174 \\ \hline \$1905 & & \$1905 \\ \end{array}$$

Total receipts were \$1905.

166. [1.10] Multiply the number of rentals times the sum of the rental fee and the launch fee.

Total receipts were \$12,420.

The Burj Dubai is 1467 feet taller than the Empire State Building.

168. [1.9]
$$1\stackrel{6}{7}\stackrel{17}{7}6$$
 1 WTC in New York -1483 Petronas Towers 293 difference

The 1 WTC in New York will be 293 feet taller than the Petronas Towers.

The combined height of these seven buildings is 11,958 feet.

(b) Two miles is the same as $2 \times 5280 = 10{,}560$ feet, so the combined height is greater than two miles.

$$11,958$$
 8 combined height $-10,560$ feet in two miles 1398 difference

The combined height of the seven buildings is 1398 feet more than a two miles.

170. [1.9] One yard is the same as three feet, so 100 yards is the same as 300 feet. The Willis Tower is 1451 feet tall, so divide 1451 by 300.

$$\begin{array}{r}
 4 \\
300 \overline{\smash{\big)}\ 1451} \\
 \underline{1200} \\
 251
\end{array}$$

The height of the Willis Tower is equivalent to more than the length of 4 football fields (a little less than 5).

Chapter 1 Test

- 1. 9205 is nine thousand, two hundred five.
- 2. 25,065 is twenty-five thousand, sixty-five.
- **3.** Four hundred twenty-six thousand, five is 426,005.

4.
$$\begin{array}{r} 122\\853\\66\\4022\\+3589\\\hline8530\\ \end{array}$$

5.
$$\begin{array}{r}
11,12\\
17,063\\
7\\
12\\
1505\\
93,710\\
+333\\
\hline
112,630
\end{array}$$

7.
$$\begin{array}{r}
810615 \\
9075 \\
-2869 \\
\hline
6206
\end{array}$$

8.
$$7 \times 6 \times 4 = (7 \times 6) \times 4 = 42 \times 4 = 168$$

 $57 \cdot 3000 = 171,000$ Attach 000.

10. 85(19)

13. $\frac{835}{0}$ is undefined

15.
$$\begin{array}{r}
160 \\
280 \overline{\smash)44,800} \\
\underline{280} \\
1680 \\
\underline{1680} \\
00
\end{array}$$

16. 6347 rounded to the nearest ten: 6347

Next digit is 5 or more. Tens place changes (4+1=5). The digit to the right of the underlined place changes to zero. **6350**

17. 76,489 rounded to the nearest thousand: 76,489

Next digit is 4 or less. Thousands place does not change. All digits to the right of the underlined place change to zero. **76,000**

- 18. $5^2 + 8(2)$ Exponent 25 + 8(2) Multiply. 25 + 16 = 41 Add.
- **19.** $7 \cdot \sqrt{64} 14 \cdot 2$ Square root $7 \cdot 8 14 \cdot 2$ Multiply. 56 28 = 28 Subtract.
- **20.** Estimate:

$$$500 + $500 + $500 + $400 - $800 = $1100$$

Exact: Add the rent collected.

$$\begin{array}{r} 1 & 11 \\ 5 & 485 \\ 500 \\ 515 \\ + & 425 \\ \hline \$1925 \end{array}$$

Subtract expenses.

$$$1\ ^{812}_{92}5 \\ -785_{$1140}$$
 amount left

She has \$1140 left.

21. Estimate: $90,000 \div 400 = 225$ acres

Exact: Divide the total number of gallons by the number of gallons produced from one acre.

It would take 231 acres.

22. Estimate: \$2000 - \$500 - \$200 - \$200 = \$1100Exact: \$1906 - \$528 - \$195 - \$235 = \$948

Her new balance is \$948.

23. If we multiply the number of identifications each minute, 48, by the number of minutes in an hour, 60, and then multiply that number by the number of hours, 4, we'll get the total number of identifications in 4 hours.

Estimate:
$$(50 \times 60 \times 4) + (40 \times 60 \times 3)$$

= $(3000 \times 4) + (2400 \times 3)$
= $12,000 + 7200 = 19,200$ chicks

Exact:
$$(48 \times 60 \times 4) + (36 \times 60 \times 3)$$

= $(2880 \times 4) + (2160 \times 3)$
= $11,520 + 6480 = 18,000$ chicks

The total number of baby chicks identified is 18,000.

- **24.** (1) Locate the place to which you are rounding and underline it.
 - (2) Look only at the next digit to the right. If this digit is a 4 or less, do not change the underlined digit. If the digit is a 5 or more, increase the underlined digit by 1.
 - (3) Change all digits to the right of the underlined place to zeros.

Each person's example will vary, but the following two examples illustrate the two general cases.

- (A) 124,999 rounds to 120,000
- (B) 125,000 rounds to 130,000
- **25.** (1) Read the problem carefully.
 - (2) Work out a plan.
 - (3) Estimate a reasonable answer.
 - (4) Solve the problem.
 - (5) State the answer.
 - (6) Check your work.